

Big Data and Data Mining

Week 3/4: Classification



Fenerbahce University

Instructors

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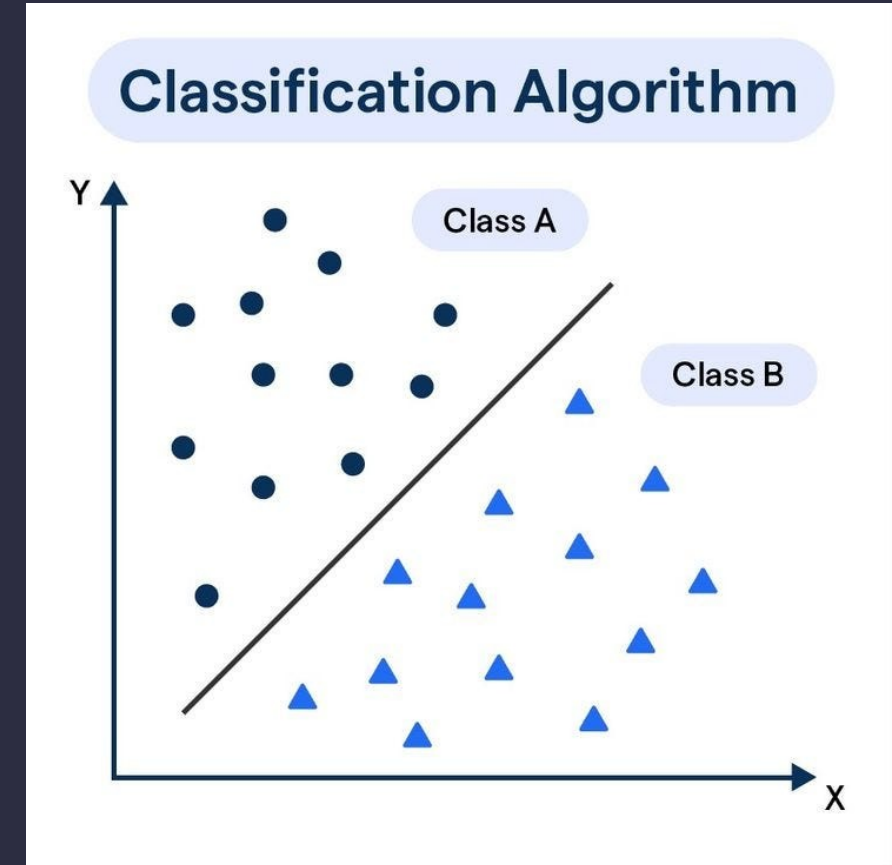
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Classification

- What is classification?
- Issues regarding classification
- Bayesian Classification
- Classification by decision tree induction
- Classification by Neural Networks
- Classification by Support Vector Machines (SVM)
- Instance Based Methods
- Classification accuracy
- Summary

Classification

- **Classification:**
 - predicts categorical class labels
 - classifies data (constructs a model) based on the training set and the values (**class labels**) in a classifying attribute and uses it in classifying new data



Classification

- Classification:
- Typical Applications
 - credit approval
 - target marketing
 - medical diagnosis
 - treatment effectiveness analysis

COVID-19 Radiography Database



COVID-19



lung opacity



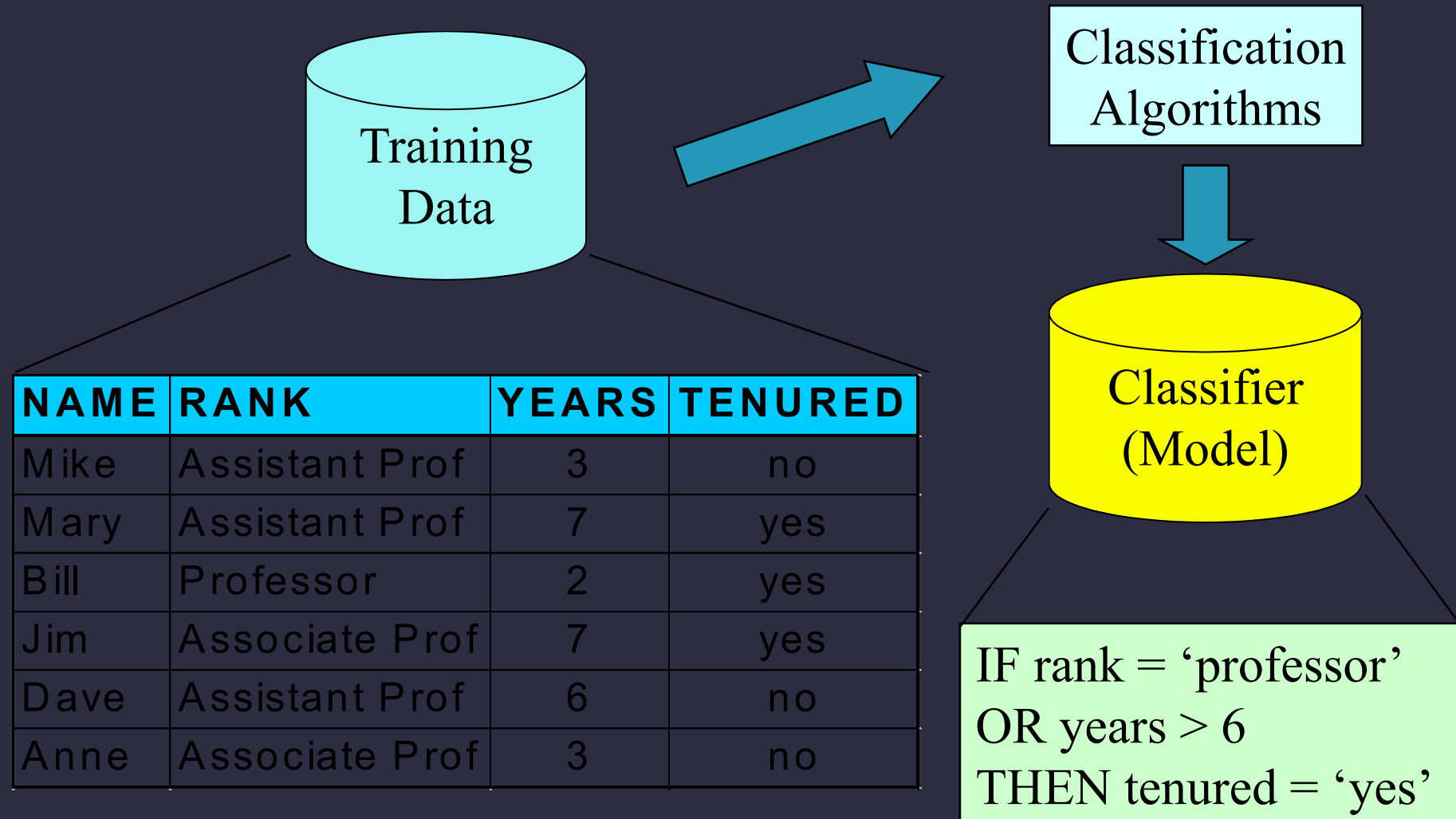
normal



viral pneumonia

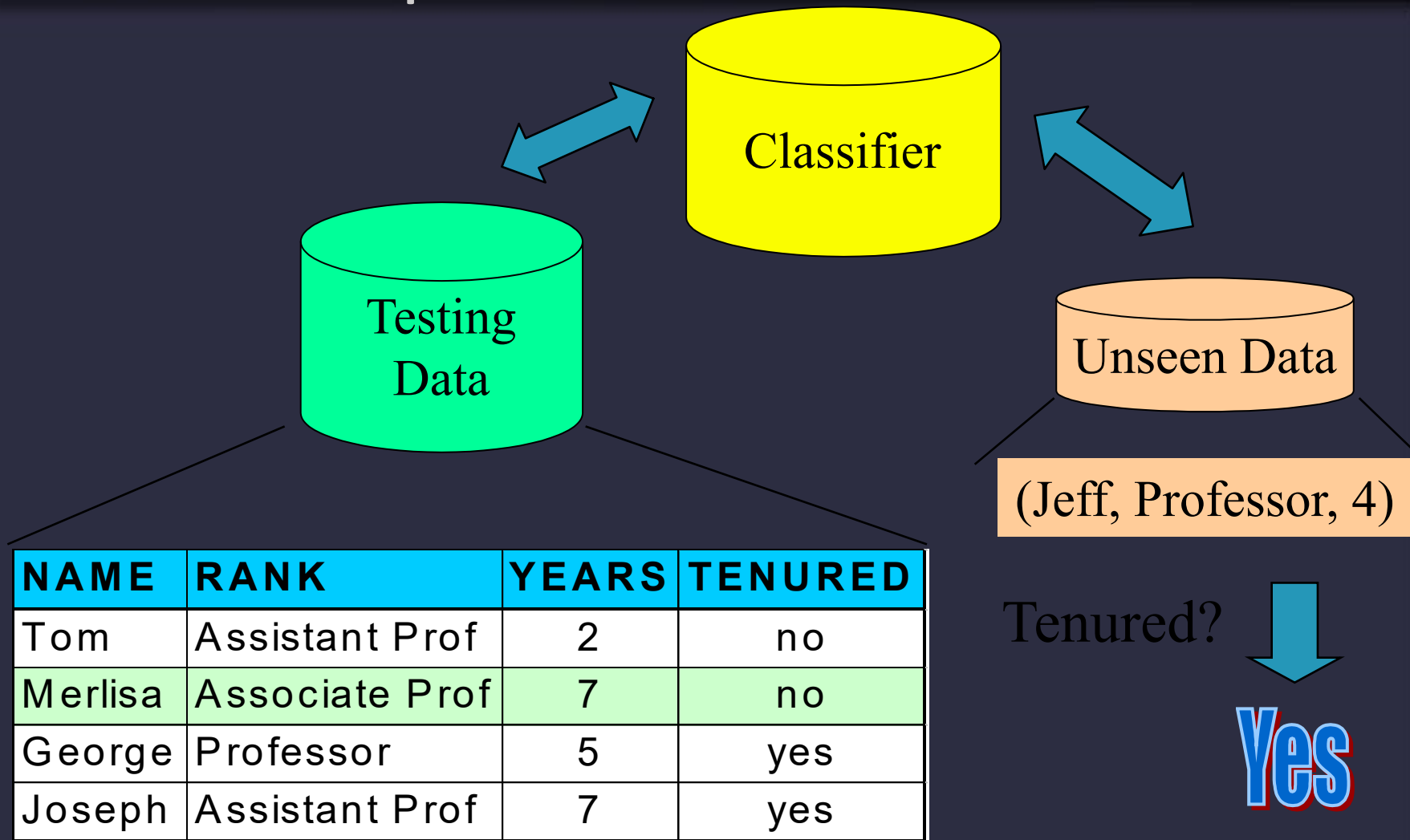
Classification—A Two-Step Process

- **Model construction:** describing a set of predetermined classes
 - Each sample is assumed to belong to a predefined class, as determined by the **class label attribute**
 - The set of sample used for model construction is **training set**
 - The model is represented as classification rules, decision trees, or mathematical formula or AI



Classification—A Two-Step Process

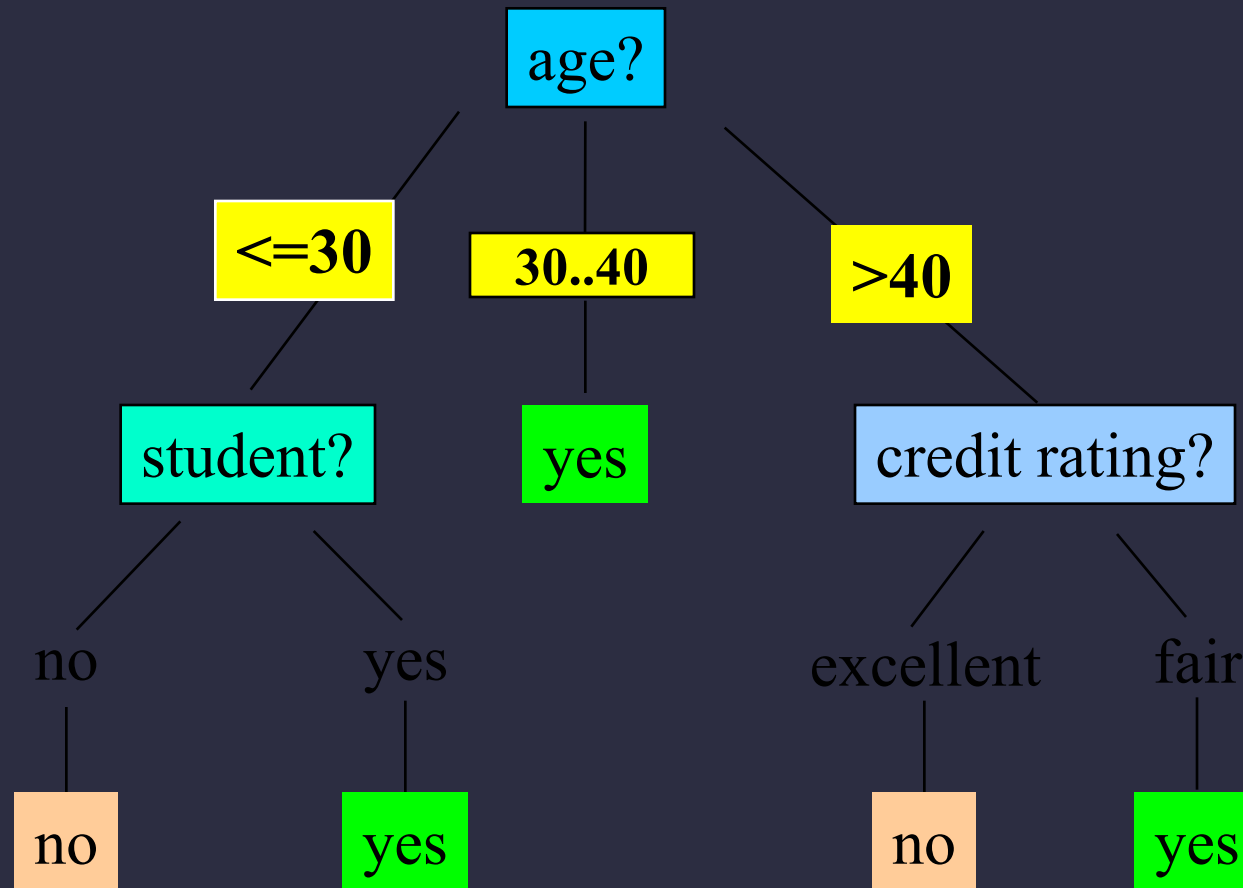
- **Model usage:** for classifying future or unknown objects
 - Estimate accuracy of the model
 - The known label of test sample is compared with the classified result from the model
 - Accuracy rate is the percentage of test set samples that are correctly classified by the model
 - Test set is independent of training set, otherwise over-fitting will occur
 - If the accuracy is acceptable, use the model to classify data tuples whose class labels are not known



Dataset for computer buyers

age	income	student	credit_rating	buys_computer
<=30	high	no	fair	no
<=30	high	no	excellent	no
31...40	high	no	fair	yes
>40	medium	no	fair	yes
>40	low	yes	fair	yes
>40	low	yes	excellent	no
31...40	low	yes	excellent	yes
<=30	medium	no	fair	no
<=30	low	yes	fair	yes
>40	medium	yes	fair	yes
<=30	medium	yes	excellent	yes
31...40	medium	no	excellent	
31...40	high	yes	fair	
>40	medium	no	excellent	

A Decision Tree for “*buys_computer*”

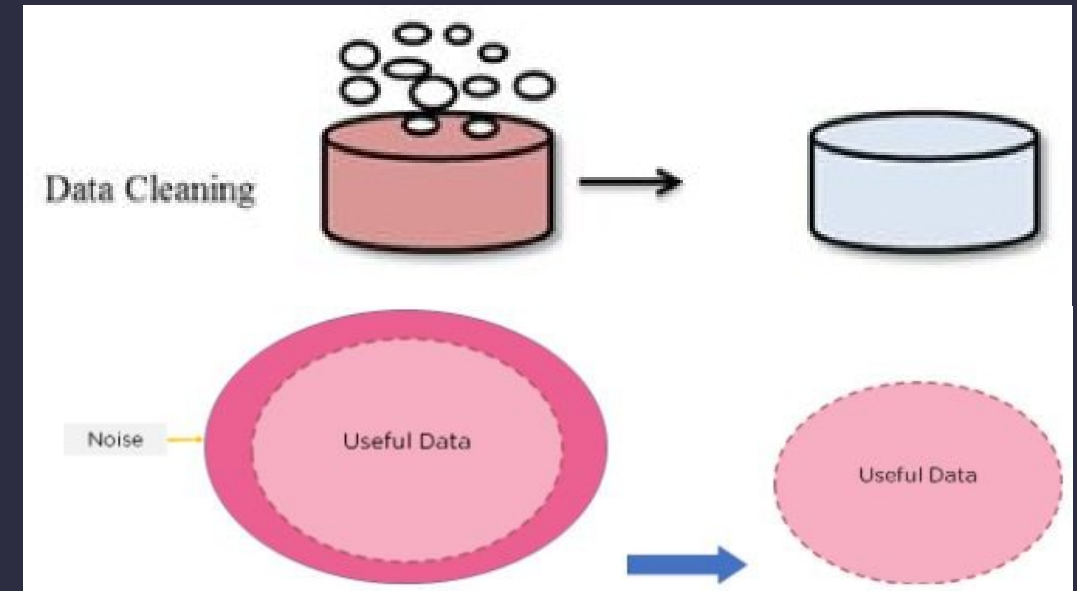


Classification

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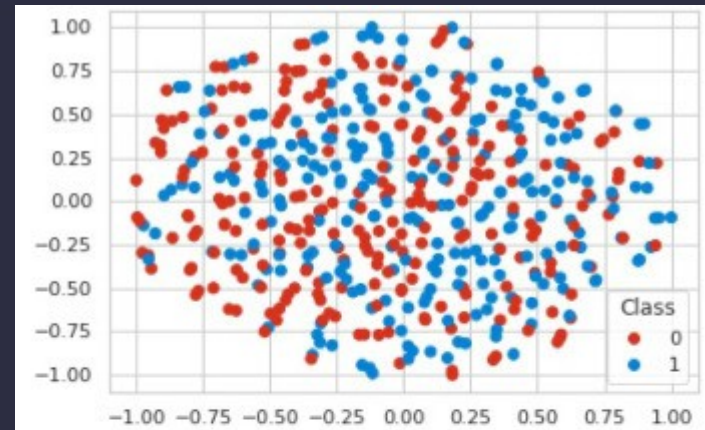
Issues (1): Data Preparation

- Data cleaning
 - Preprocess data in order to reduce noise and handle missing values

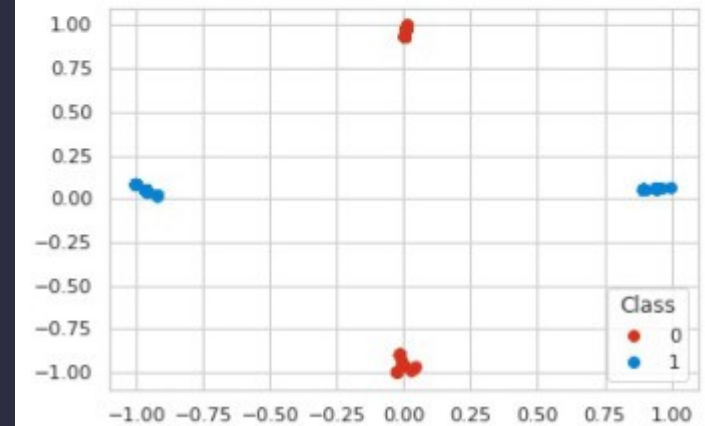


Issues (1): Data Preparation

- Relevance analysis (feature selection)
 - Remove the irrelevant or redundant attributes



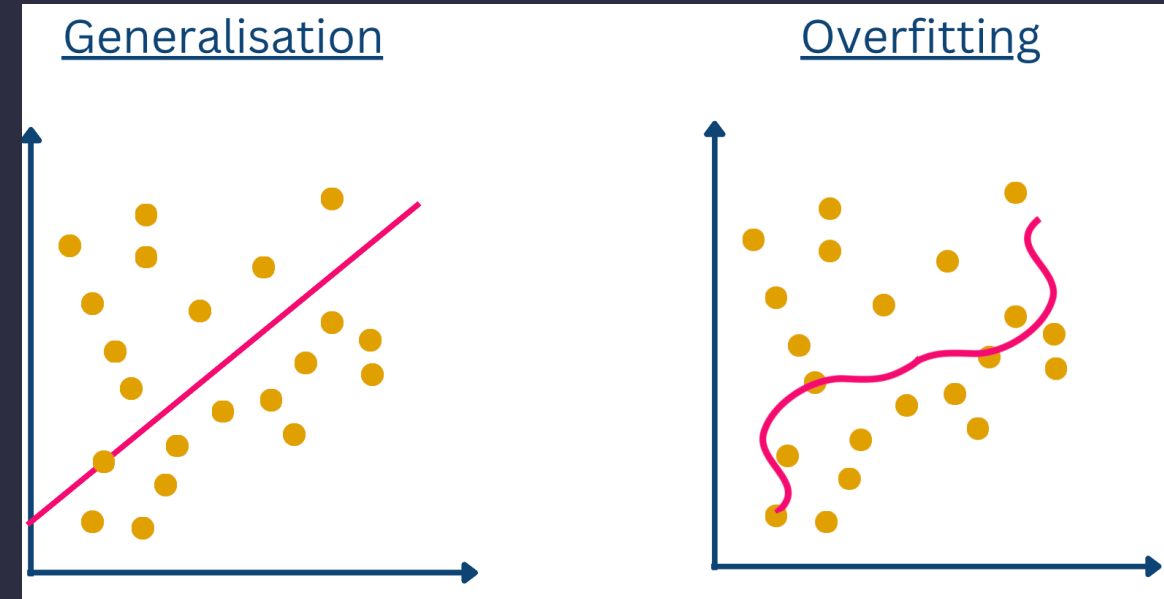
(a) All features



(b) Informative features

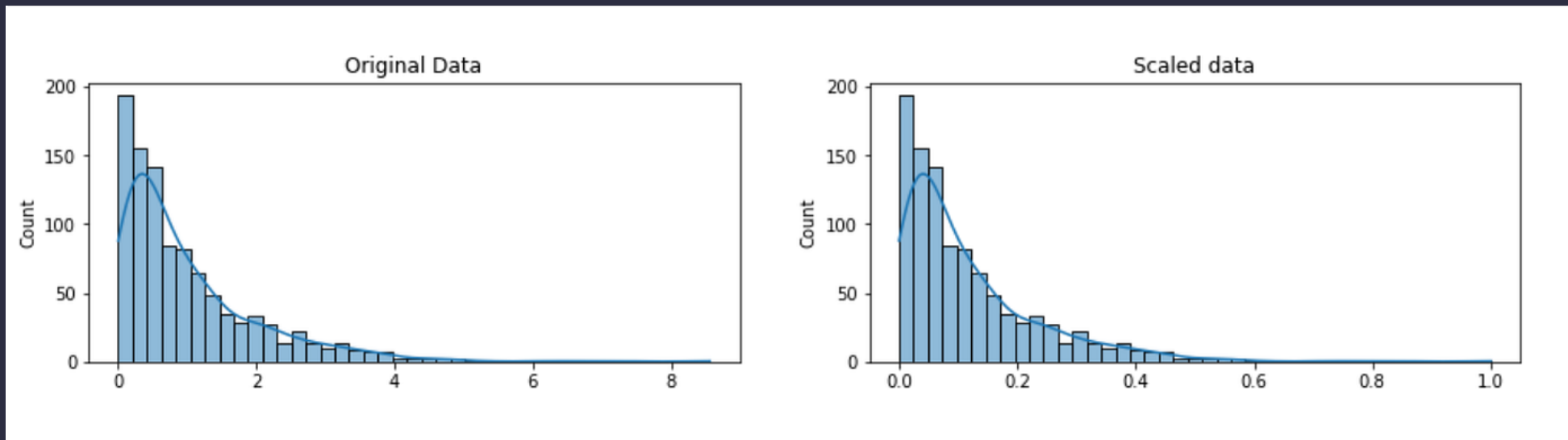
Issues (1): Data Preparation

- Data transformation
 - Generalize and/or normalize data



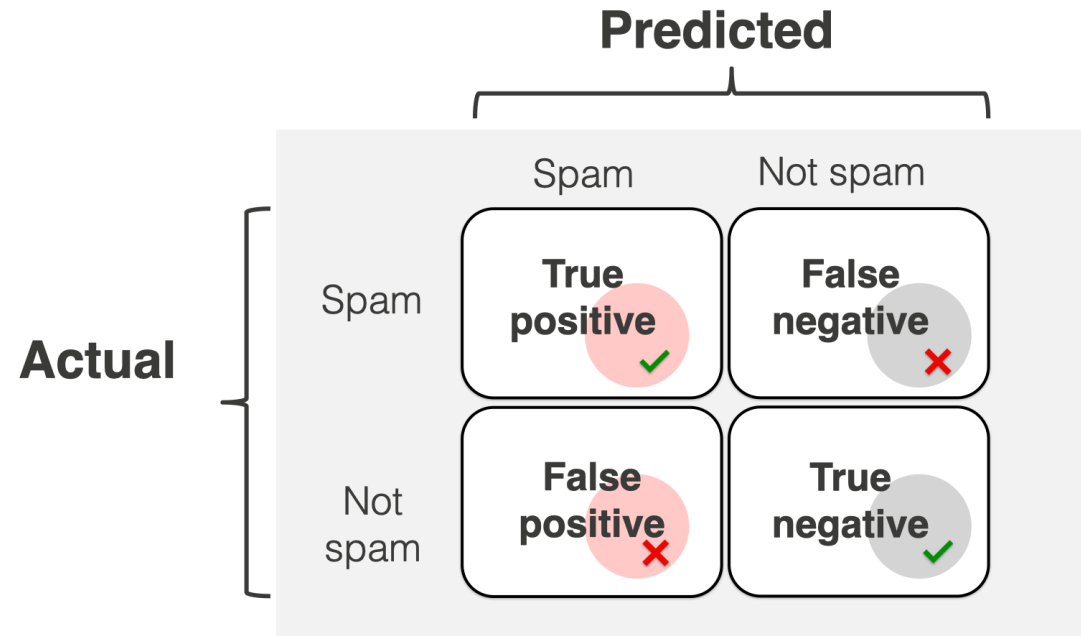
Issues (1): Data Preparation

- Data transformation
 - Generalize and/or normalize data



Issues (2): Evaluating Classification Methods

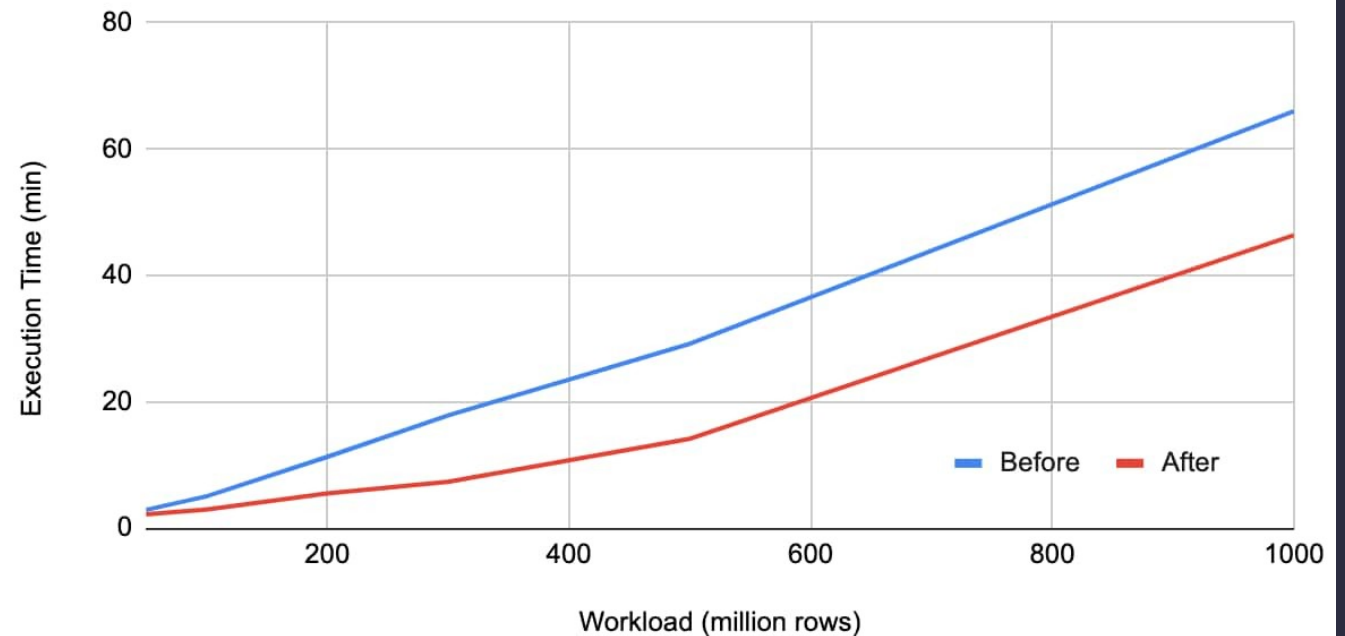
- Predictive accuracy



Issues (2): Evaluating Classification Methods

- Speed and scalability
 - time to construct the model
 - time to use the model

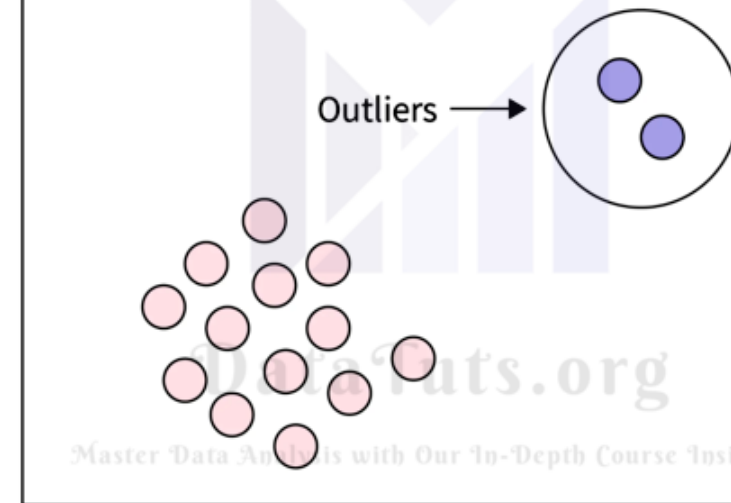
Model Execution Time (min) Before v.s. After Optimizations



Issues (2): Evaluating Classification Methods

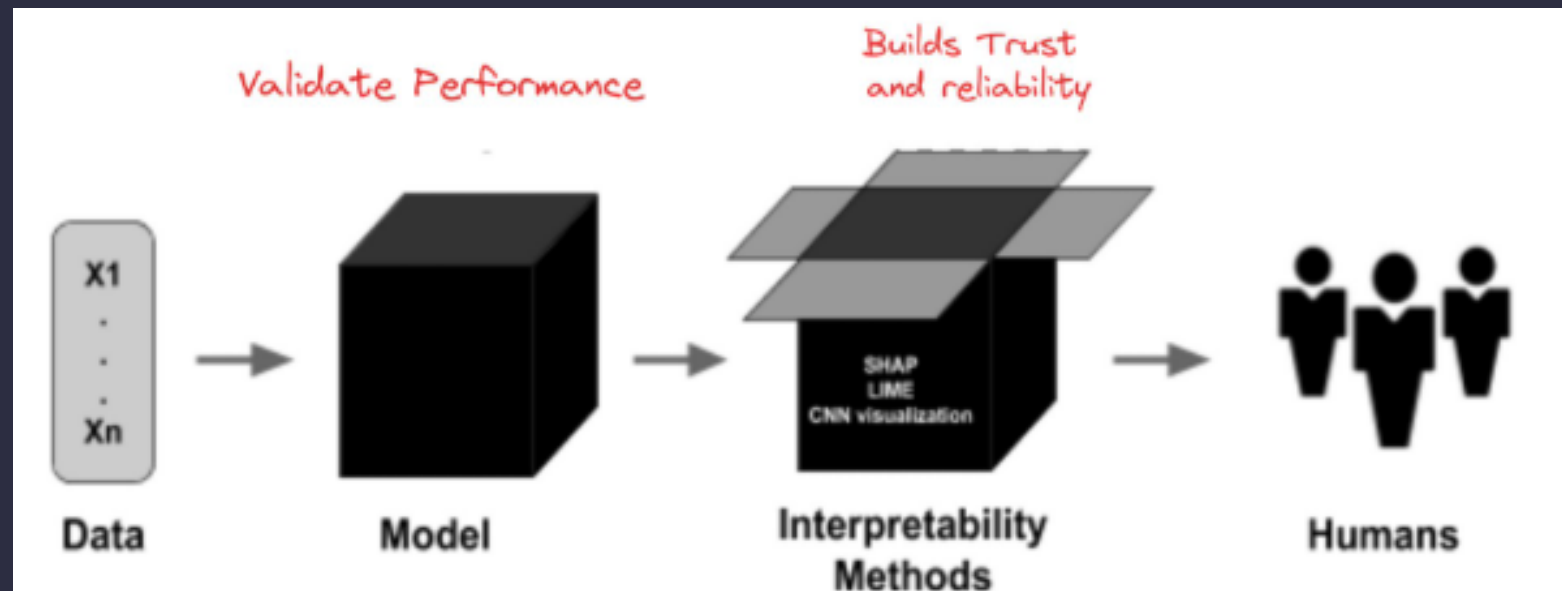
- Robustness
 - handling noise and missing values

Handling Missing Data, Outliers and noisy data



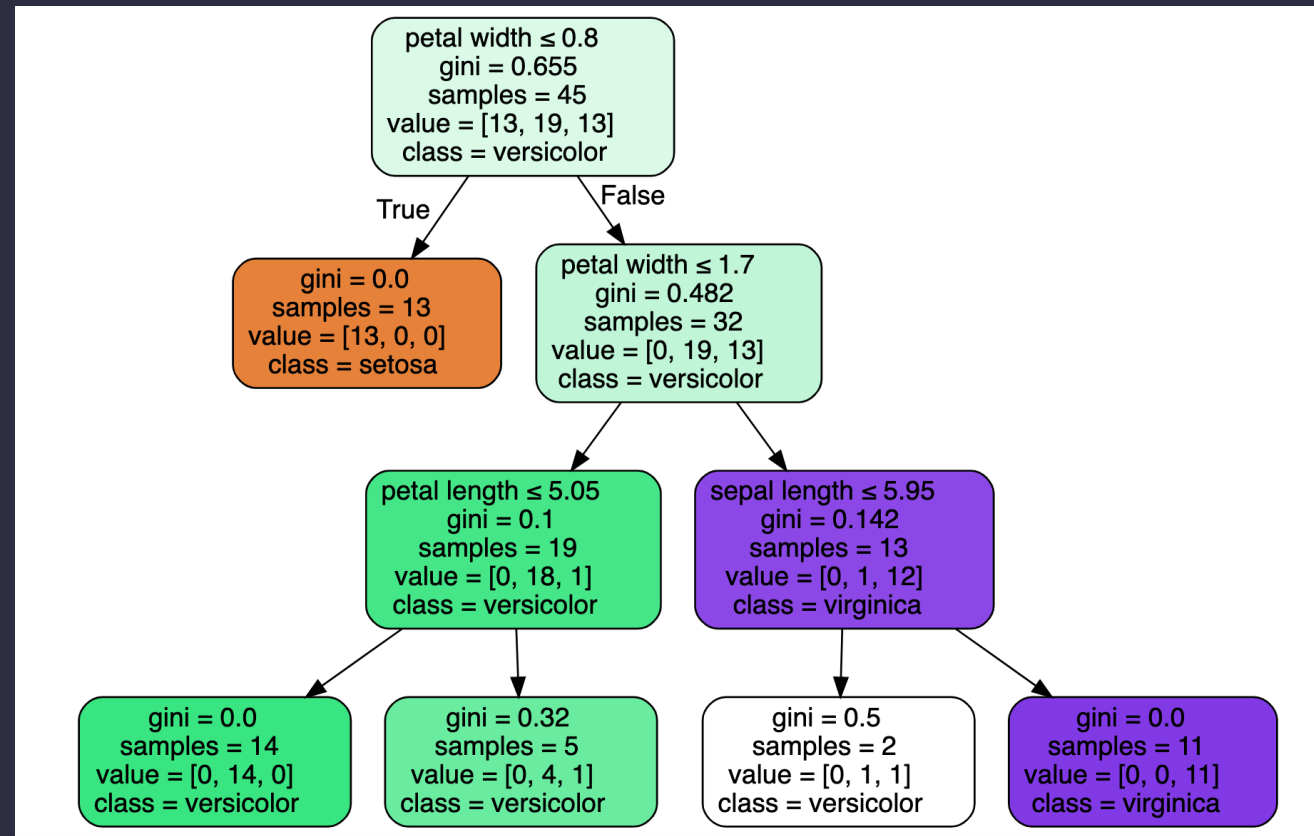
Issues (2): Evaluating Classification Methods

- Interpretability:
 - understanding and insight provided by the model



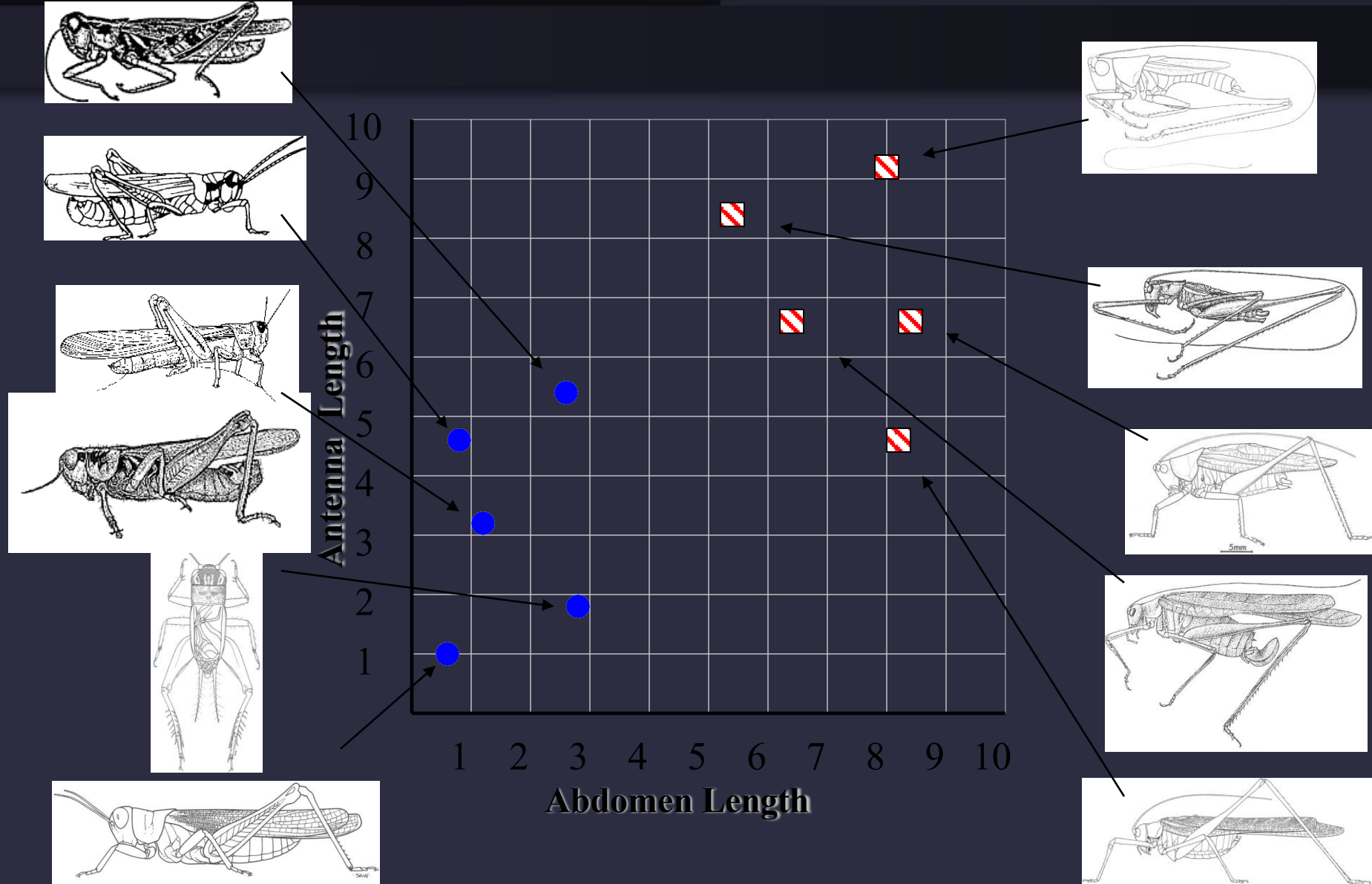
Issues (2): Evaluating Classification Methods

- Goodness of rules
 - decision tree size
 - compactness of classification rules

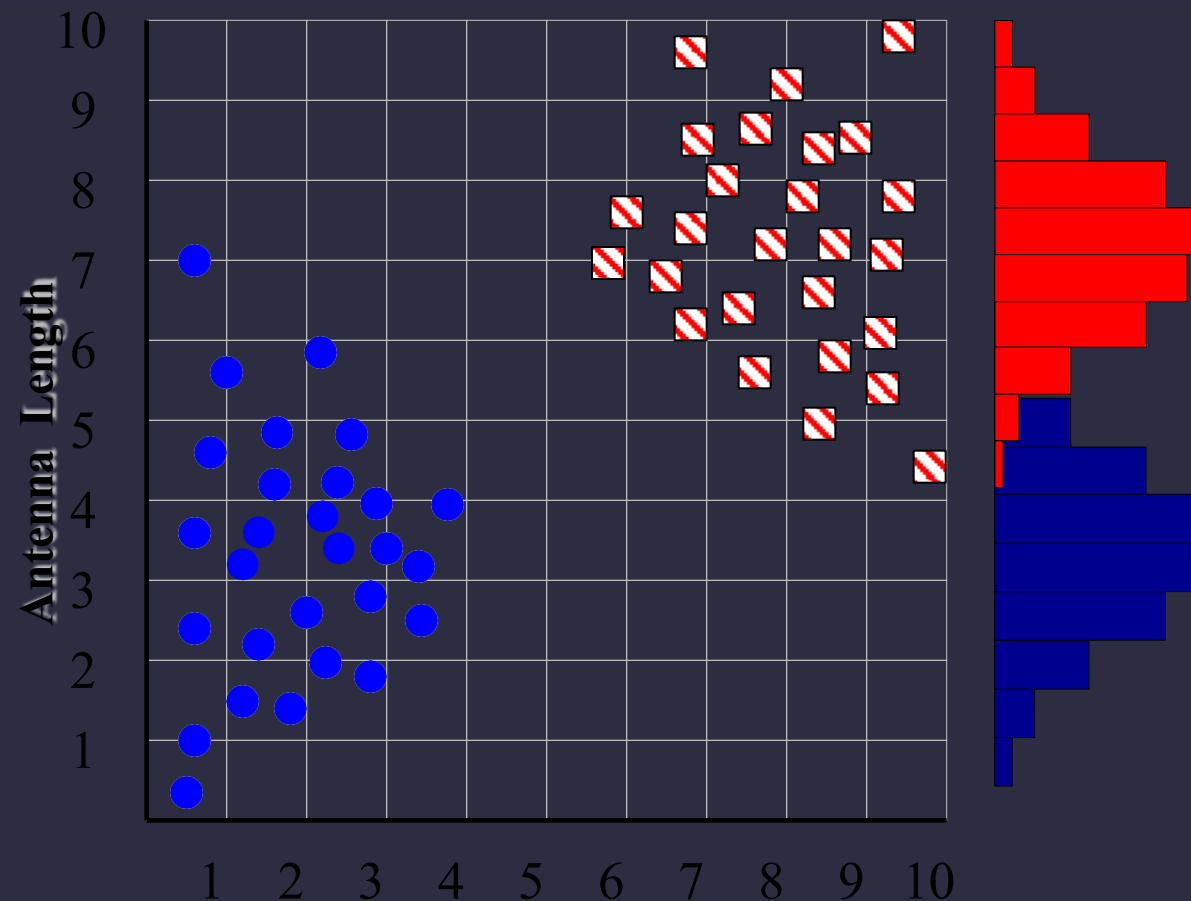


Grasshoppers

Katydid



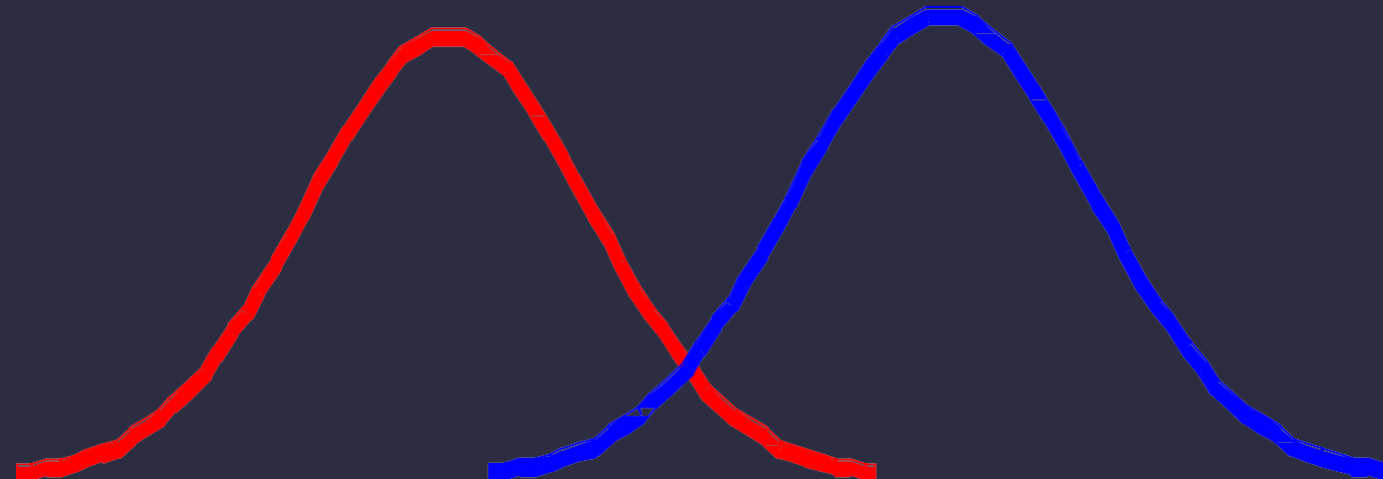
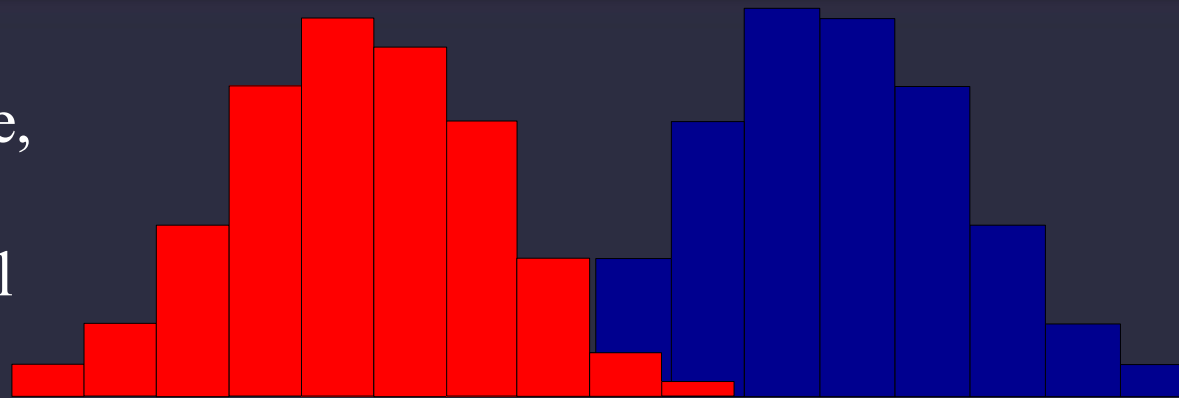
With a lot of data, we can build a histogram. Let us just build one for “Antenna Length” for now...



▨ Katydids

● Grasshoppers

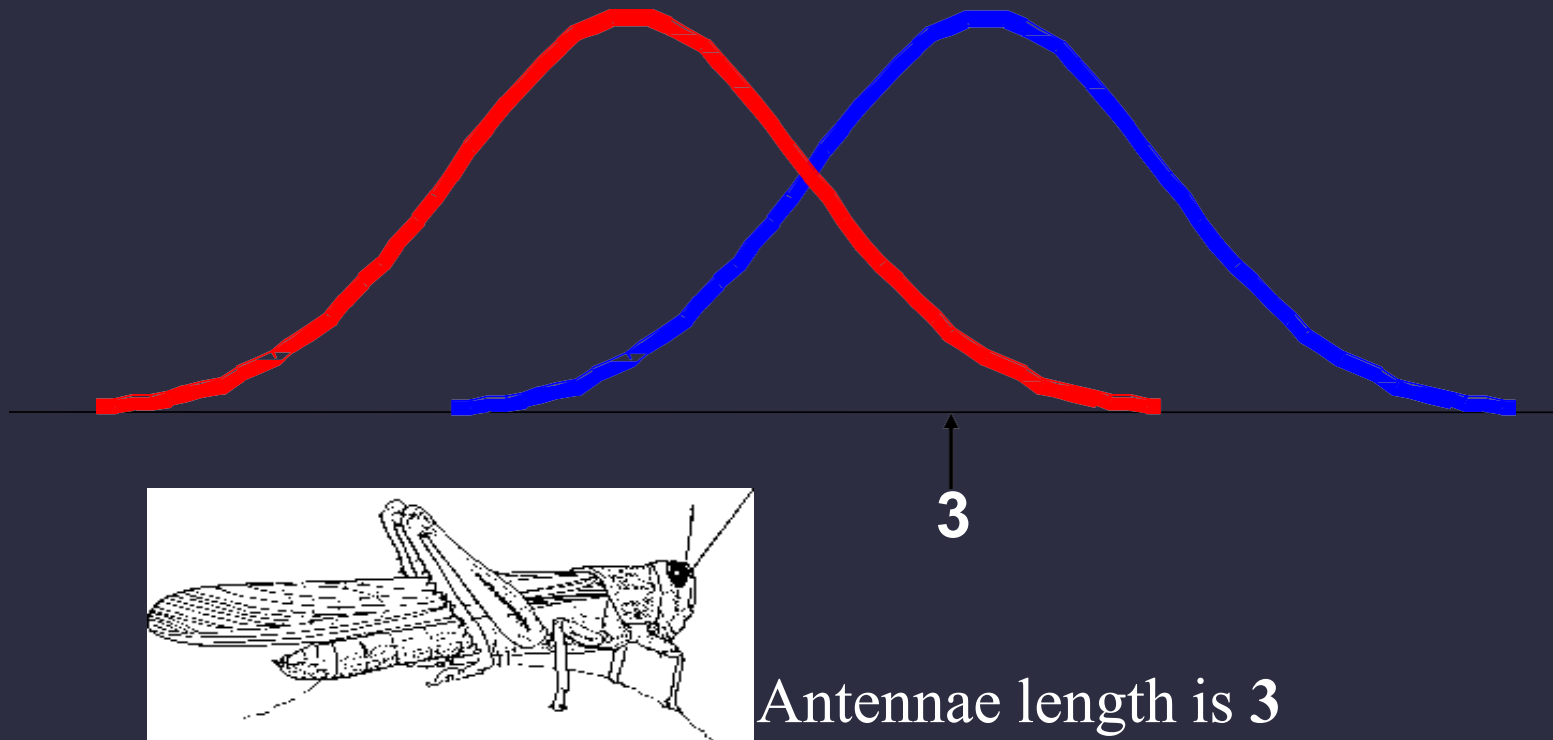
We can leave the histograms as they are, or we can summarize them with two normal distributions.



- We want to classify an insect we have found. Its antennae are 3 units long. How can we classify it?

- We can just ask ourselves, given the distributions of antennae lengths we have seen, is it more *probable* that our insect is a **Grasshopper** or a **Katydid**.
- There is a formal way to discuss the most *probable* classification...

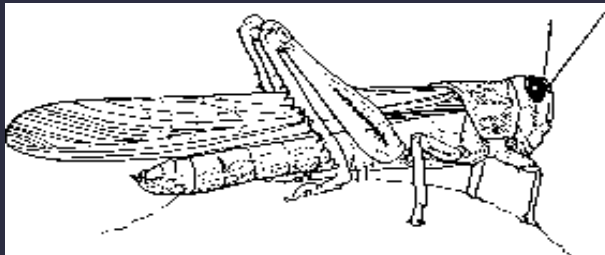
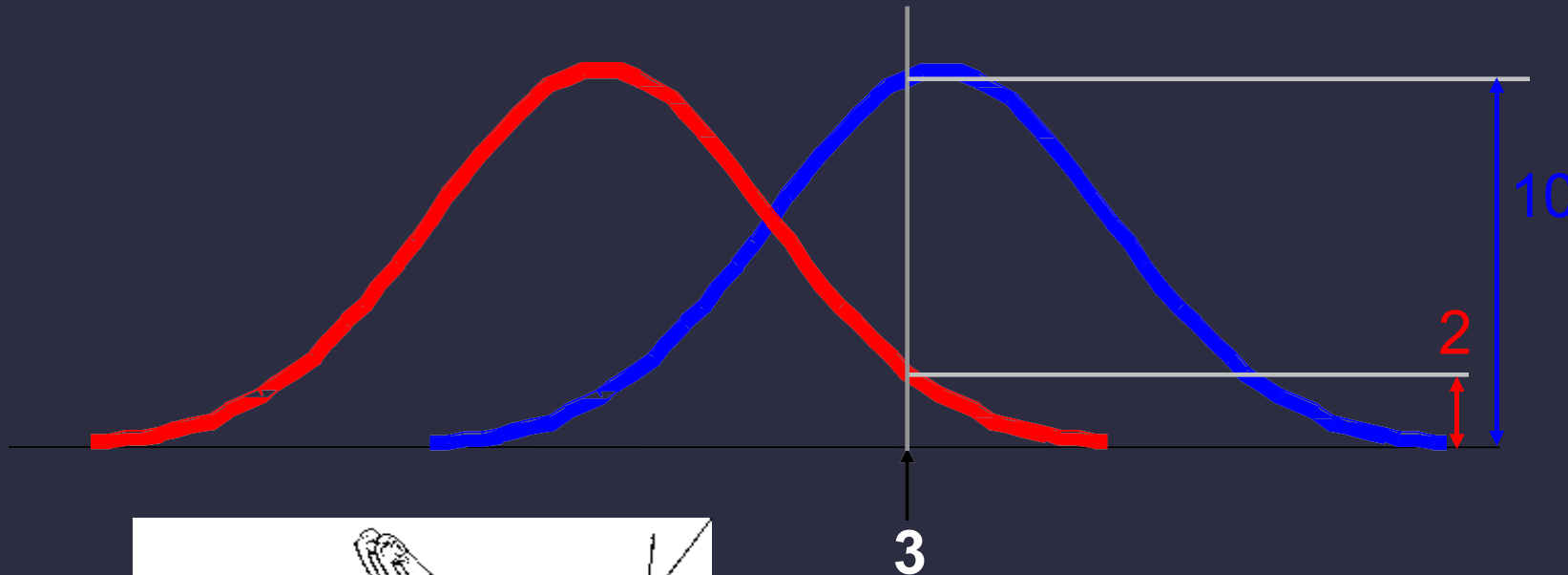
$p(c_j | d)$ = probability of class c_j , given that we have observed d



$p(c_j | d)$ = probability of class c_j , given that we have observed d

$$P(\text{Grasshopper} | 3) = 10 / (10 + 2) = 0.833$$

$$P(\text{Katydid} | 3) = 2 / (10 + 2) = 0.166$$

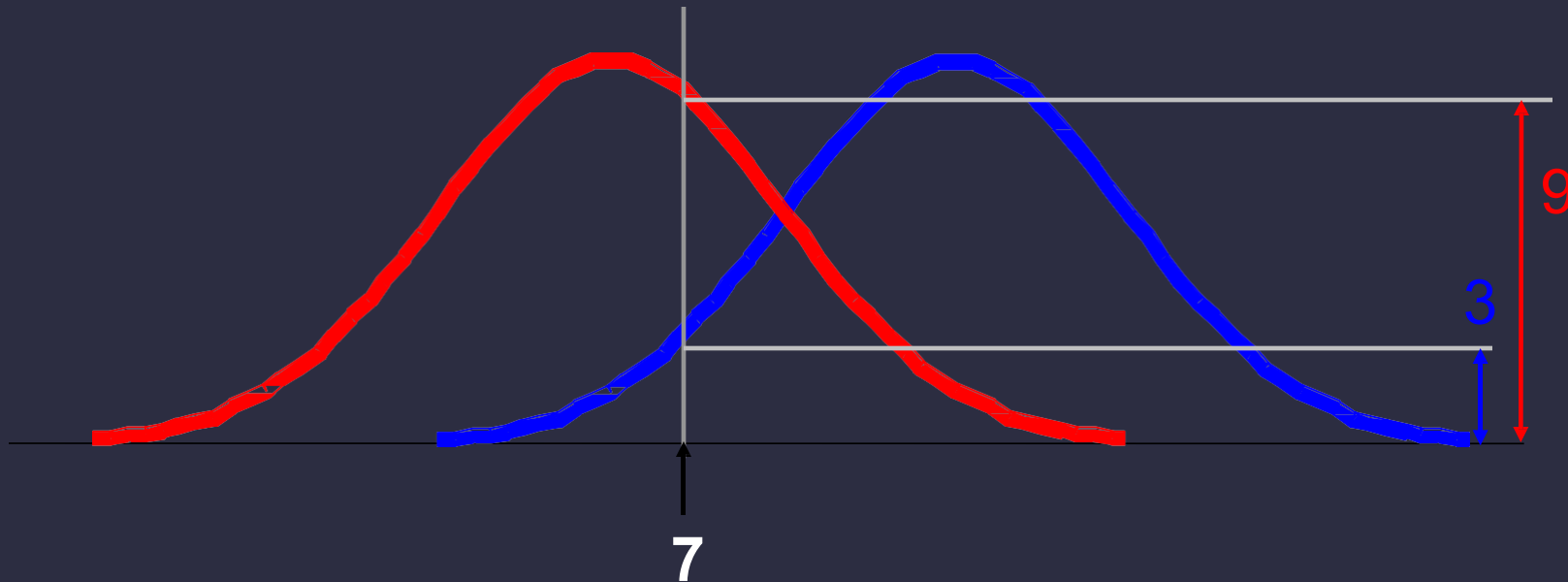


Antennae length is 3

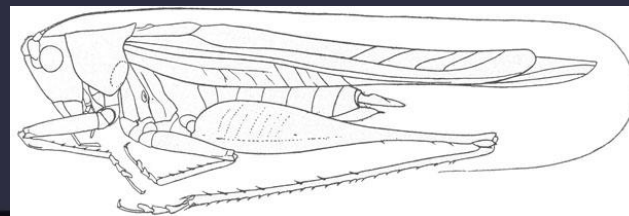
$p(c_j | d)$ = probability of class c_j , given that we have observed d

$$P(\text{Grasshopper} | 7) = 3 / (3 + 9) = 0.250$$

$$P(\text{Katydid} | 7) = 9 / (3 + 9) = 0.750$$



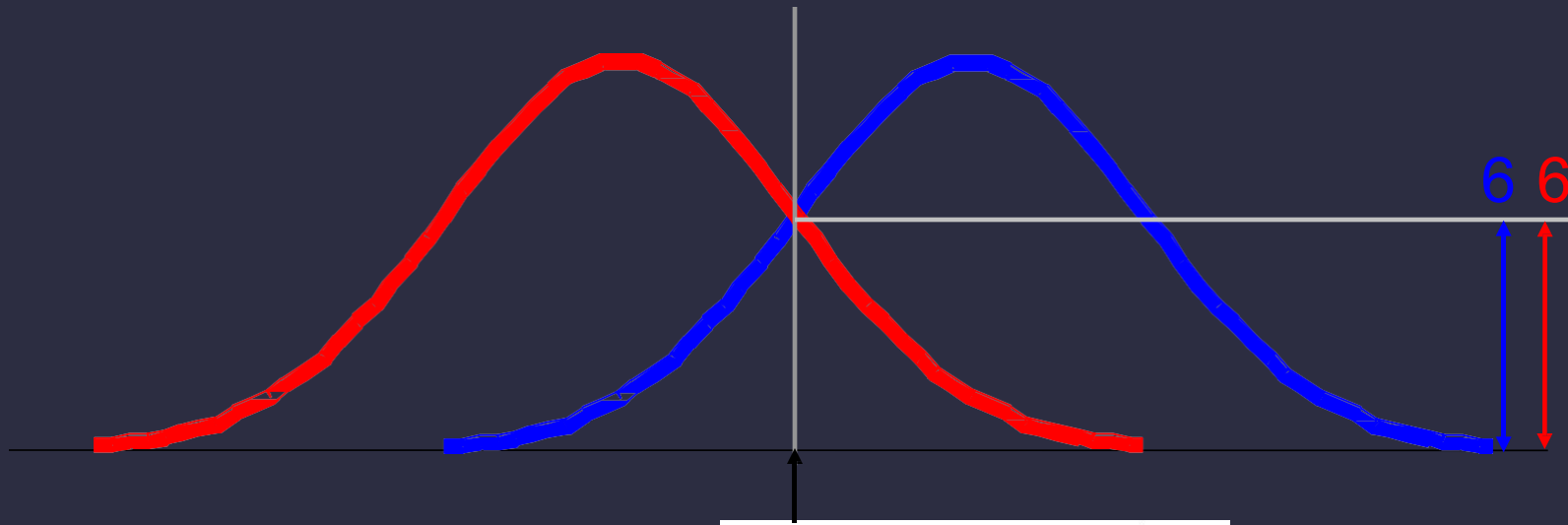
Antennae length is 7



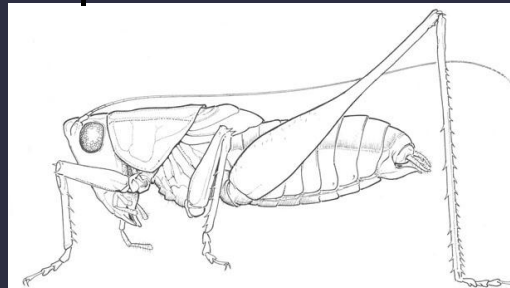
$p(c_j | d)$ = probability of class c_j , given that we have observed d

$$P(\text{Grasshopper} | 5) = 6 / (6 + 6) = 0.500$$

$$P(\text{Katydid} | 5) = 6 / (6 + 6) = 0.500$$



Antennae length is 5



Bayes Classifiers

That was a visual intuition for a simple case of the Bayes classifier, also called:

- Idiot Bayes
- Naïve Bayes
- Simple Bayes

Find out the probability of the previously unseen instance belonging to each class, then simply pick the most probable class.

Bayes Classifiers

Bayesian classifiers use **Bayes theorem**, which says

$$p(c_j | d) = \frac{p(d | c_j) p(c_j)}{p(d)}$$

- $p(c_j | d)$ = probability of instance d being in class c_j , This is what we are trying to compute
- $p(d | c_j)$ = probability of generating instance d given class c_j ,
We can imagine that being in class c_j , causes you to have feature d with some probability
- $p(c_j)$ = probability of occurrence of class c_j ,
This is just how frequent the class c_j , is in our database
- $p(d)$ = probability of instance d occurring

Assume that we have two classes

$c_1 = \text{male}$, and $c_2 = \text{female}$.

We have a person whose sex we do not know, say “*drew*” or *d*.

Classifying *drew* as male or female is equivalent to asking is it more probable that *drew* is *male* or *female*, I.e which is greater $p(\text{male} \mid \text{drew})$ or $p(\text{female} \mid \text{drew})$

(Note: “Drew can be a male or female name”)



Drew Barrymore



Drew Carey



What is the probability of being called “*drew*” given that you are a male?

What is the probability of being a male?

$$p(\text{male} \mid \text{drew}) = \frac{p(\text{drew} \mid \text{male}) p(\text{male})}{p(\text{drew})}$$

What is the probability of being named “*drew*”?
(actually irrelevant, since it is that same for all classes)

Is Officer Drew a Male or Female?



Officer Drew

Luckily, we have a small database with names and sex.

We can use it to apply Bayes rule...

$$p(c_j | d) = \frac{p(d | c_j) p(c_j)}{p(d)}$$

Name	Sex
Drew	Male
Claudia	Female
Drew	Female
Drew	Female
Alberto	Male
Karin	Female
Nina	Female
Sergio	Male



Officer Drew

$$p(c_j | d) = \frac{p(d | c_j) p(c_j)}{p(d)}$$

$$p(\text{male} | \text{drew}) = \frac{p(\text{drew} | \text{male}) p(\text{male})}{p(\text{drew})}$$

$$p(\text{male} | \text{drew}) = \frac{1/3 * 3/8}{3/8} = \frac{0.125}{3/8}$$

$$p(\text{female} | \text{drew}) = \frac{2/5 * 5/8}{3/8} = \frac{0.250}{3/8}$$

Name	Sex
Drew	Male
Claudia	Female
Drew	Female
Drew	Female
Alberto	Male
Karin	Female
Nina	Female
Sergio	Male

Officer Drew is more likely to be a Female.

So far we have only considered Bayes Classification when we have one attribute (the “*antennae length*”, or the “*name*”).

But we may have many features.

How do we use all the features?

$$p(c_j | d) = \frac{p(d | c_j) p(c_j)}{p(d)}$$

Name	Over 170cm	Eye	Hair length	Sex
Drew	No	Blue	Short	Male
Claudia	Yes	Brown	Long	Female
Drew	No	Blue	Long	Female
Drew	No	Blue	Long	Female
Alberto	Yes	Brown	Short	Male
Karin	No	Blue	Long	Female
Nina	Yes	Brown	Short	Female
Sergio	Yes	Blue	Long	Male

- To simplify the task, **naïve Bayesian classifiers** assume attributes have independent distributions, and thereby estimate

$$p(d|c_j) = p(d_1|c_j) * p(d_2|c_j) * \dots * p(d_n|c_j)$$

↑
The probability of class c_j generating instance d , equals....

↑
The probability of class c_j generating the observed value for feature 1, multiplied by..

↑
The probability of class c_j generating the observed value for feature 2, multiplied by..

$$p(\text{male} | \text{drew}) = \frac{p(\text{drew} | \text{male}) p(\text{male})}{p(\text{drew})}$$

- To simplify the task, **naïve Bayesian classifiers** assume attributes have independent distributions, and thereby estimate

$$p(d|c_j) = p(d_1|c_j) * p(d_2|c_j) * \dots * p(d_n|c_j)$$

$$p(\text{officer drew}|c_j) = p(\text{over_170}_{\text{cm}} = \text{yes}|c_j) * p(\text{eye} = \text{blue}|c_j) * \dots$$



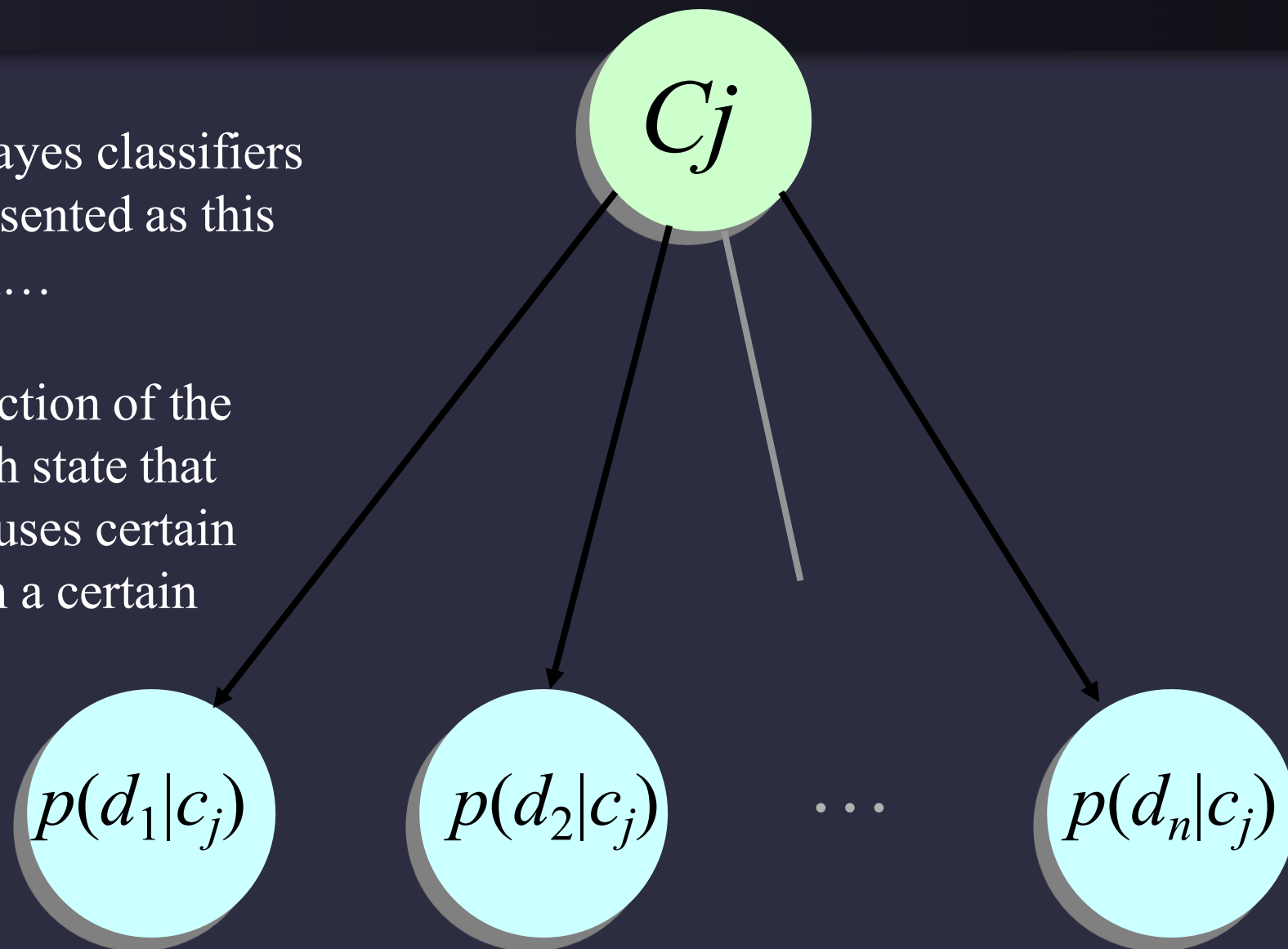
Officer Drew
is blue-eyed,
over 170_{cm}
tall, and has
long hair

$$p(\text{officer drew} | \text{Female}) = 2/5 * 3/5 * \dots$$

$$p(\text{officer drew} | \text{Male}) = 2/3 * 2/3 * \dots$$

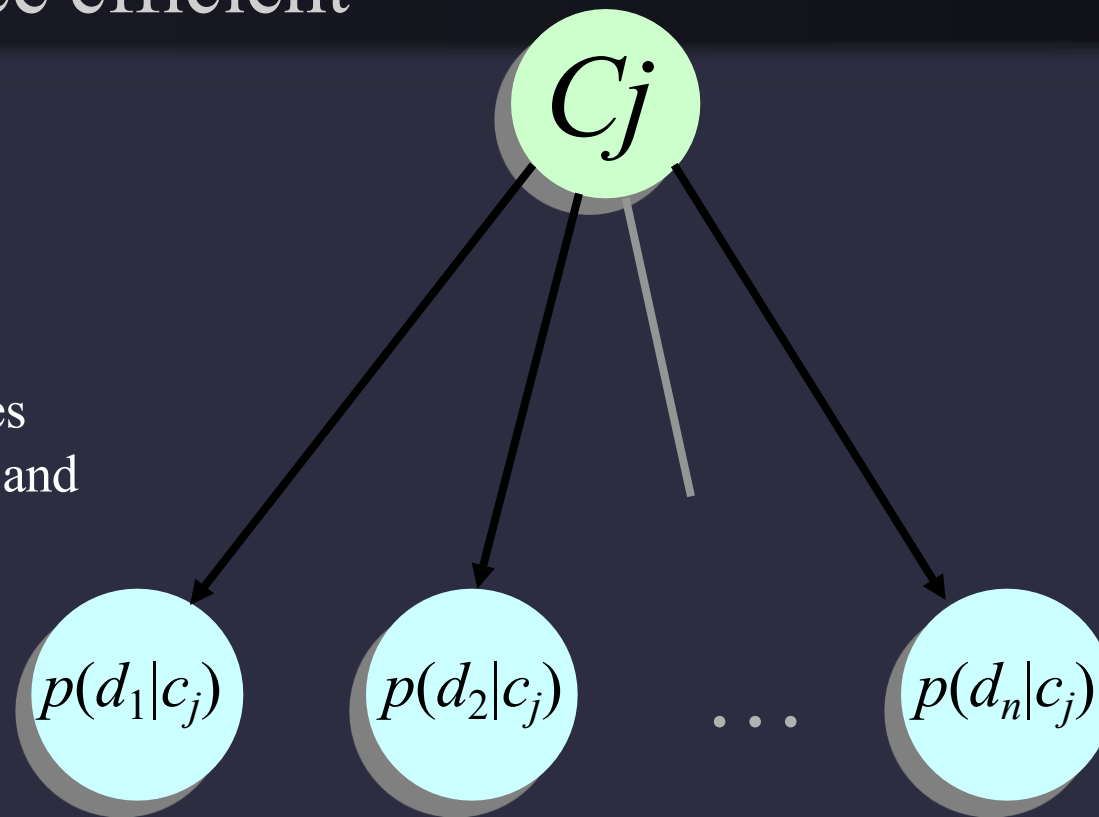
The Naive Bayes classifiers is often represented as this type of graph...

Note the direction of the arrows, which state that each class causes certain features, with a certain probability



Naïve Bayes is fast and space efficient

We can look up all the probabilities with a single scan of the database and store them in a (small) table...



Sex	Over190 _{cm}	
Male	Yes	0.15
	No	0.85
Female	Yes	0.01
	No	0.99

Sex	Long Hair	
Male	Yes	0.05
	No	0.95
Female	Yes	0.70
	No	0.30

Sex	
Male	
Female	

Naïve Bayes is NOT sensitive to irrelevant features...

Suppose we are trying to classify a persons sex based on several features, including eye color. (Of course, eye color is completely irrelevant to a persons gender)

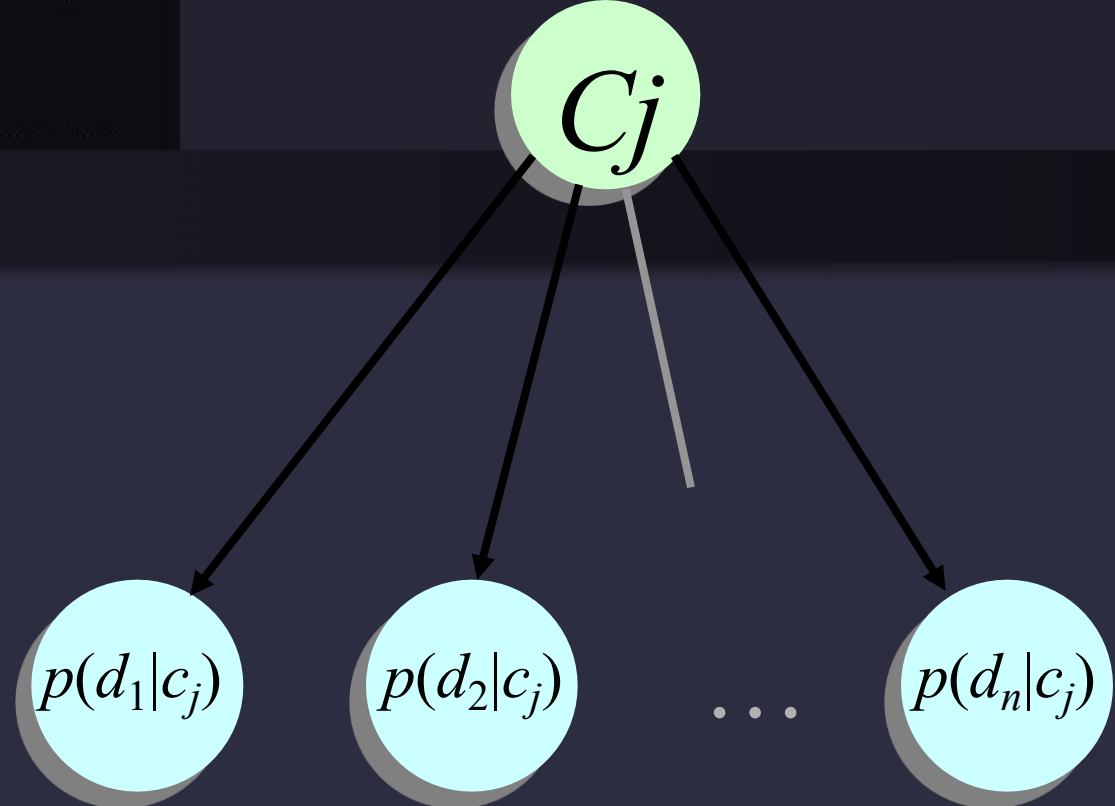
$$p(\text{Jessica} | c_j) = p(\text{eye} = \text{brown} | c_j) * p(\text{wears_dress} = \text{yes} | c_j) * \dots$$

$$p(\text{Jessica} | \text{Female}) = 9,000/10,000 * 9,975/10,000 * \dots$$

$$p(\text{Jessica} | \text{Male}) = 9,001/10,000 * 2/10,000 * \dots$$

Almost the same!

We can have an arbitrary number of classes, or feature values

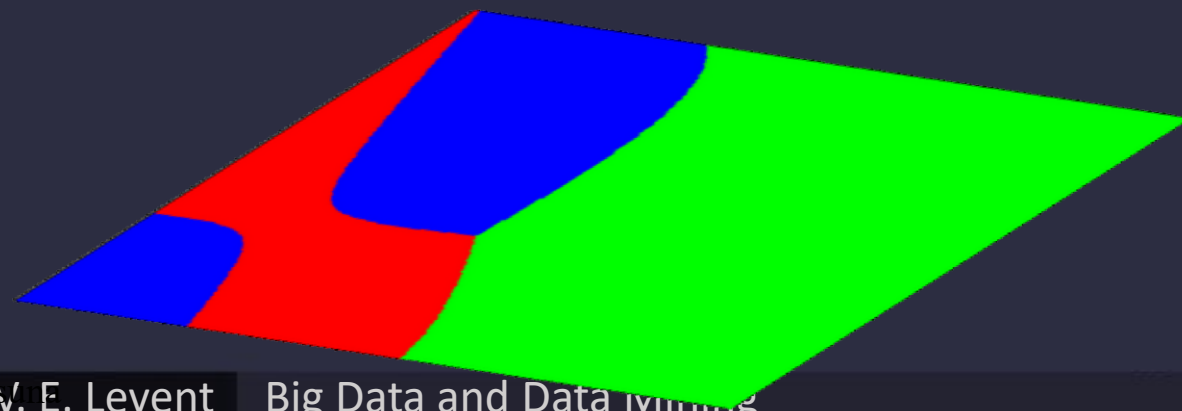
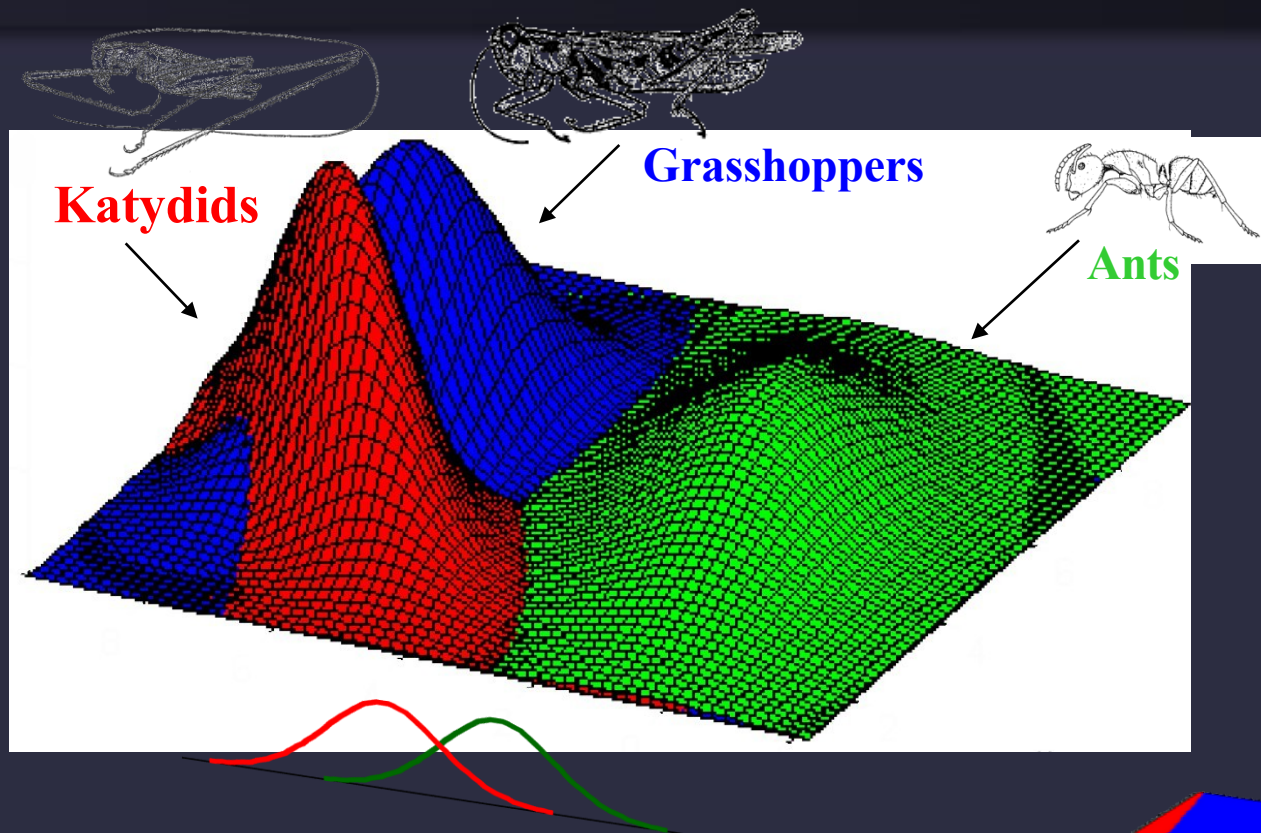


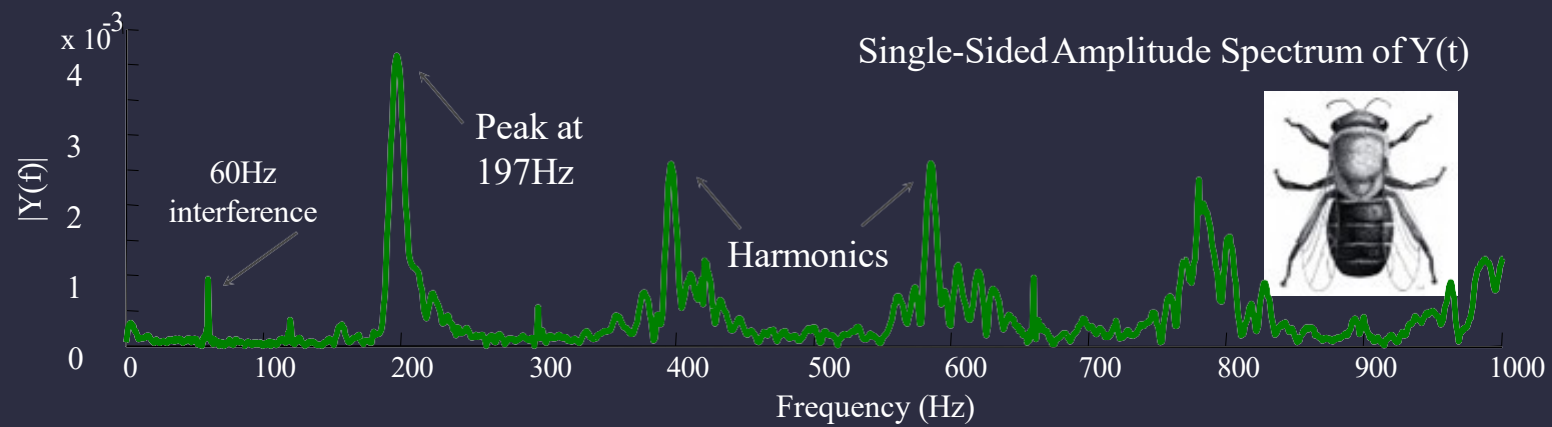
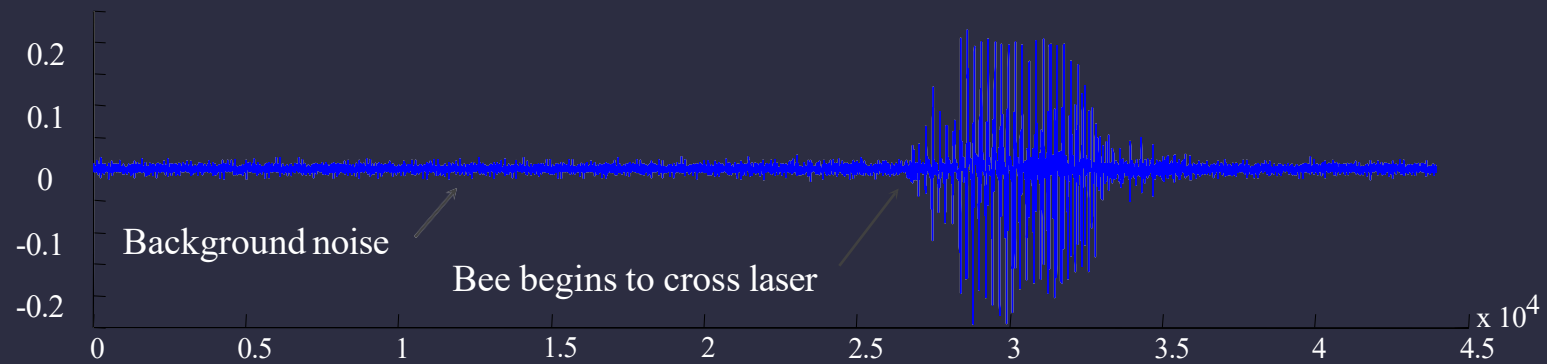
Animal	Mass >10 _{kg}	
Cat	Yes	0.15
	No	0.85
Dog	Yes	0.91
	No	0.09
Pig	Yes	0.99
	No	0.01

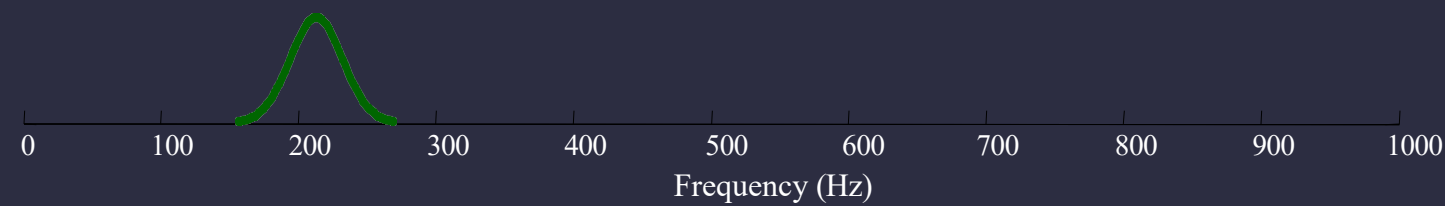
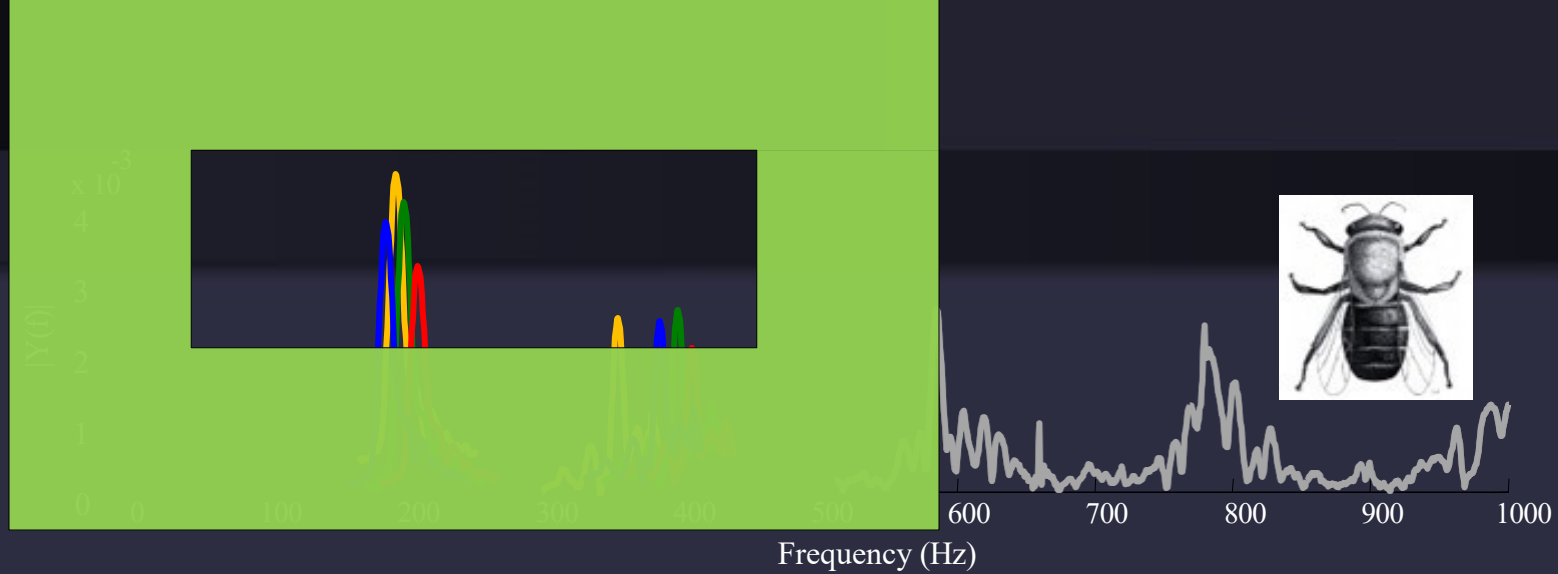
Animal	Color	
Cat	Black	0.33
	White	0.23
	Brown	0.44
Dog	Black	0.97
	White	0.03
	Brown	0.90
Pig	Black	0.04
	White	0.01

Animal
Cat
Dog
Pig

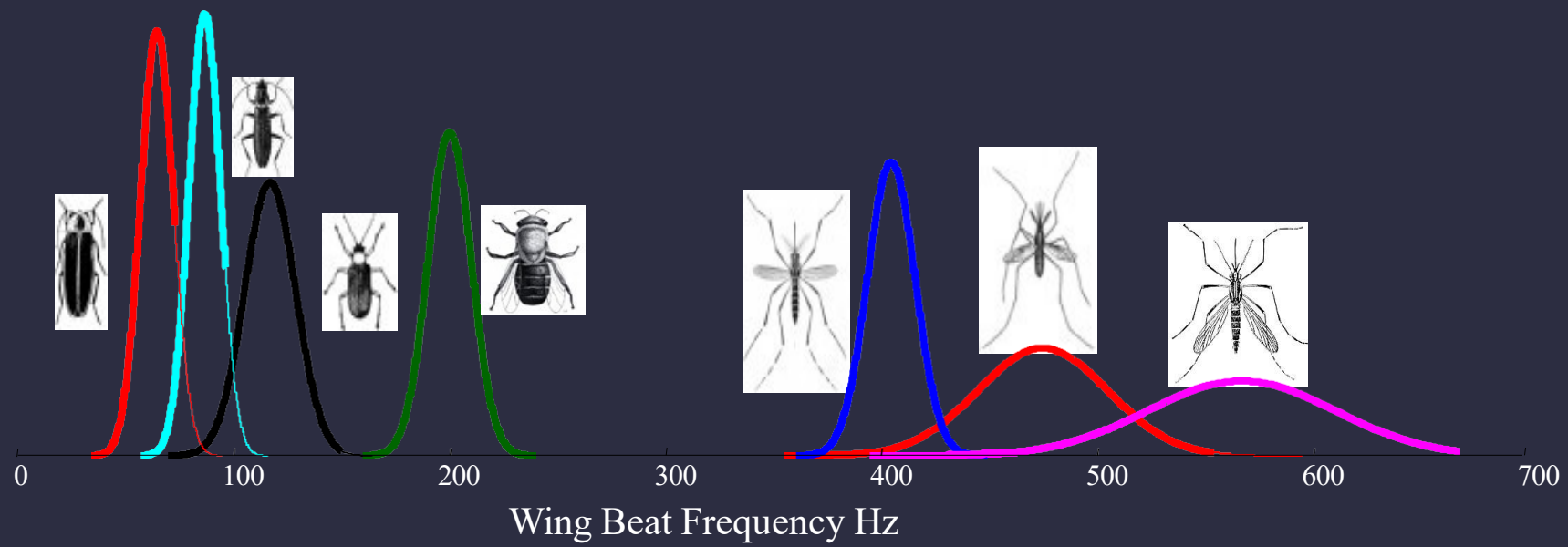
The Naïve Bayesian Classifier has a piecewise quadratic decision boundary

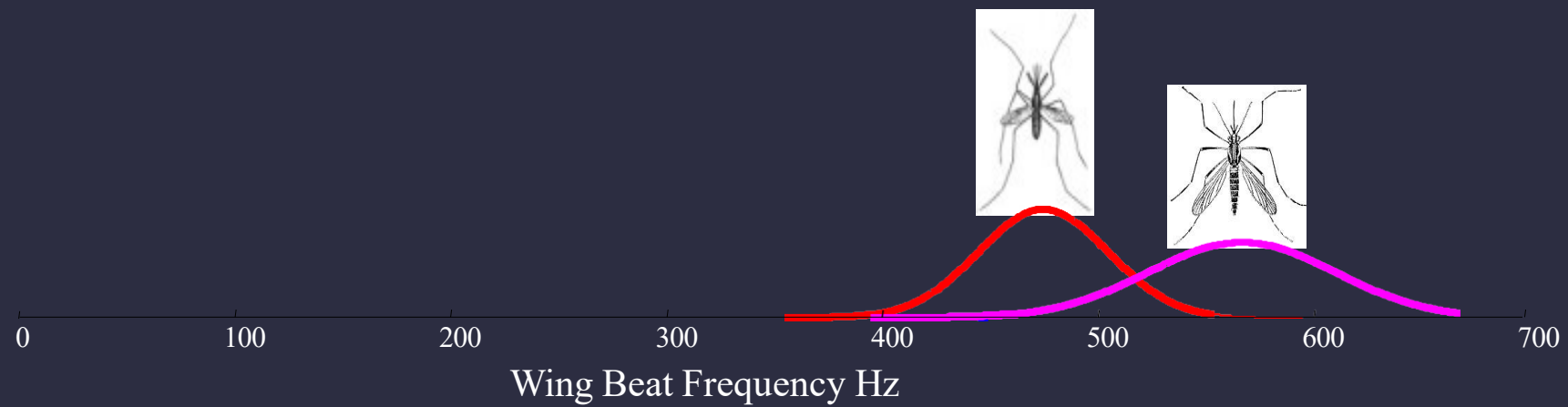


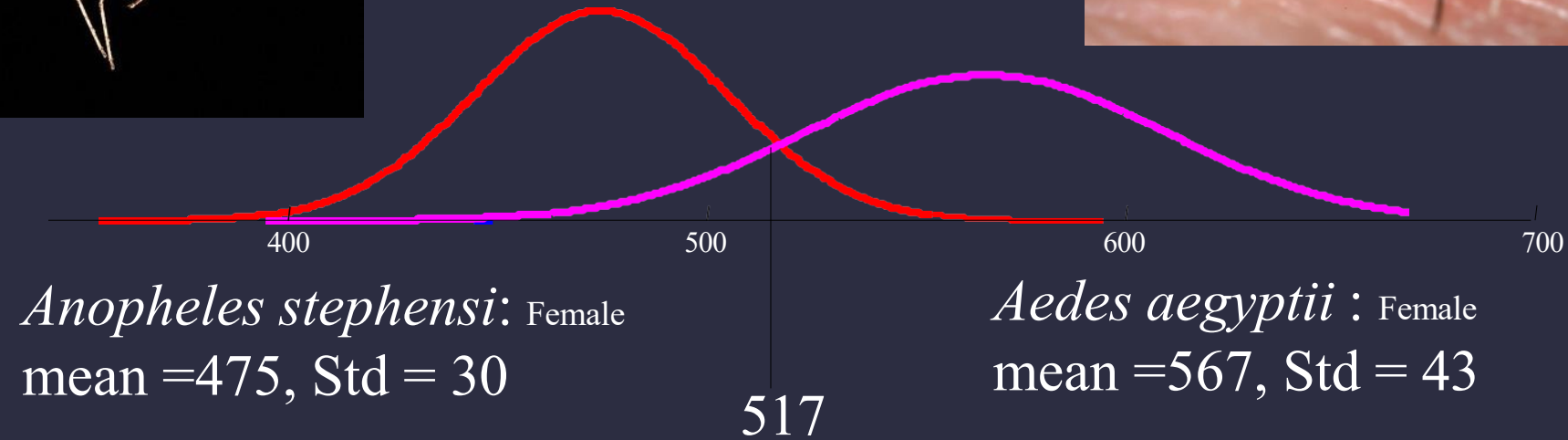




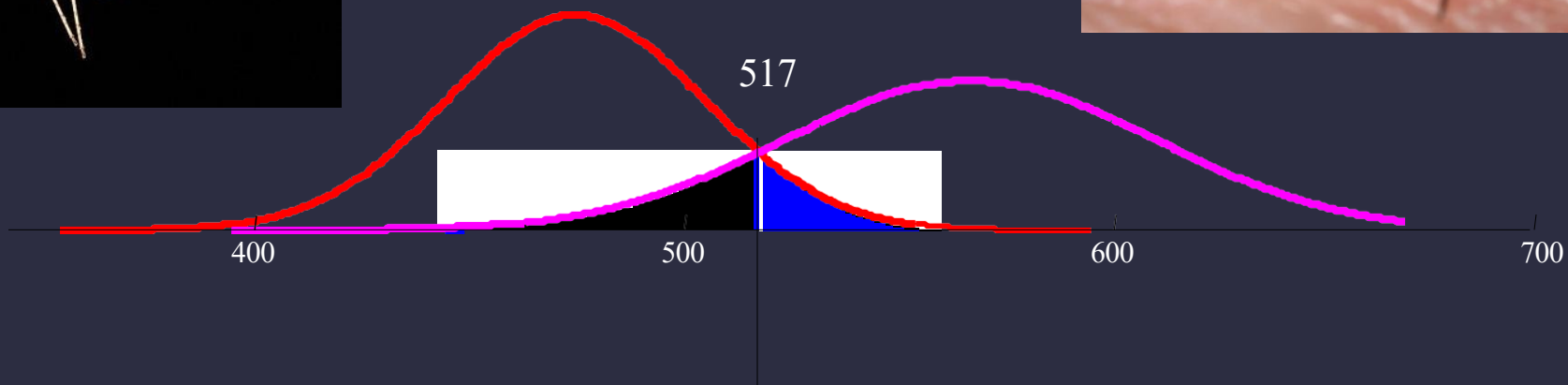
$$\frac{1}{\sqrt{2\pi}\sigma} e^{-\frac{(x-\mu)^2}{2\sigma^2}}$$







If I see an insect with a wingbeat frequency of 500, what is it?

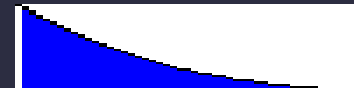


What is the error rate?

12.2% of the
area under the
pink curve

8.02% of the
area under the
red curve

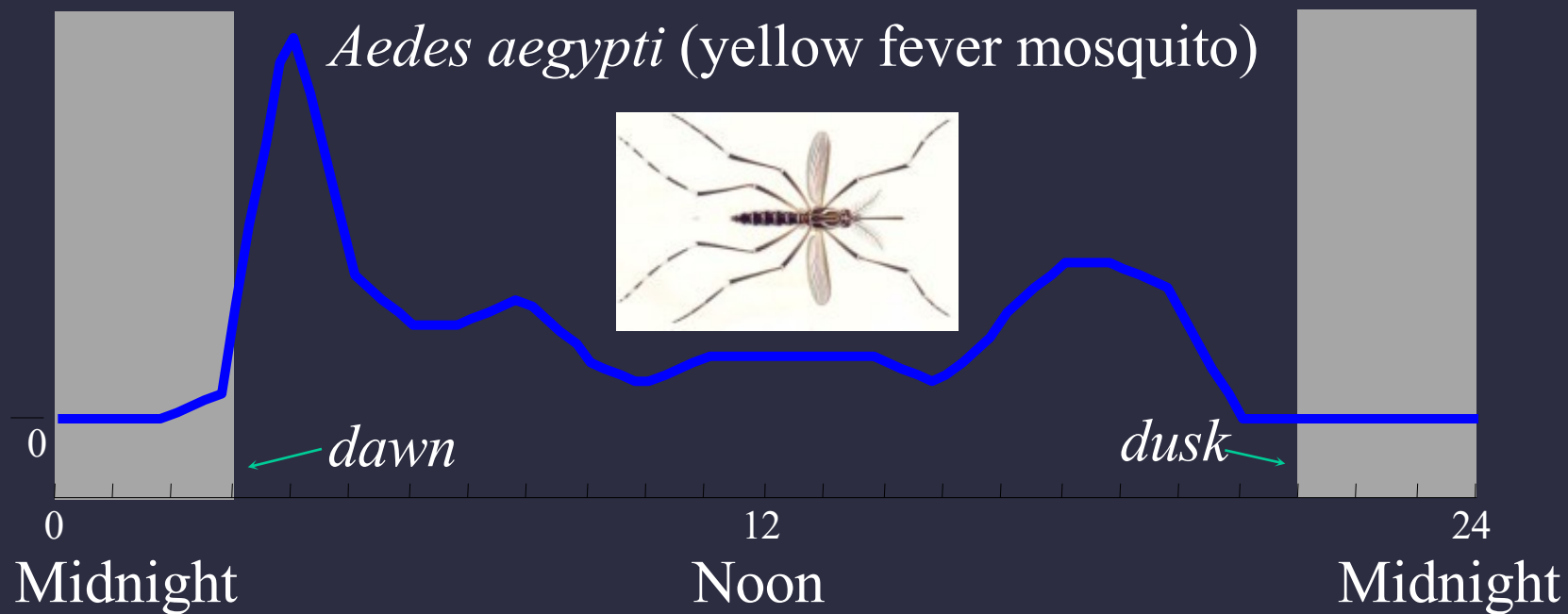
Can we get more features?



$$\frac{1}{\sqrt{2\pi}\sigma} \exp\left(-\frac{(x-\mu)^2}{2\sigma^2}\right)$$

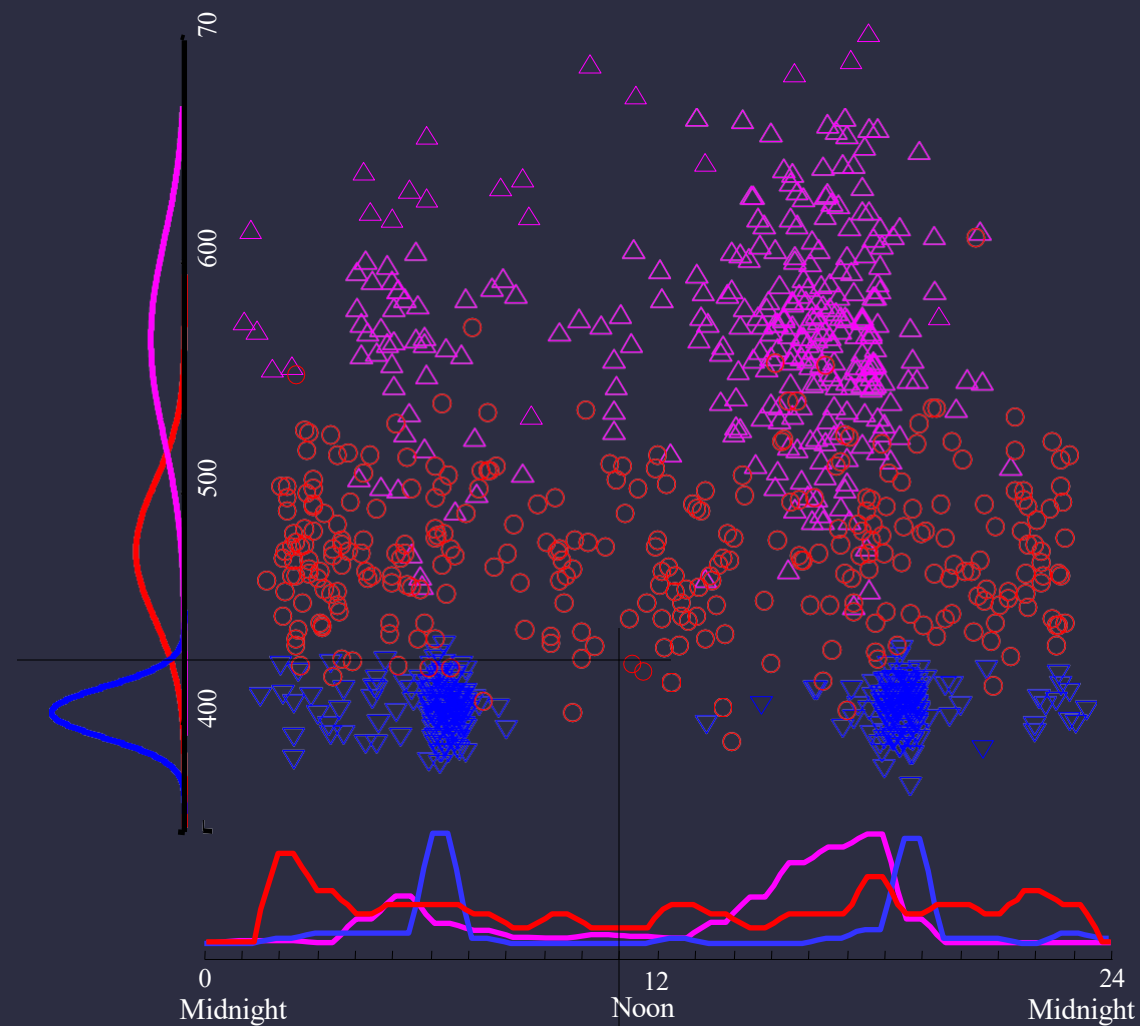
$$P(\text{Anopheles} | \text{wingbeat} = 500) = \frac{1}{\sqrt{2\pi} 30} e^{-\frac{(500-475)^2}{2 \times 30^2}}$$

Circadian Features



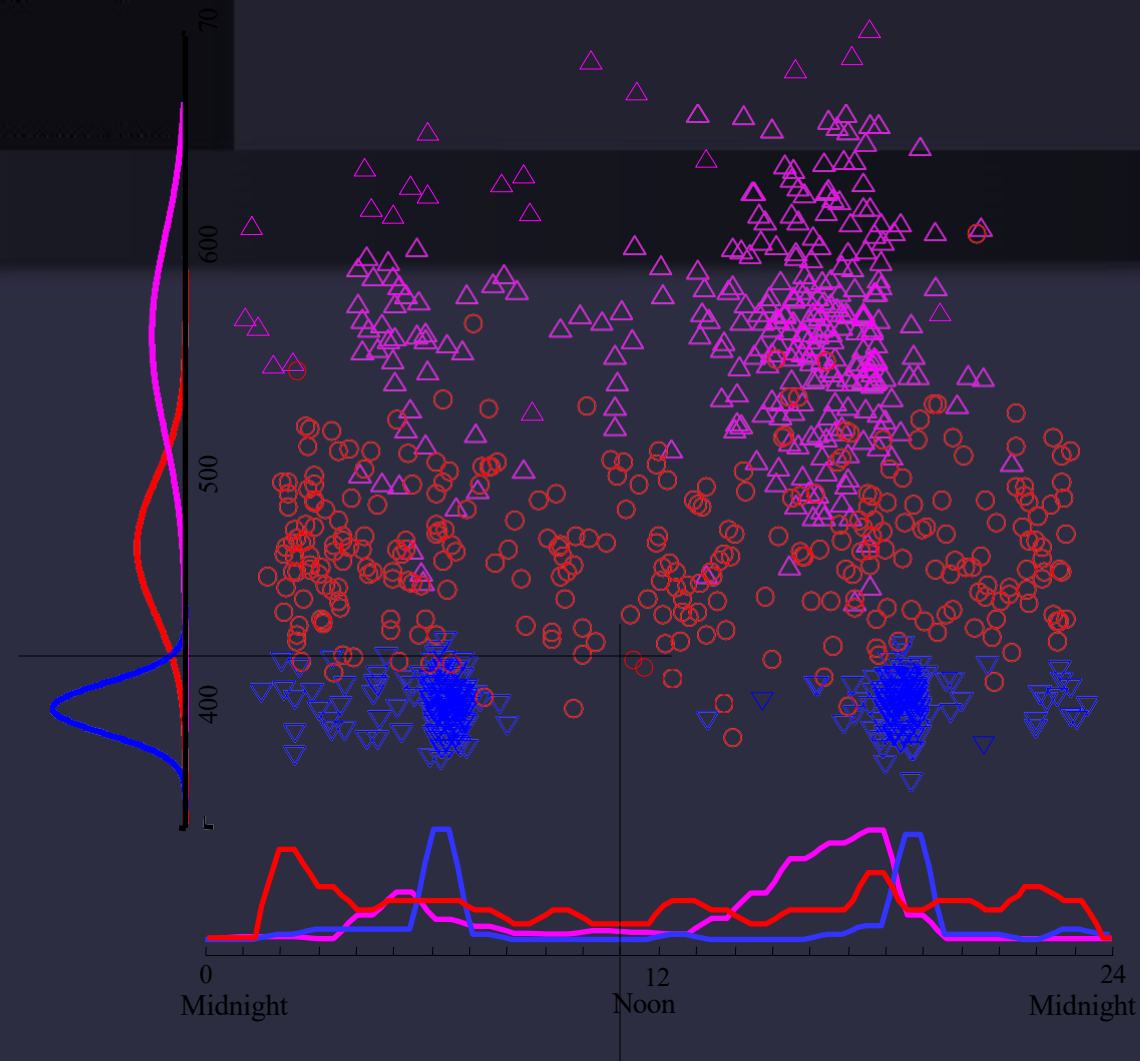
Suppose I observe an insect with a wingbeat frequency of 420Hz at 11:00am

What is it?



Suppose I observe an insect with a wingbeat frequency of 420 at 11:00am

What is it?



$$(Culex \mid [420\text{Hz}, 11:00\text{am}]) = (6 / (6 + 6 + 0)) * (2 / (2 + 4 + 3)) = 0.111$$

$$(Anopheles \mid [420\text{Hz}, 11:00\text{am}]) = (6 / (6 + 6 + 0)) * (4 / (2 + 4 + 3)) = 0.222$$

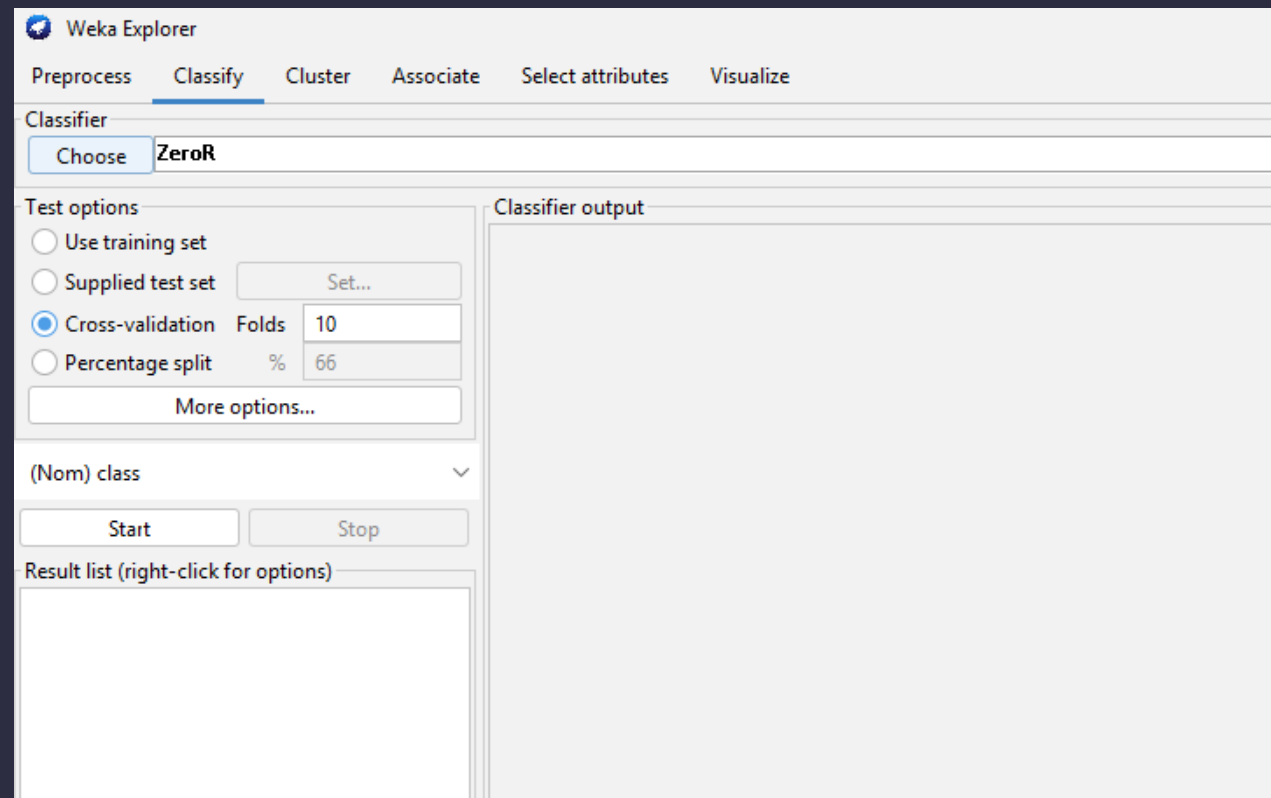
$$(Aedes \mid [420\text{Hz}, 11:00\text{am}]) = (0 / (6 + 6 + 0)) * (3 / (2 + 4 + 3)) = 0.000$$

Advantages/Disadvantages of Naïve Bayes

- Advantages:
 - Fast to train (single scan). Fast to classify
 - Not sensitive to irrelevant features
 - Handles real and discrete data
 - Handles streaming data well
- Disadvantages:
 - Assumes independence of features

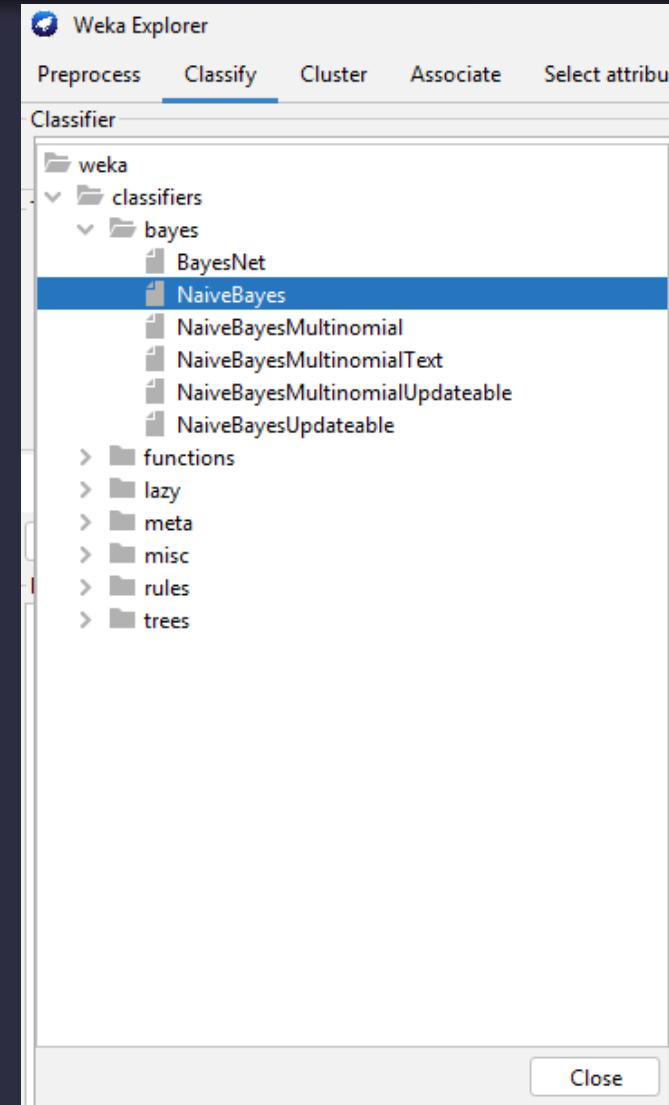
Naïve Bayes

Load Iris Dataset and goto Classify Tab



Naïve Bayes

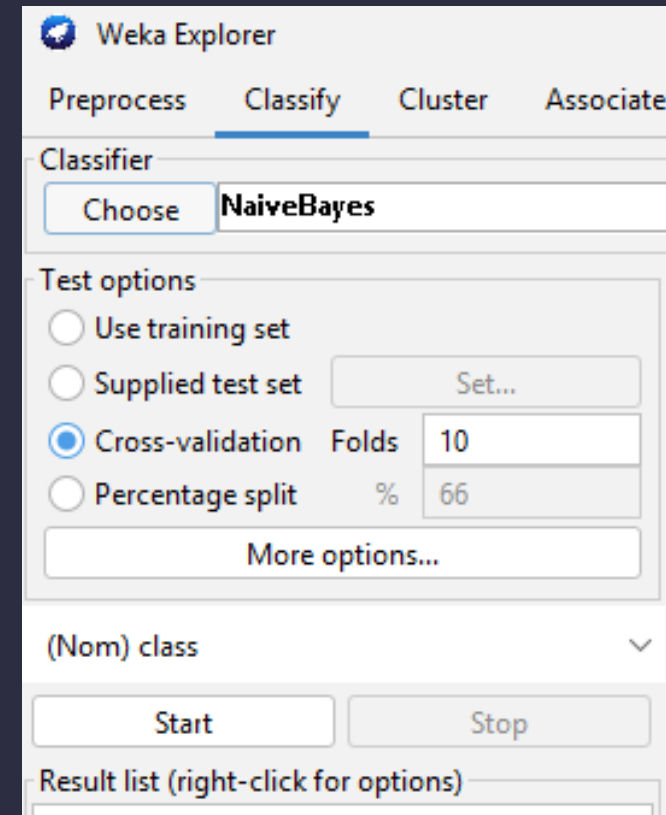
Select Naive Bayes Classifier



Naïve Bayes

Cross-Validation

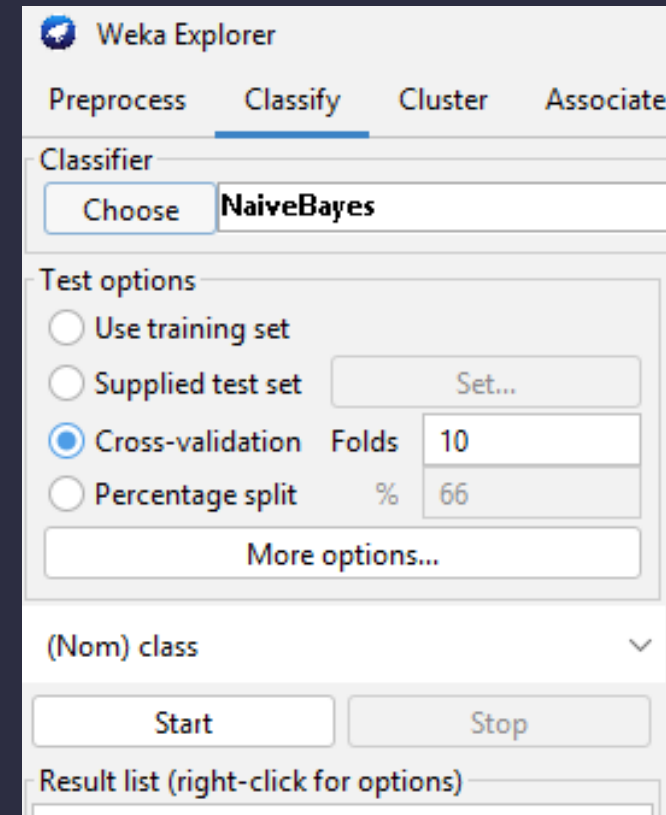
- 10 percent will used for only validation



Naïve Bayes

Cross-Validation

- 10 percent will used for only validation



Naïve Bayes

Start

Weka Explorer

Preprocess **Classify** Cluster Associate Select attributes Visualize

Classifier: Choose **NaiveBayes**

Test options:

- ☐ Use training set
- ☐ Supplied test set
- ☒ Cross-validation Folds
- ☐ Percentage split %

(Nom) class

Result list (right-click for options)

17:24:16 - bayes.NaiveBayes

Classifier output

Attribute	mean	std. dev.	weight sum	precision
sepalwidth	3.4015	0.3925	50	0.1091
petallength	1.4694	0.1782	50	0.1405
petalwidth	0.2743	0.1096	50	0.1143

Time taken to build model: 0 seconds

=== Stratified cross-validation ===

=== Summary ===

Correctly Classified Instances	144	96	%
Kappa statistic	0.94		
Mean absolute error	0.0342		
Root mean squared error	0.155		
Relative absolute error	7.6997 %		
Root relative squared error	32.8794 %		
Total Number of Instances	150		

=== Detailed Accuracy By Class ===

	TP Rate	FP Rate	Precision	Recall	F-Measure	MCC	ROC Area	PRC Area	Class
	1,000	0,000	1,000	1,000	1,000	1,000	1,000	1,000	Iris-setosa
	0,960	0,040	0,923	0,960	0,941	0,911	0,992	0,983	Iris-versicolor
	0,920	0,020	0,958	0,920	0,939	0,910	0,992	0,986	Iris-virginica
Weighted Avg.	0,960	0,020	0,960	0,960	0,960	0,940	0,994	0,989	

=== Confusion Matrix ===

a	b	c	<-- classified as
50	0	0	a = Iris-setosa
0	48	2	b = Iris-versicolor
0	4	46	c = Iris-virginica

Naïve Bayes

Start

Percentage Split

Weka Explorer

Preprocess Classify Cluster Associate Select attributes Visualize

Classifier: Choose NaiveBayes

Test options

☐ Use training set

☐ Supplied test set Set...

☐ Cross-validation Folds 10

☒ Percentage split % 80

More options...

(Nom) class

Start Stop

Result list (right-click for options)

17:24:16 - bayes.NaiveBayes

17:25:42 - bayes.NaiveBayes

17:25:52 - bayes.NaiveBayes

Classifier output

	std. dev.	weight sum	precision
petallength	0.3925	0.3038	0.3088
mean	50	50	50
std. dev.	0.1091	0.1091	0.1091
weight sum	0.14694	4.2452	5.5516
precision	0.1782	0.4712	0.5529
mean	50	50	50
std. dev.	0.1405	0.1405	0.1405
weight sum	0.2743	1.3097	2.0343
precision	0.1096	0.1915	0.2646
mean	50	50	50
std. dev.	0.1143	0.1143	0.1143
weight sum			
precision			

Time taken to build model: 0 seconds

=== Evaluation on test split ===

Time taken to test model on test split: 0 seconds

=== Summary ===

	Correctly Classified Instances	29	96.6667 %
Kappa statistic	0.9497		
Mean absolute error	0.0304		
Root mean squared error	0.1226		
Relative absolute error	6.8425 %		
Root relative squared error	25.9804 %		
Total Number of Instances	30		

=== Detailed Accuracy By Class ===

	TP Rate	FP Rate	Precision	Recall	F-Measure	MCC	ROC Area	PRC Area	Class
1,000	0,000	1,000	1,000	1,000	1,000	1,000	1,000	1,000	Iris-setosa
1,000	0,050	0,909	1,000	0,952	0,929	0,995	0,991		Iris-versicolor
0,889	0,000	1,000	0,889	0,941	0,921	0,995	0,989		Iris-virginica
Weighted Avg.	0,967	0,017	0,970	0,967	0,966	0,953	0,997	0,994	

=== Confusion Matrix ===

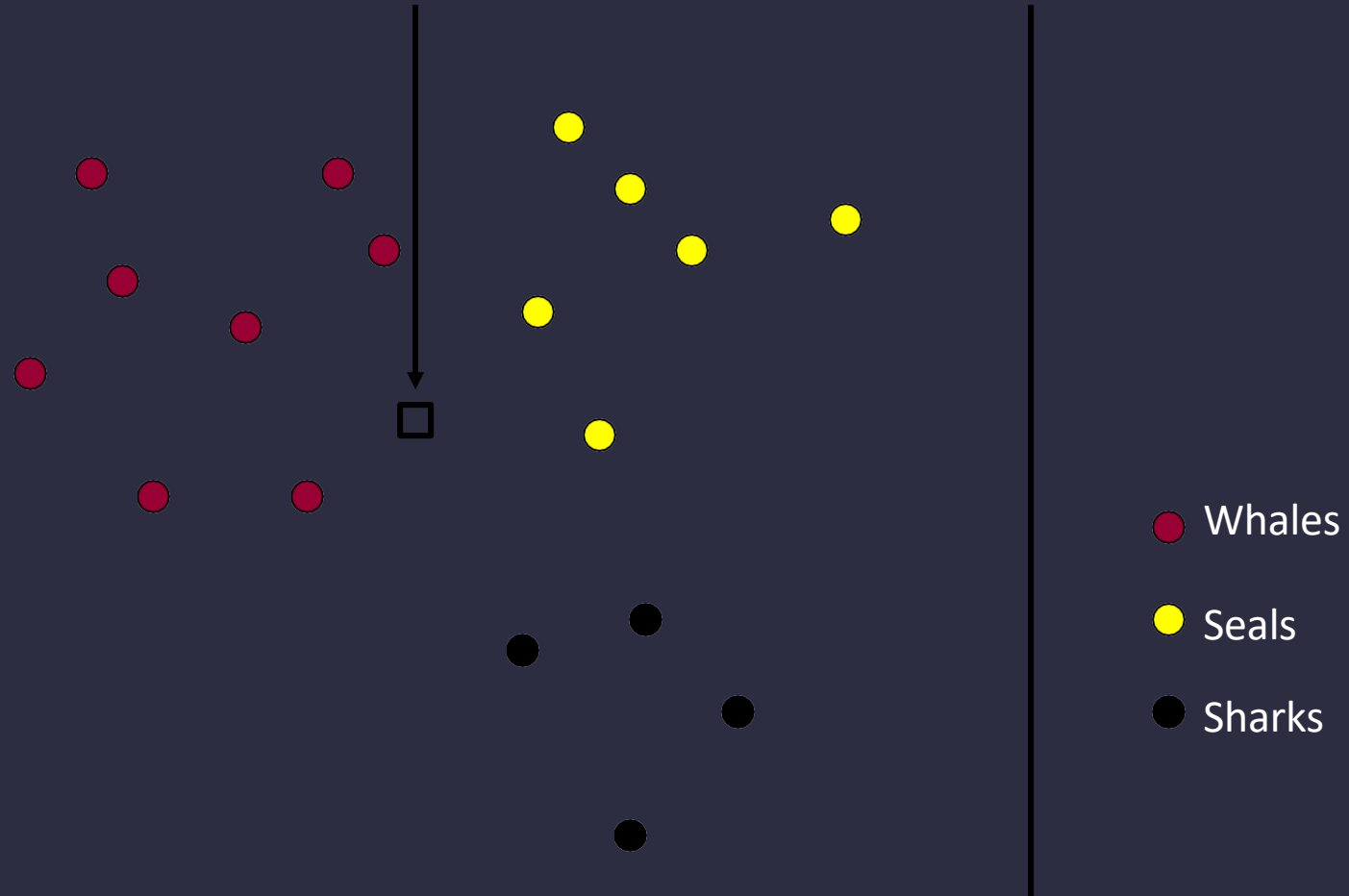
```

a b c <-- classified as
11 0 0 | a = Iris-setosa
0 10 0 | b = Iris-versicolor
0 1 8 | c = Iris-virginica

```

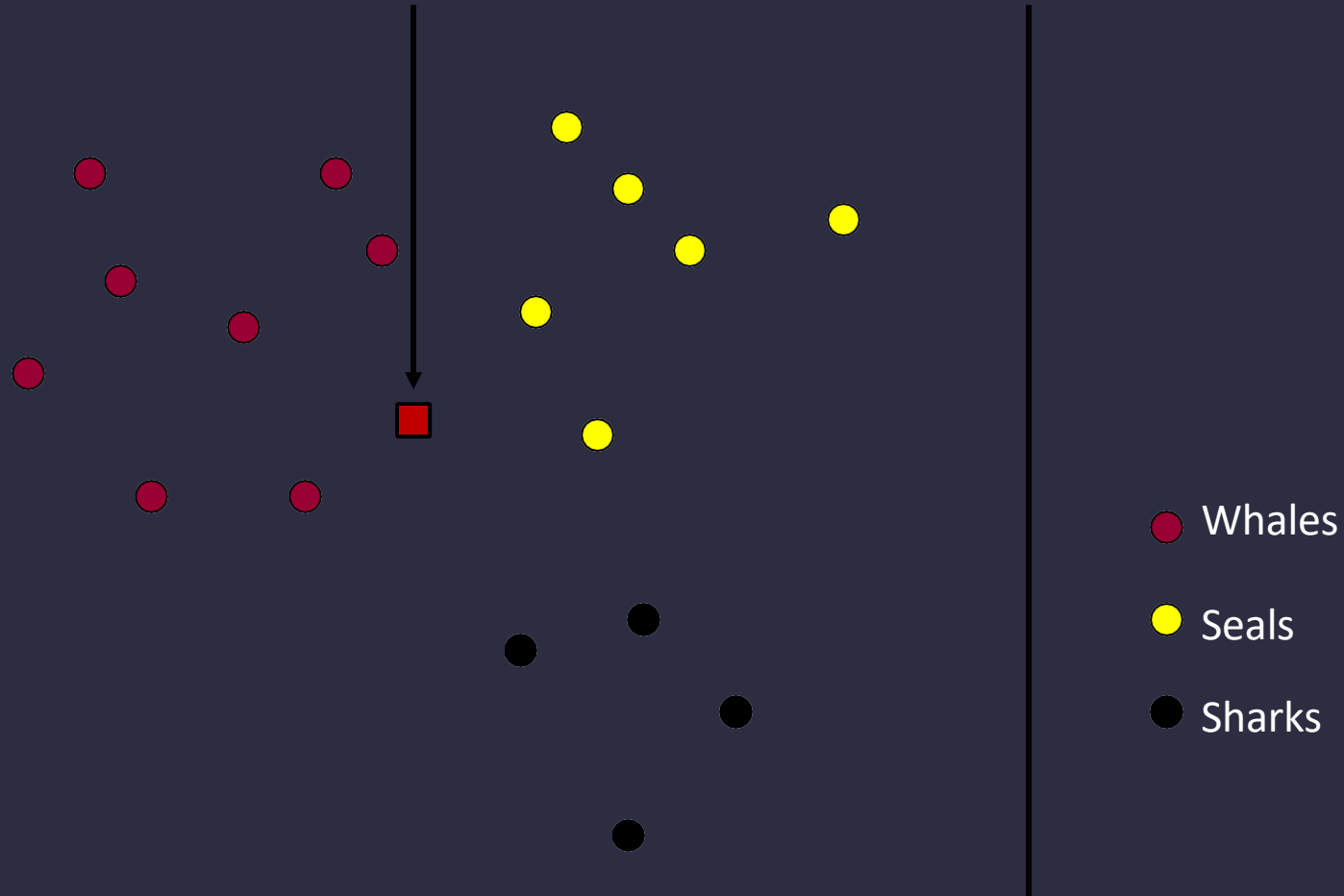
K-Nearest Neighbor

Test subject



Nearest Neighbor Classifier

Test subject



Nearest Neighbor Classification

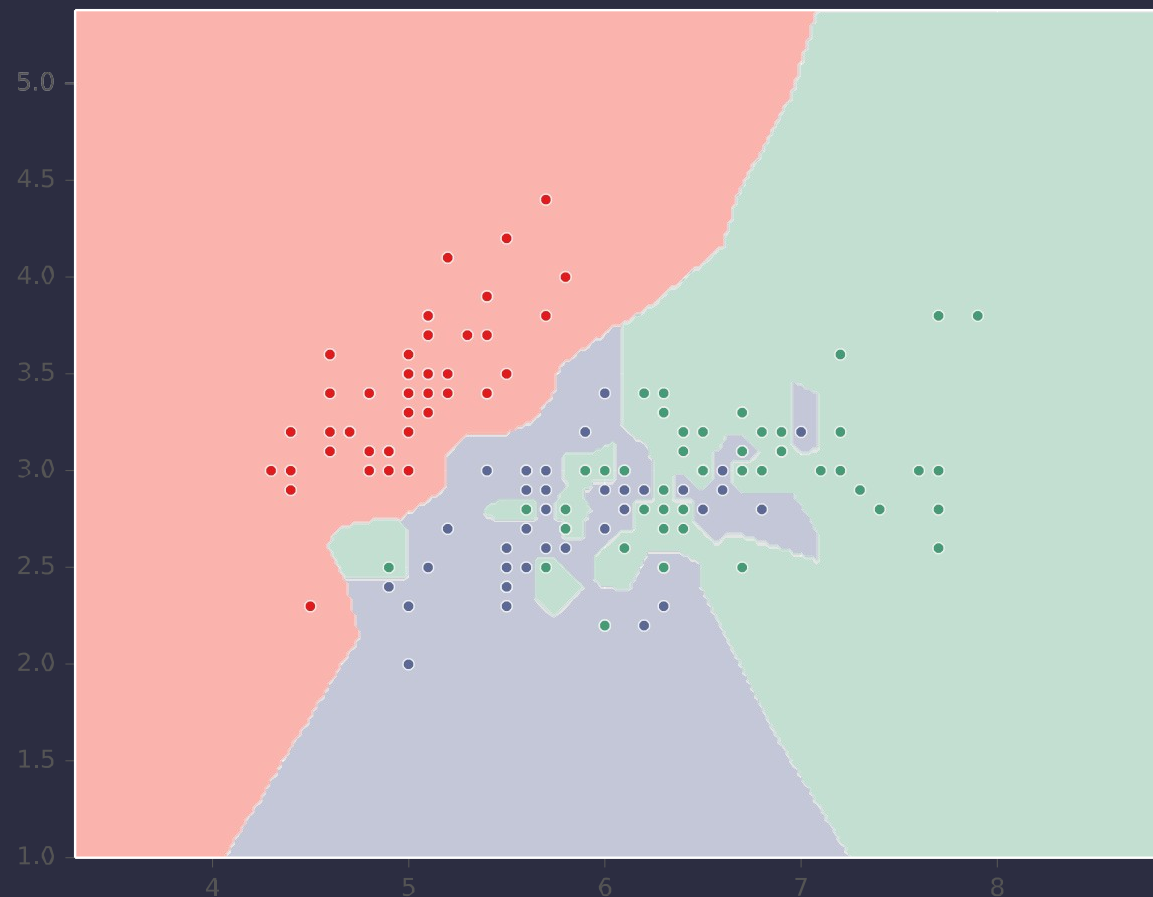
Given a training dataset $\mathcal{D} = \{y^{(n)}, \mathbf{x}^{(n)}\}_{n=1}^N$, $y \in \{1, \dots, C\}$, $\mathbf{x} \in \mathbb{R}^M$

and a test input \mathbf{x}_{test} , predict the class label

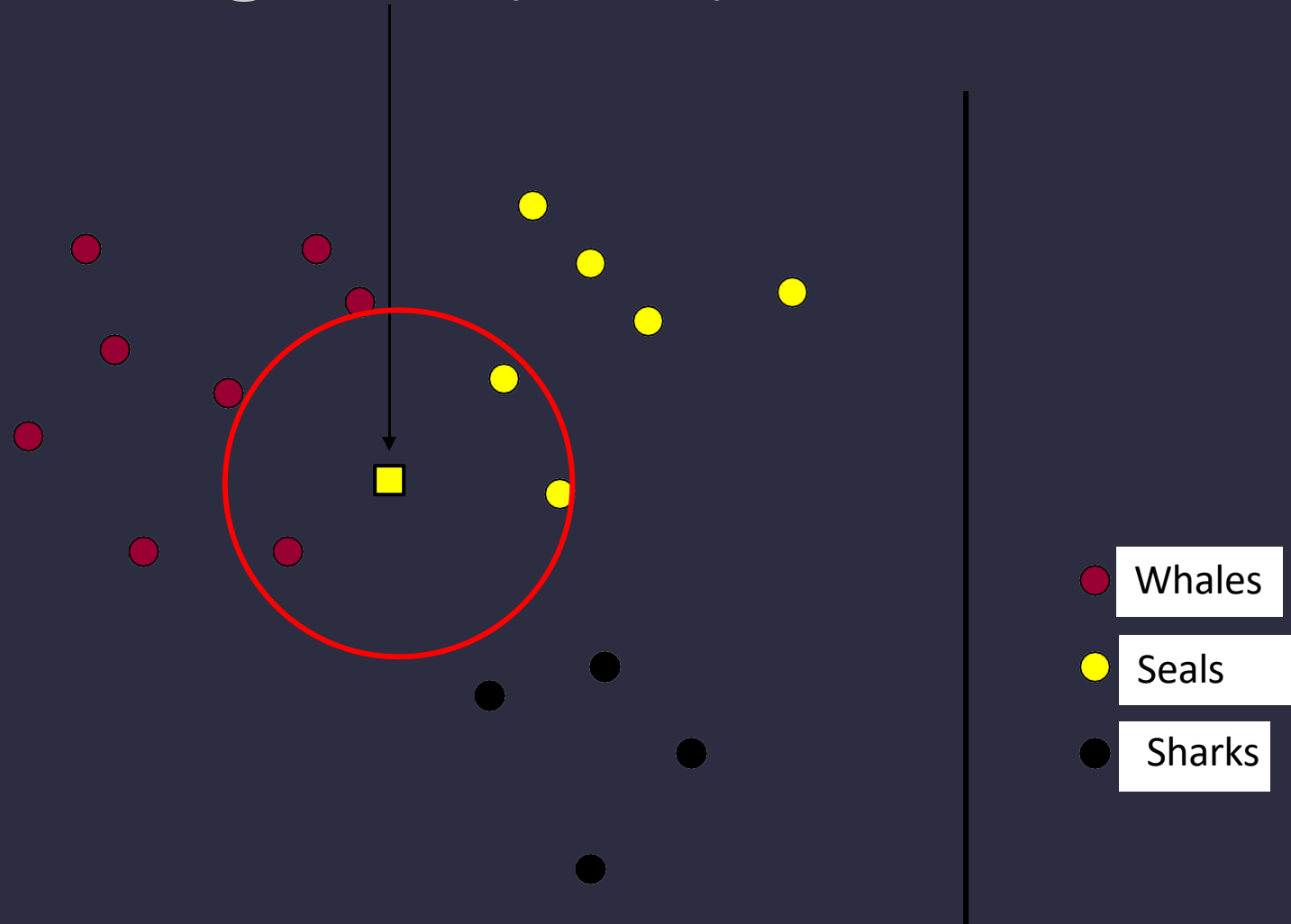
- 1) Find the closest point in the training data to \mathbf{x}_{test}
- 2) Return the class label of that closest point

Need distance function! What should $d(\mathbf{x}, \mathbf{z})$ be?

Nearest Neighbor on Fisher Iris Data

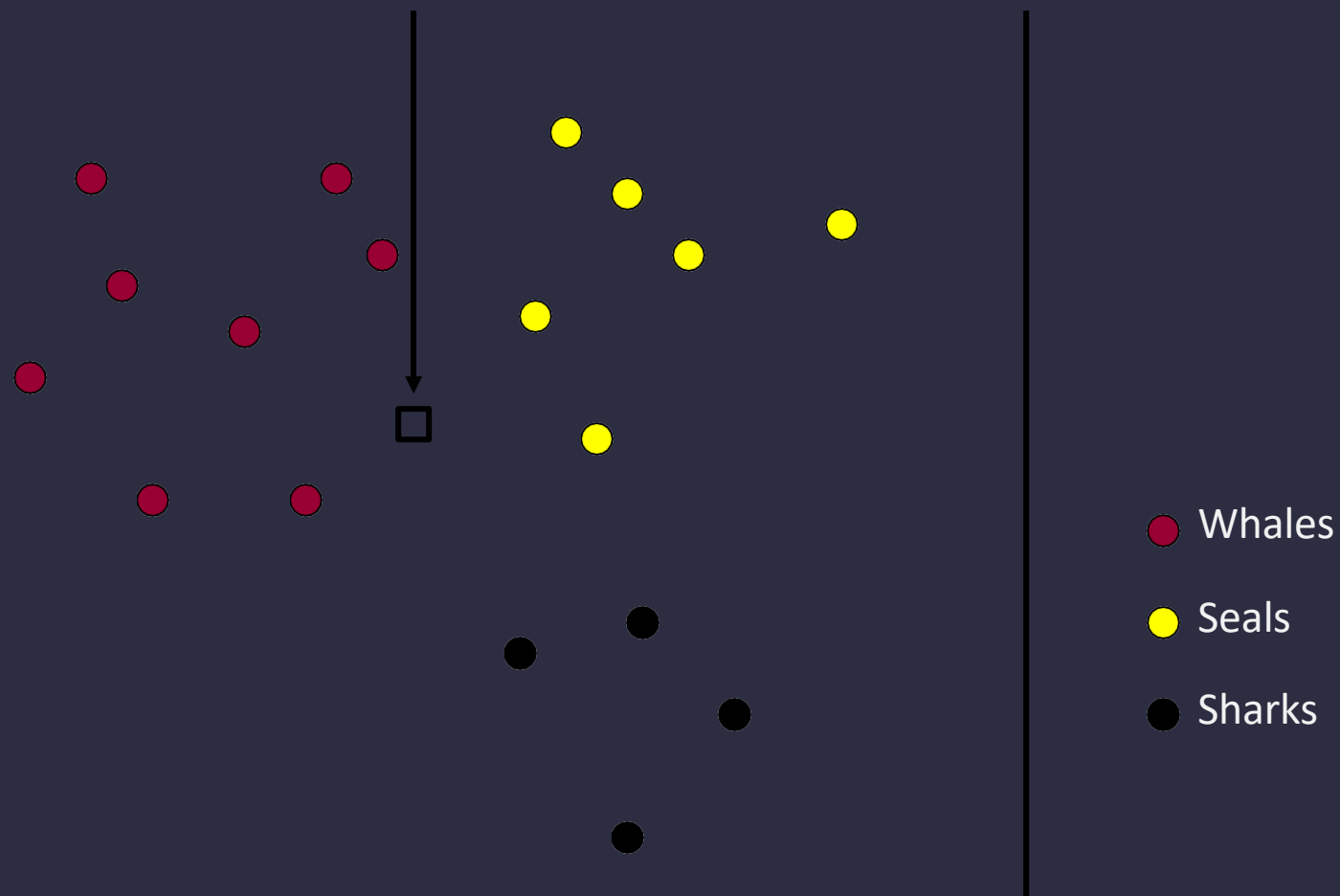


3-Nearest Neighbor (kNN) classifier

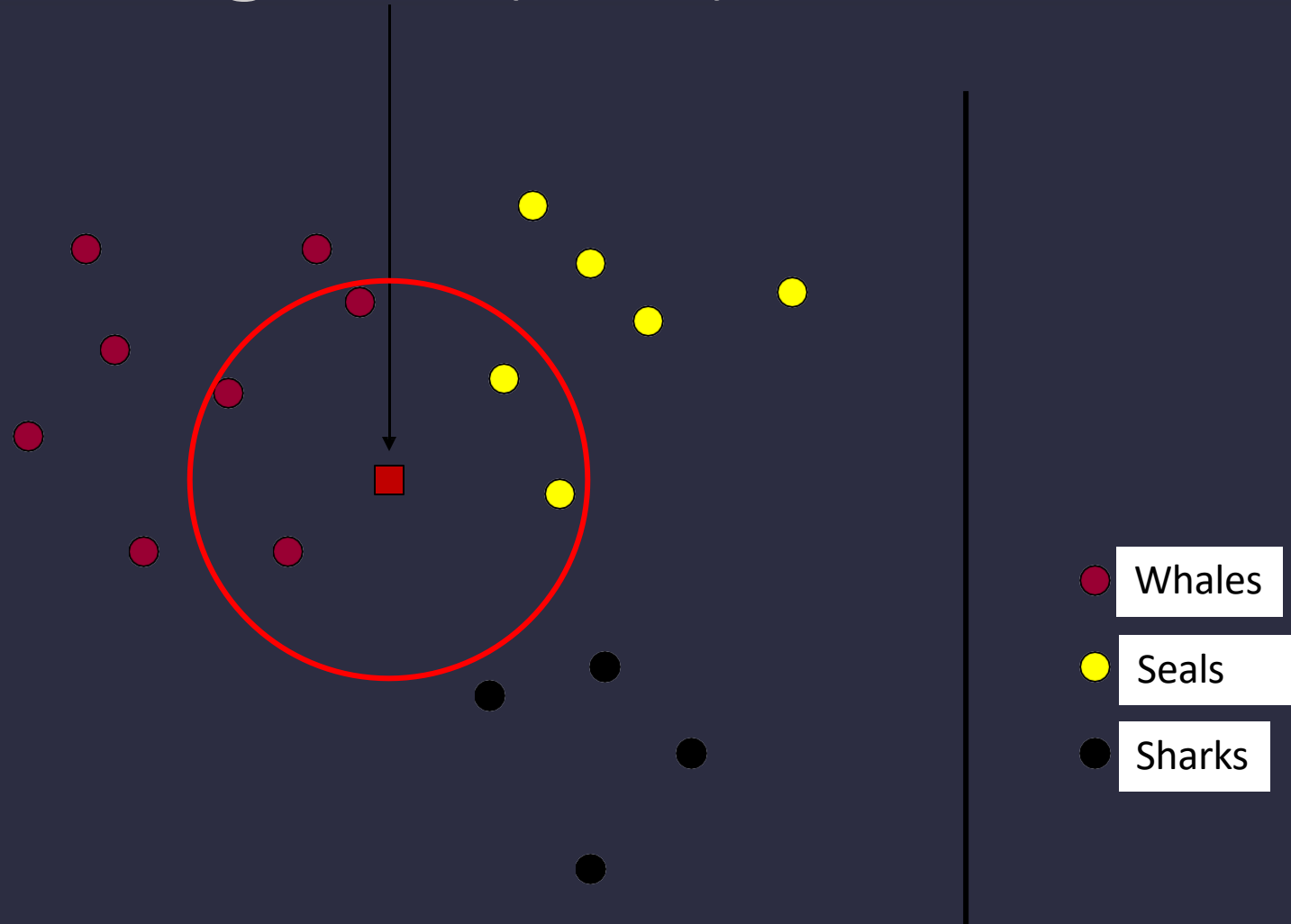


kNN classifier (k=5)

Test subject



5-Nearest Neighbor (kNN) classifier



What is the best k ?

How do we choose a learner that is accurate and also generalizes to unseen data?

- Larger $k \rightarrow$ predicted label is more stable
- Smaller $k \rightarrow$ predicted label is more affected by individual training points

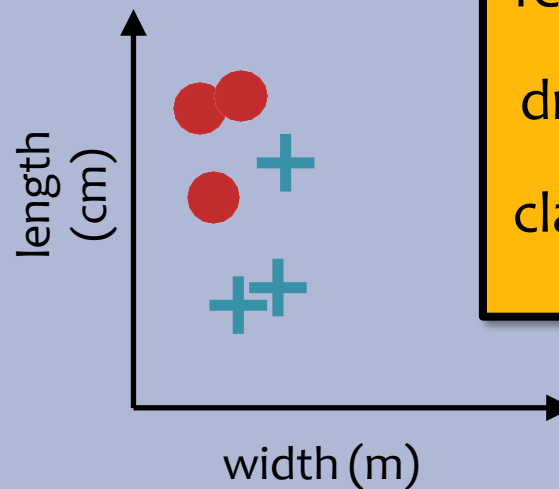
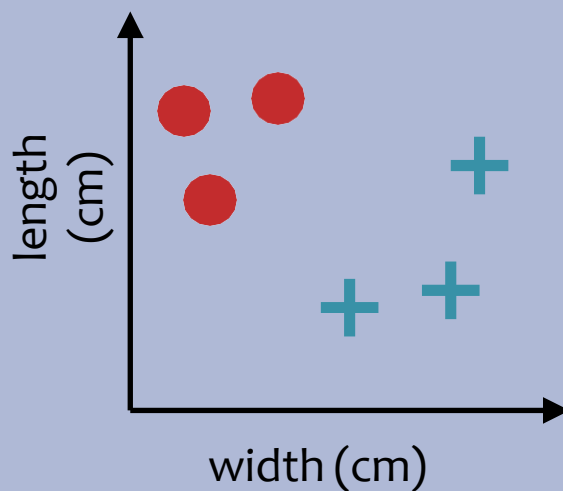
But how to choose k ?

k-NN: Details

Inductive Bias:

1. Close points should have similar labels
2. All dimensions are created equally!

Example: two features for k-NN



big problem:
feature scale
could
dramatically
influence
classification
results

KNN Mini Project

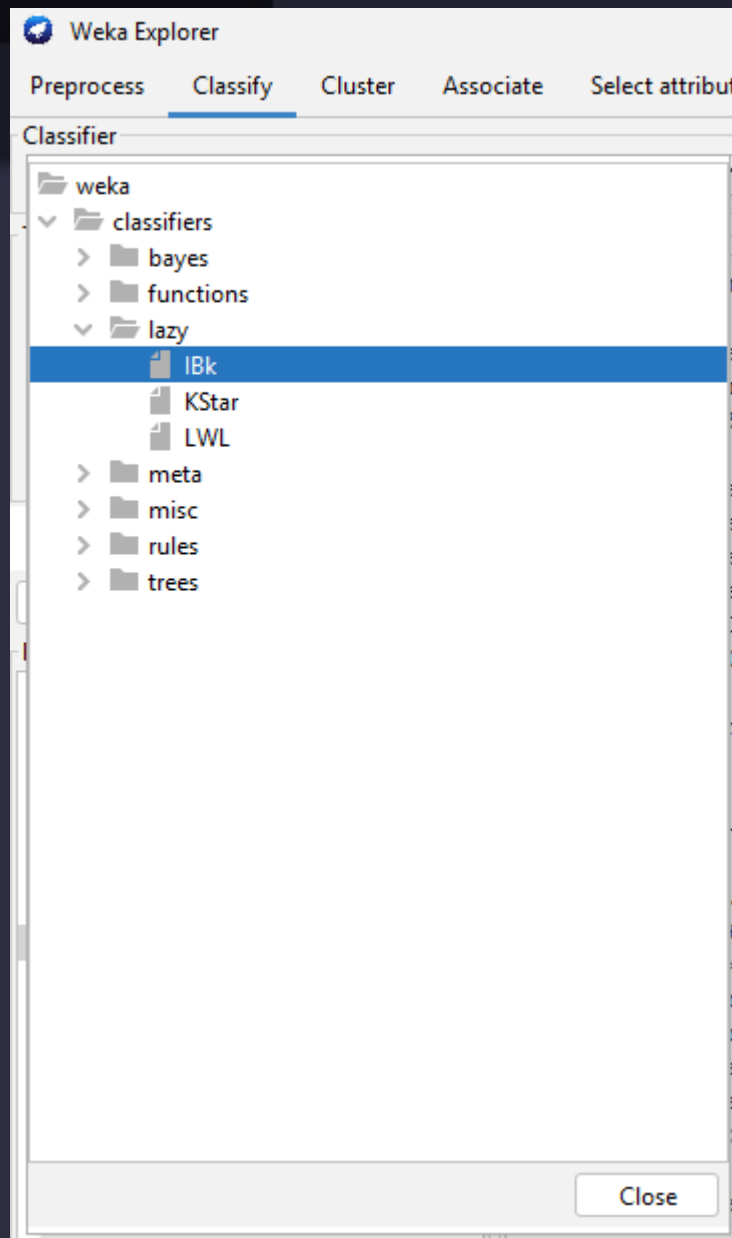
Visit to view project specifications

http://levent.tc/files/courses/big_data/mini_projects/knn/proje1_knn.pdf

Prepare a presentation

KNN on Weka

Select Classifier



KNN on Weka

Settings

weka.gui.GenericObjectEditor

weka.classifiers.lazy.IBk

About

K-nearest neighbours classifier.

More

Capabilities

KNN

batchSize

crossValidate

debug

distanceWeighting

doNotCheckCapabilities

meanSquared

nearestNeighbourSearchAlgorithm **LinearNNSearch** -A "weka.core.Euclidean"

numDecimalPlaces

windowSize

Open... Save... OK Cancel

KNN on Weka

Classification

Weka Explorer

Preprocess **Classify** Cluster Associate Select attributes Visualize

Classifier: Choose **IBk -K 3 -W 0 -A "weka.core.neighboursearch.LinearNNSearch -A \"weka.core.EuclideanDistance -R first-last\""**

Test options

☐ Use training set

☐ Supplied test set

☒ Cross-validation Folds

☐ Percentage split %

(Nom) class

Result list (right-click for options)

- 17:24:16 - bayes.NaiveBayes
- 17:25:42 - bayes.NaiveBayes
- 17:25:52 - bayes.NaiveBayes
- 17:26:29 - bayes.NaiveBayesMultinomial
- 17:26:33 - bayes.NaiveBayes
- 17:26:34 - bayes.NaiveBayes
- 23:12:04 - trees.DecisionStump
- 23:12:28 - trees.J48
- 23:42:38 - lazy.IBk**

Classifier output

=== Run information ===

Scheme: weka.classifiers.lazy.IBk -K 3 -W 0 -A "weka.core.neighboursearch.LinearNNSearch -A \"weka.core.EuclideanDistance -R first-last\""

Relation: iris

Instances: 150

Attributes: 5

sepalength

sepalwidth

petallength

petalwidth

class

Test mode: 10-fold cross-validation

=== Classifier model (full training set) ===

IB1 instance-based classifier

using 3 nearest neighbour(s) for classification

Time taken to build model: 0 seconds

=== Stratified cross-validation ===

=== Summary ===

Correctly Classified Instances	143	95.3333 %
Kappa statistic	0.93	
Mean absolute error	0.04	
Root mean squared error	0.1703	
Relative absolute error	9.0013 %	
Root relative squared error	36.1192 %	
Total Number of Instances	150	

=== Detailed Accuracy By Class ===

	TP Rate	FP Rate	Precision	Recall	F-Measure	MCC	ROC Area	PRC Area	Class
	1,000	0,000	1,000	1,000	1,000	1,000	1,000	1,000	Iris-setosa
	0,940	0,040	0,922	0,940	0,931	0,896	0,963	0,910	Iris-versicolor
	0,920	0,030	0,939	0,920	0,929	0,895	0,958	0,919	Iris-virginica
Weighted Avg.	0,953	0,023	0,953	0,953	0,953	0,930	0,974	0,943	

=== Confusion Matrix ===

a b c <-- classified as

50 0 0 | a = Iris-setosa

0 47 3 | b = Iris-versicolor

0 4 46 | c = Iris-virginica

Decision Tree

Problem Setting

- Set of possible instances X
- Set of possible labels Y
- Unknown target function $f : X \rightarrow Y$
- Set of function hypotheses $H = \{h \mid h : X \rightarrow Y\}$

Input: Training examples of unknown target function f

$$\{\langle \mathbf{x}_i, y \rangle\}_{i=1}^n = \{\langle \mathbf{x}_1, y_1 \rangle, \dots, \langle \mathbf{x}_n, y_n \rangle\}$$

Output: Best approximates f

Sample Dataset

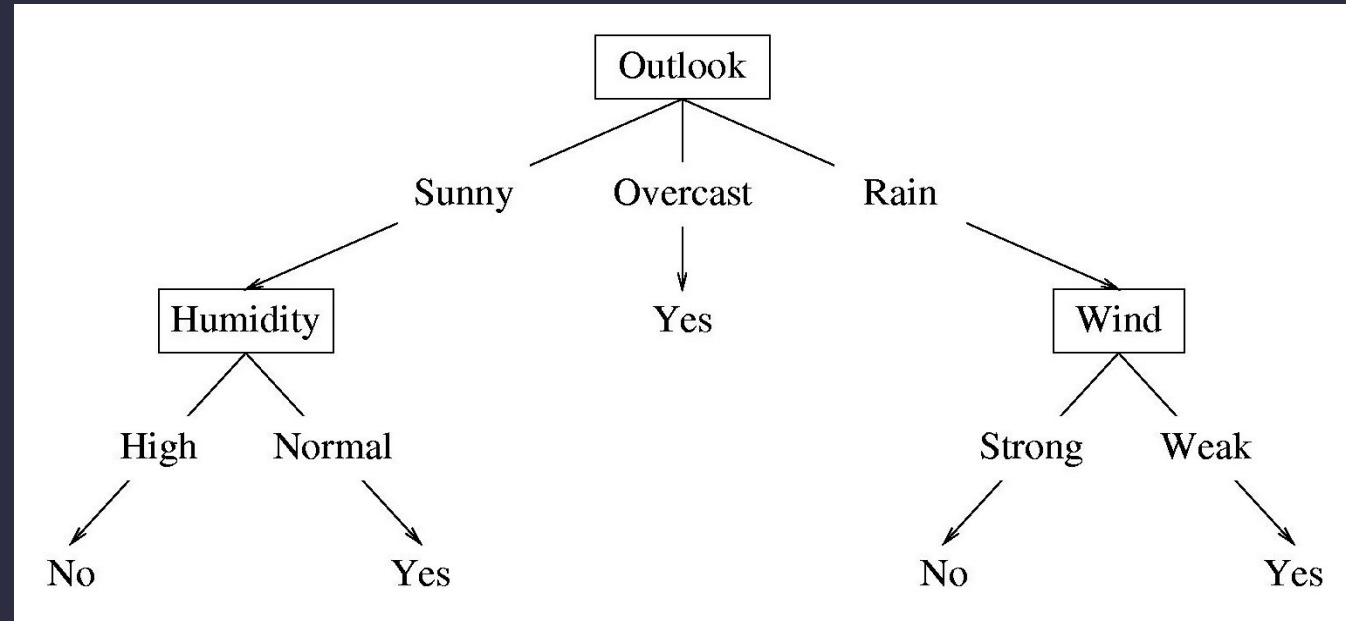
- Columns denote features X_i
- Rows denote labeled instances \mathbf{x}_i, y_i
- Class label denotes whether a tennis game was played

\mathbf{x}_i, y_i

Predictors				Response
Outlook	Temperature	Humidity	Wind	Class
Sunny	Hot	High	Weak	No
Sunny	Hot	High	Strong	No
Overcast	Hot	High	Weak	Yes
Rain	Mild	High	Weak	Yes
Rain	Cool	Normal	Weak	Yes
Rain	Cool	Normal	Strong	No
Overcast	Cool	Normal	Strong	Yes
Sunny	Mild	High	Weak	No
Sunny	Cool	Normal	Weak	Yes
Rain	Mild	Normal	Weak	Yes
Sunny	Mild	Normal	Strong	Yes
Overcast	Mild	High	Strong	Yes
Overcast	Hot	Normal	Weak	Yes
Rain	Mild	High	Strong	No

Decision Tree

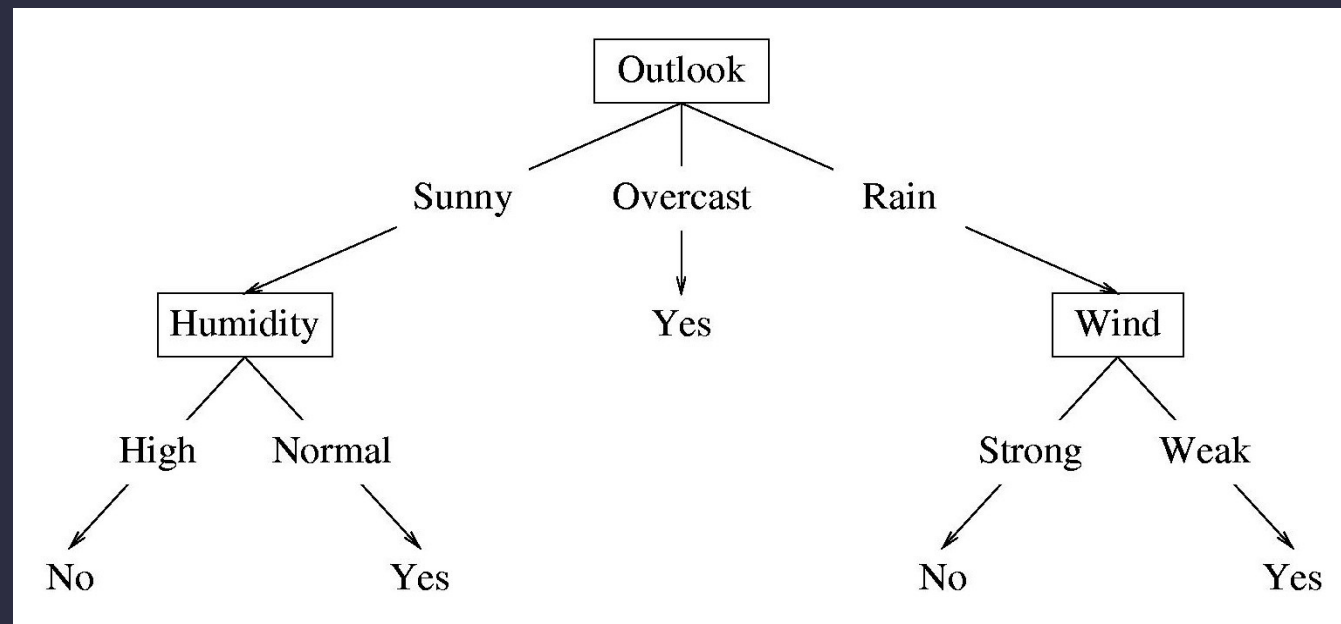
- A possible decision tree for the data:



- Each internal node: test one attribute X_i
- Each branch from a node: selects one value for X_i
- Each leaf node: predict Y

Decision Tree

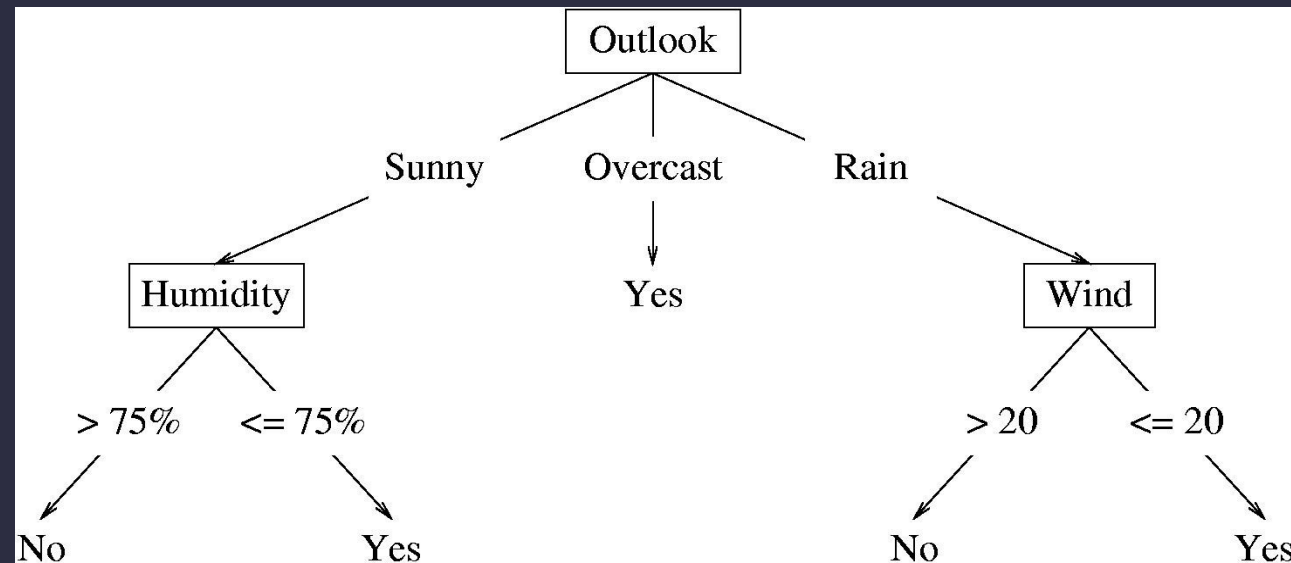
- A possible decision tree for the data:



- What prediction would we make for
<outlook=sunny, temperature=hot, humidity=high, wind=weak> ?

Decision Tree

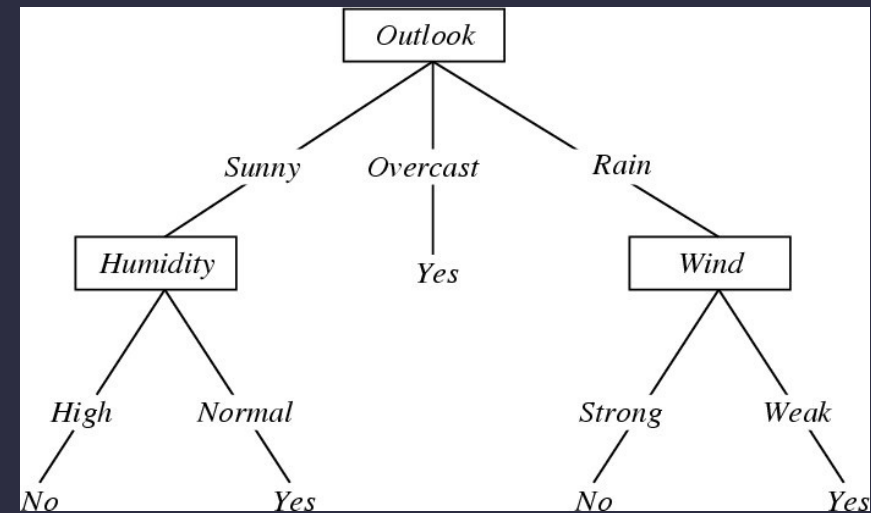
- If features are continuous, internal nodes can test the value of a feature against a threshold



Decision Tree Learning

Problem Setting:

- Set of possible instances X
 - each instance x in X is a feature vector
 - e.g., $\langle \text{Humidity}=\text{low}, \text{Wind}=\text{weak}, \text{Outlook}=\text{rain}, \text{Temp}=\text{hot} \rangle$
- Unknown target function $f: X \rightarrow Y$
 - Y is discrete valued
- Set of function hypotheses $H = \{ h \mid h : X \rightarrow Y \}$
 - each hypothesis h is a decision tree
 - trees sorts x to leaf, which assigns y



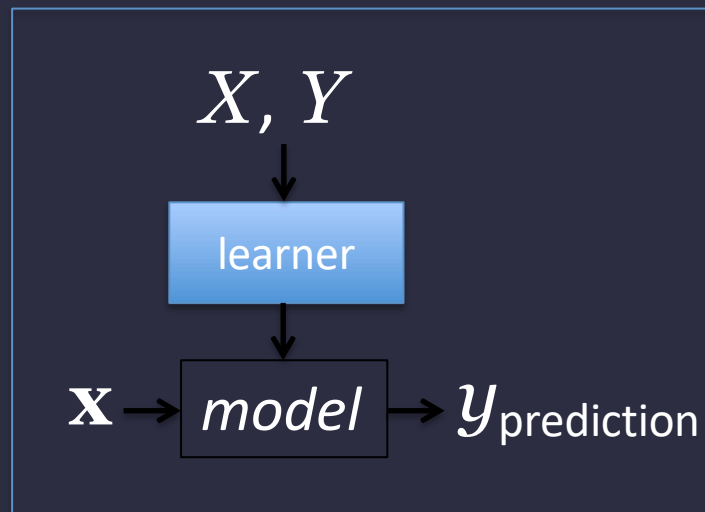
Stages of (Batch) Machine Learning

Given: labeled training data $X, Y = \{h\mathbf{x}_i, y_i\}_{i=1}^n$

- Assumes each $\mathbf{x}_i \leftarrow D(X)$ with $y_i = f_{target}(\mathbf{x}_i)$

Train the model:

$model \leftarrow classifier.train(X, Y)$

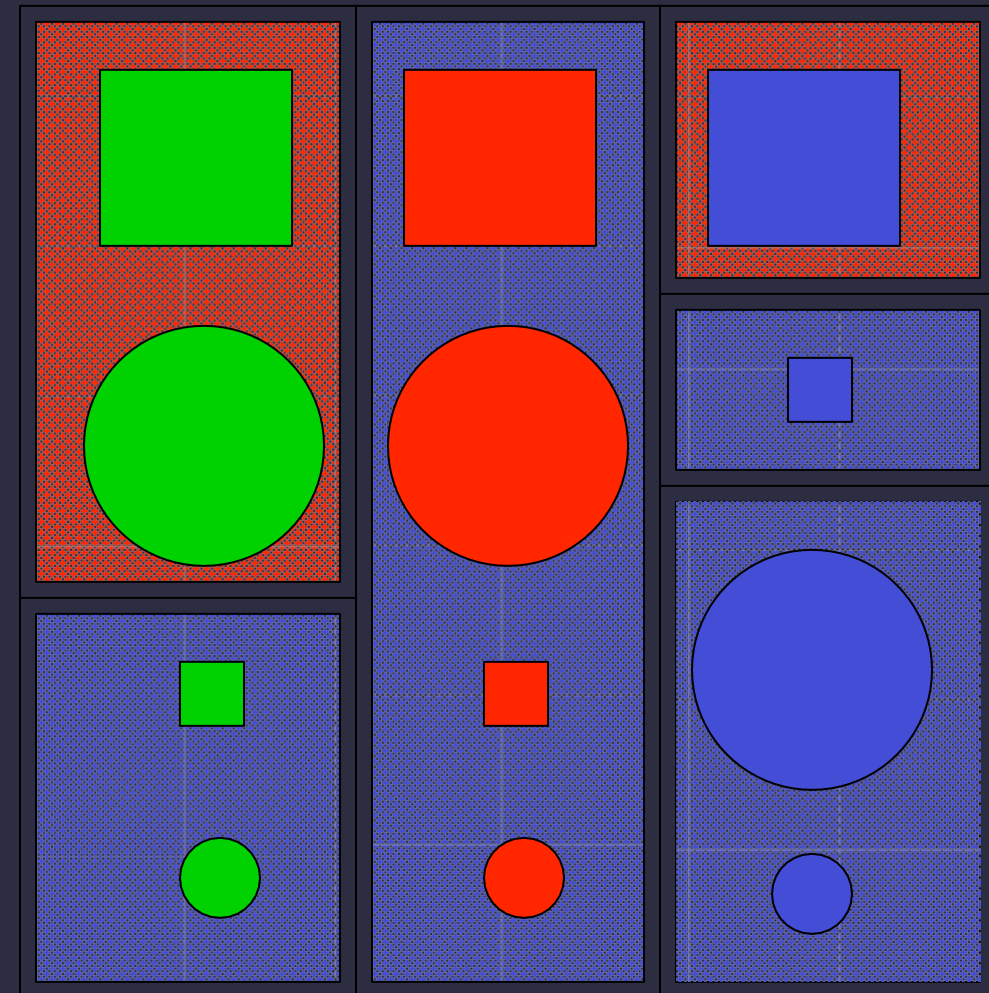
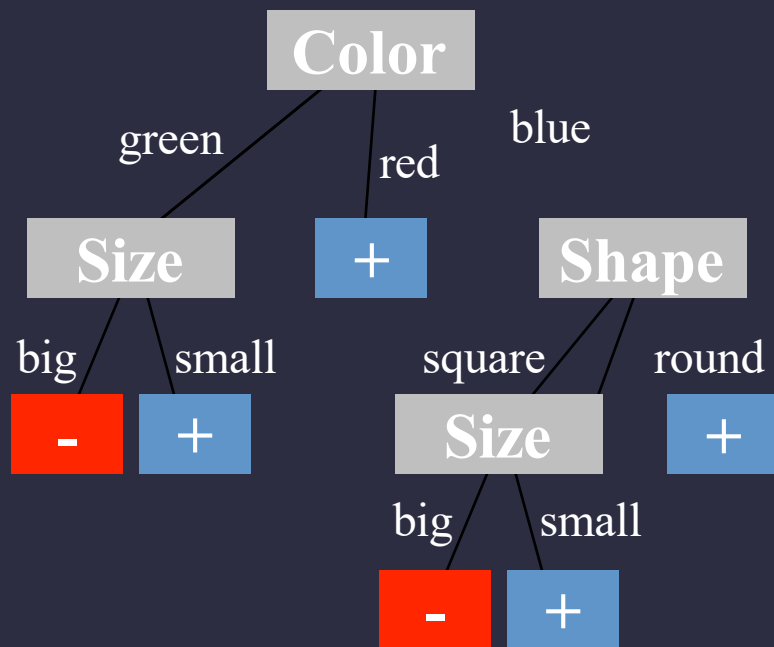


Apply the model to new data:

- Given: new unlabeled instance $\mathbf{x} \leftarrow D(X)$

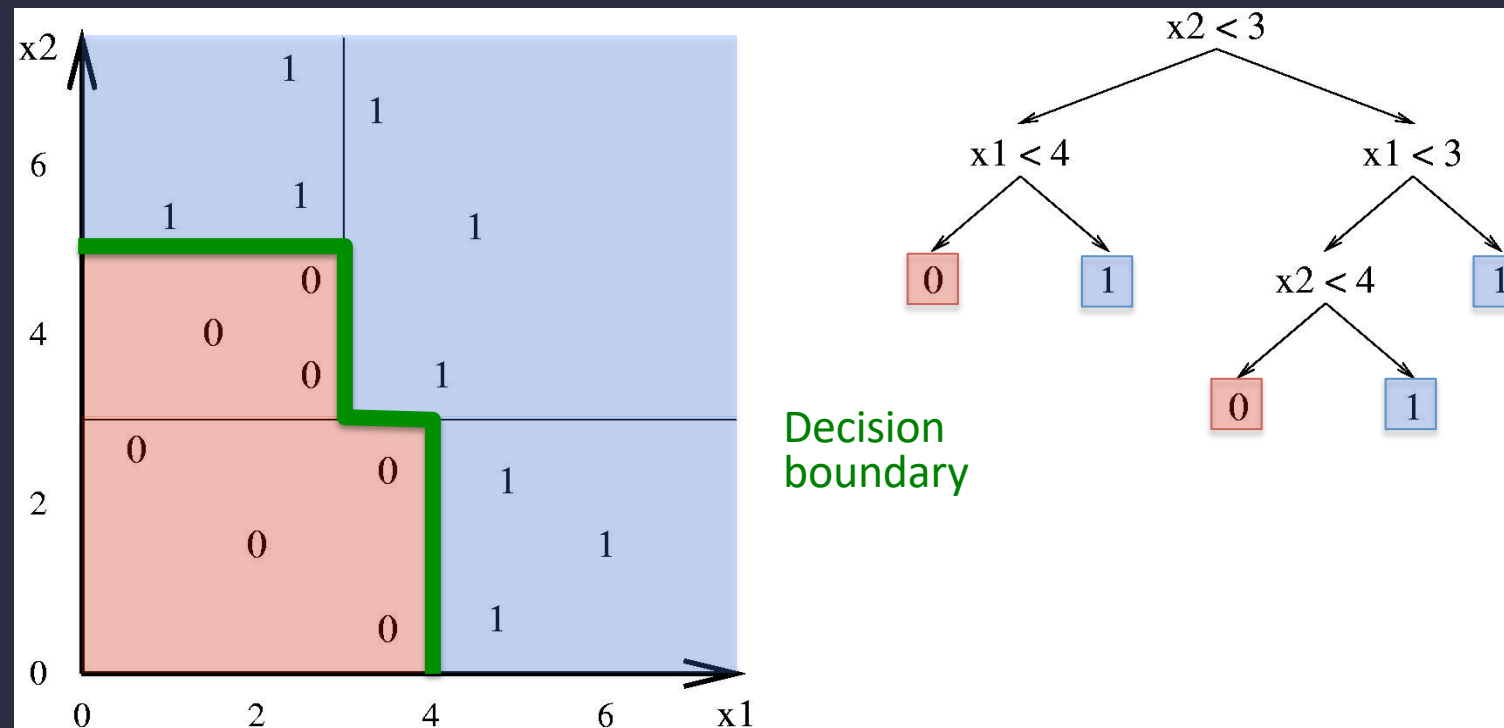
$y_{prediction} \leftarrow model.predict(\mathbf{x})$

Decision Tree Induced Partition



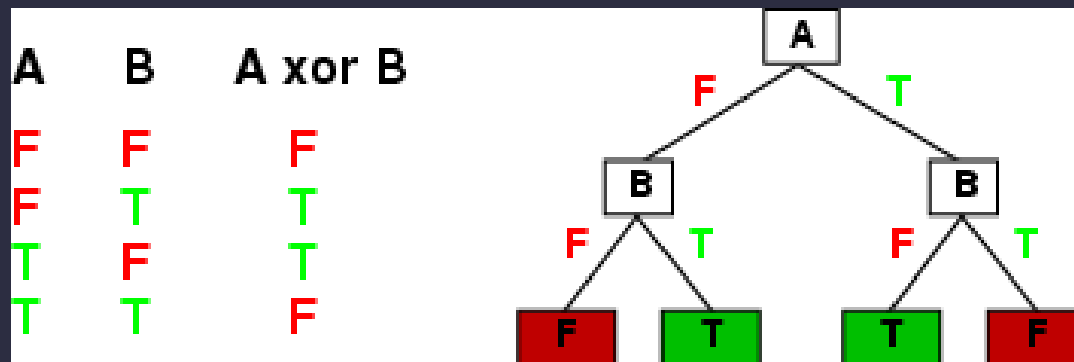
Decision Tree – Decision Boundary

- Decision trees divide the feature space into axis-parallel (hyper-)rectangles
- Each rectangular region is labeled with one label
 - or a probability distribution over labels



Expressiveness

- Decision trees can represent any boolean function of the input attributes



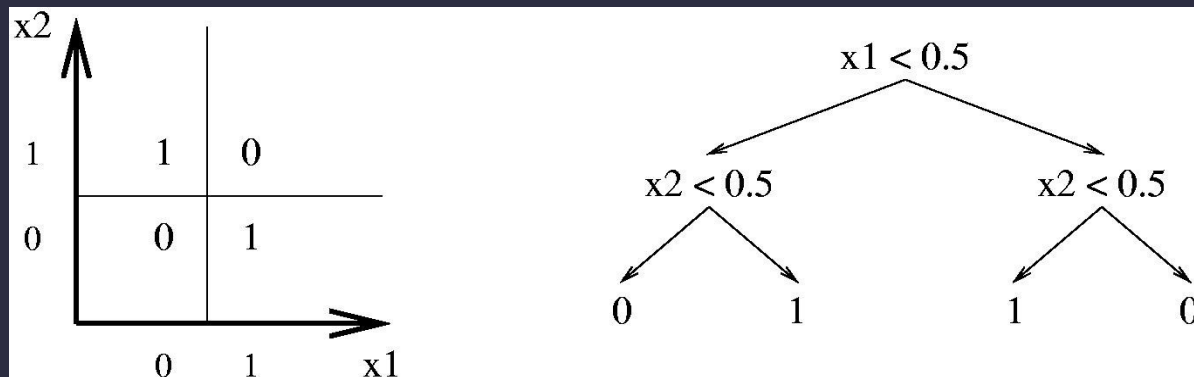
Truth table row → path to leaf

- In the worst case, the tree will require exponentially many nodes

Expressiveness

Decision trees have a variable-sized hypothesis space

- As the #nodes (or depth) increases, the hypothesis space grows
 - Depth 1 (“decision stump”): can represent any boolean function of one feature
 - Depth 2: any boolean fn of two features; some involving three features (e.g., $(x_1 \wedge x_2) \vee (\neg x_1 \wedge \neg x_3)$)
 - etc.



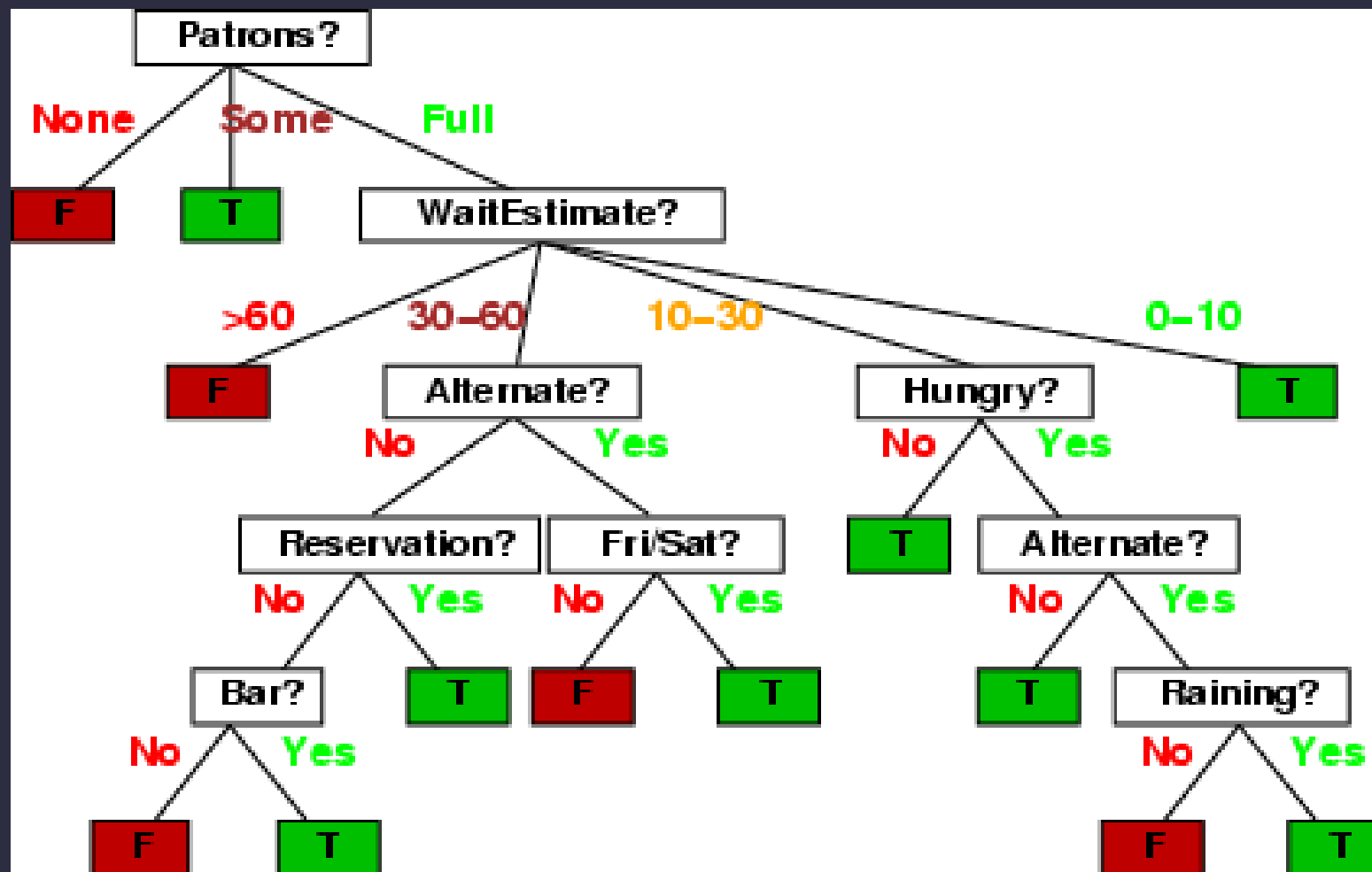
Another Example: Restaurant Domain

Model a patron's decision of whether to wait for a table at a restaurant

Example	Attributes										Target
	<i>Alt</i>	<i>Bar</i>	<i>Fri</i>	<i>Hun</i>	<i>Pat</i>	<i>Price</i>	<i>Rain</i>	<i>Res</i>	<i>Type</i>	<i>Est</i>	<i>Wait</i>
X_1	T	F	F	T	Some	\$\$\$	F	T	French	0-10	T
X_2	T	F	F	T	Full	\$	F	F	Thai	30-60	F
X_3	F	T	F	F	Some	\$	F	F	Burger	0-10	T
X_4	T	F	T	T	Full	\$	F	F	Thai	10-30	T
X_5	T	F	T	F	Full	\$\$\$	F	T	French	>60	F
X_6	F	T	F	T	Some	\$\$	T	T	Italian	0-10	T
X_7	F	T	F	F	None	\$	T	F	Burger	0-10	F
X_8	F	F	F	T	Some	\$\$	T	T	Thai	0-10	T
X_9	F	T	T	F	Full	\$	T	F	Burger	>60	F
X_{10}	T	T	T	T	Full	\$\$\$	F	T	Italian	10-30	F
X_{11}	F	F	F	F	None	\$	F	F	Thai	0-10	F
X_{12}	T	T	T	T	Full	\$	F	F	Burger	30-60	T

~7,000 possible cases

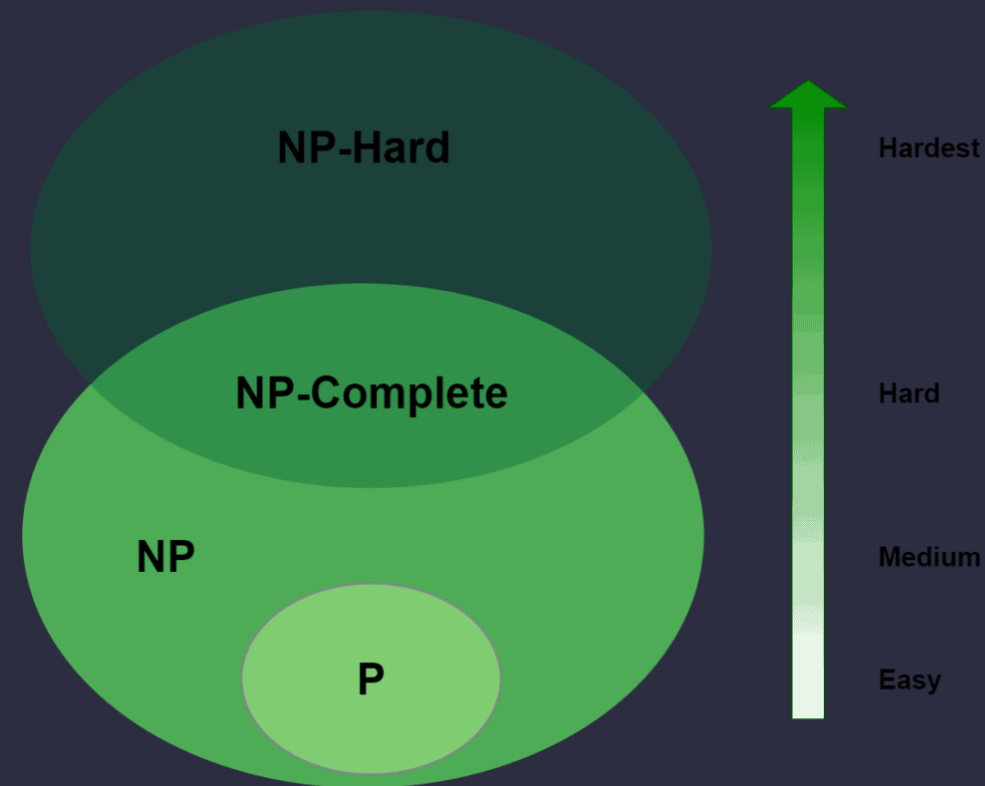
A Decision Tree from Introspection



Is this the best decision tree?

Decision Tree

- The smallest decision tree that correctly classifies all of the training examples is best
 - Finding the provably smallest decision tree is NP-hard
 - ...So instead of constructing the absolute smallest tree consistent with the training examples, construct one that is pretty small



Basic Algorithm for Top-Down Induction of Decision Trees

node = root of decision tree

Main loop:

1. $A \leftarrow$ the “best” decision attribute for the next node.
2. Assign A as decision attribute for *node*.
3. For each value of A , create a new descendant of *node*.
4. Sort training examples to leaf nodes.
5. If training examples are perfectly classified, stop.
Else, recurse over new leaf nodes.

How do we choose which attribute is best?

Choosing the Best Attribute

Key problem: choosing which attribute to split a given set of examples

- Some possibilities are:
 - **Random:** Select any attribute at random
 - **Least-Values:** Choose the attribute with the smallest number of possible values
 - **Most-Values:** Choose the attribute with the largest number of possible values
 - **Max-Gain:** Choose the attribute that has the largest expected *information gain*
 - i.e., attribute that results in smallest expected size of subtrees rooted at its children

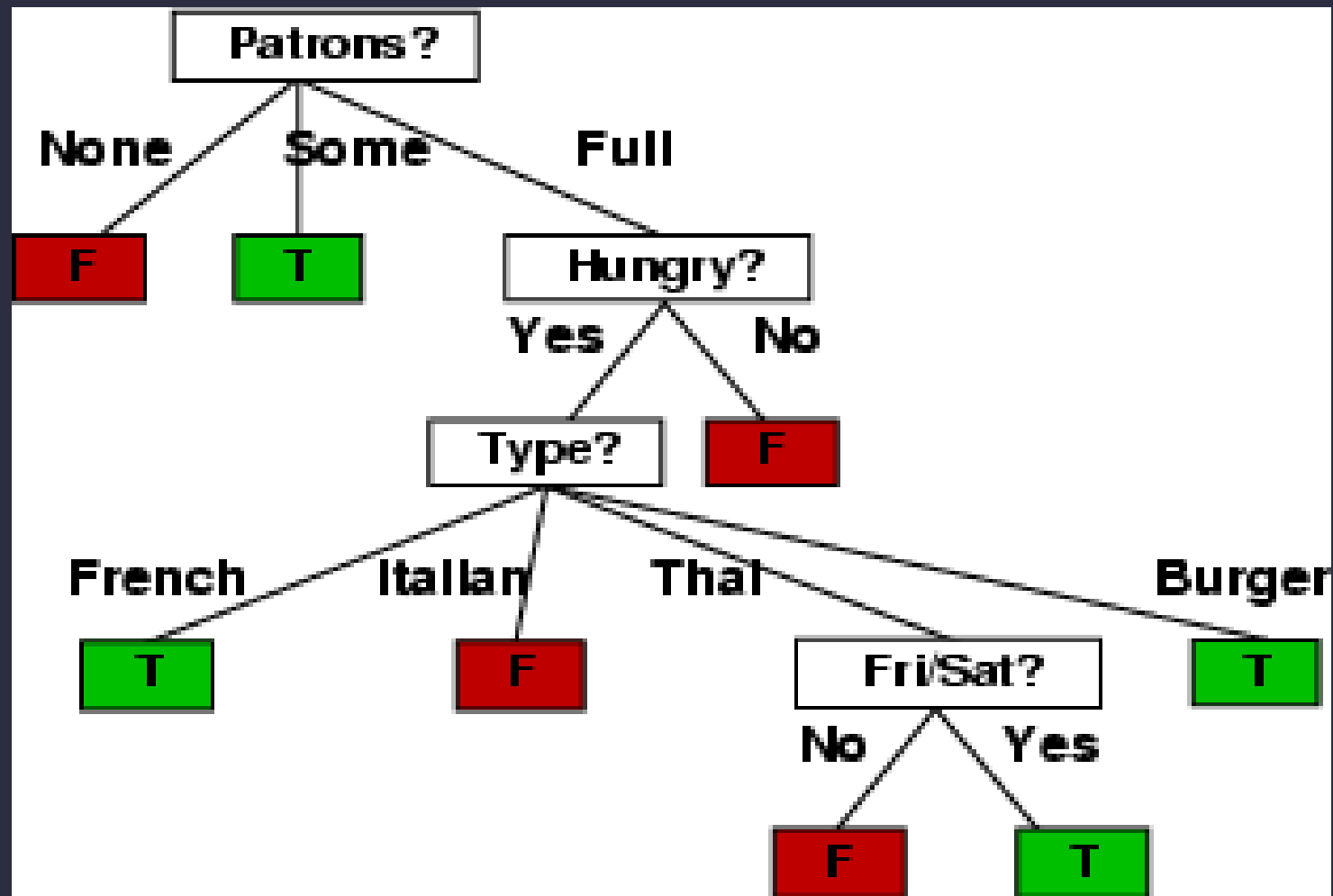
Choosing an Attribute

Idea: a good attribute splits the examples into subsets that are (ideally) “all positive” or “all negative”

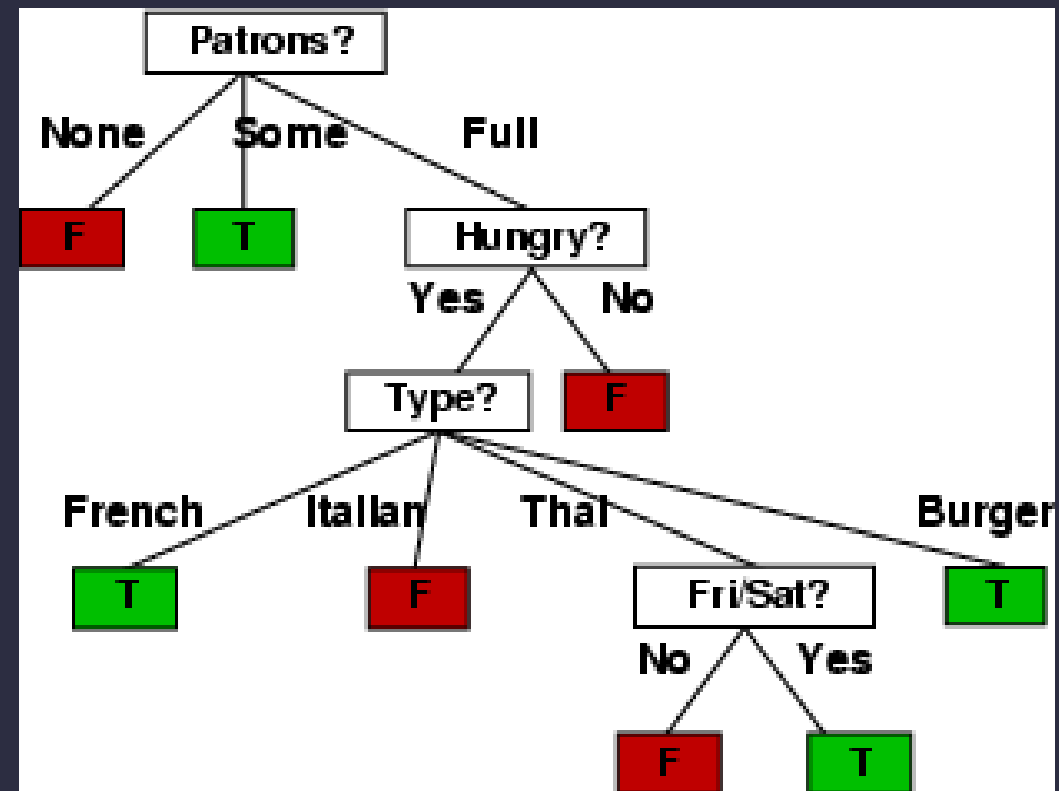
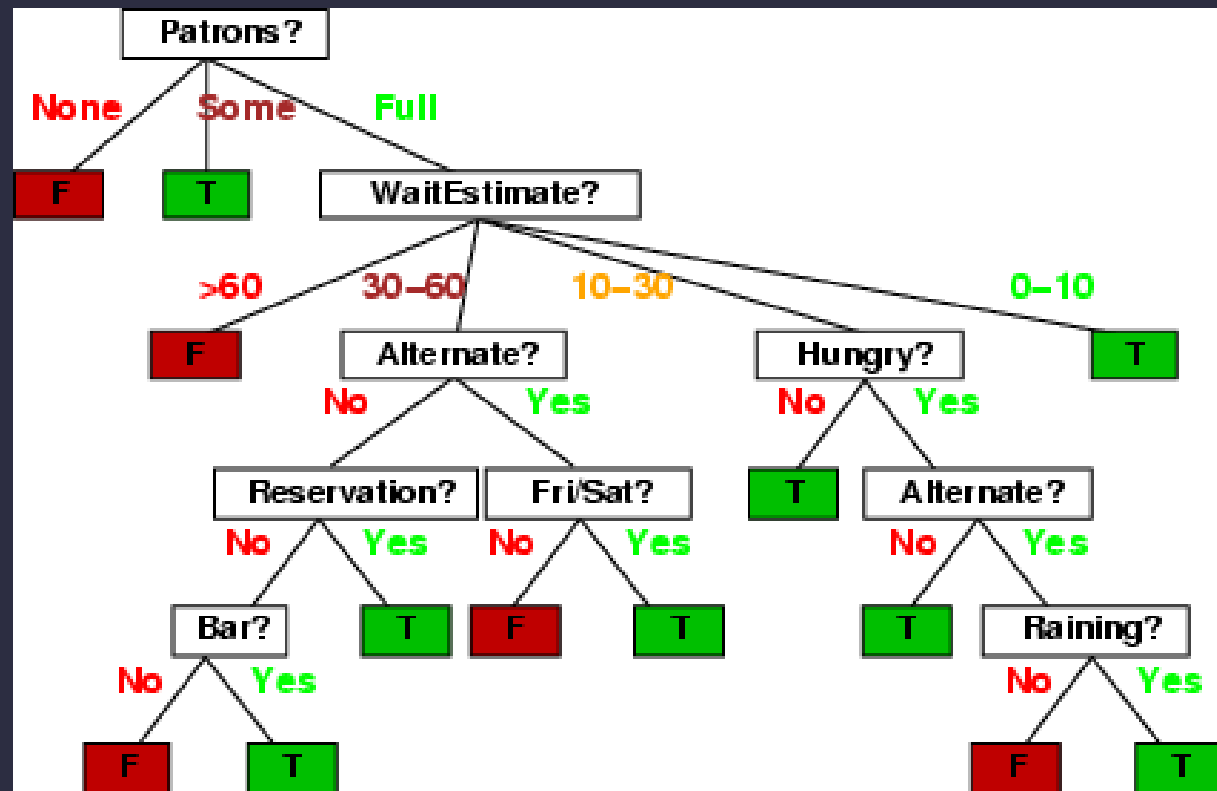


Which split is more informative: *Patrons?* or *Type?*

ID3-induced Decision Tree



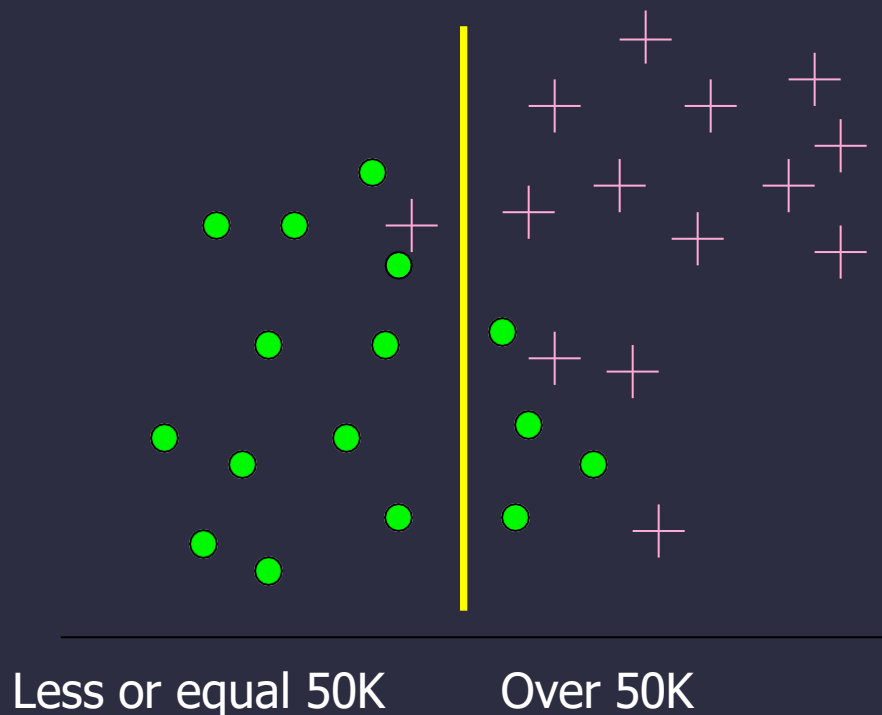
Compare the Two Decision Trees



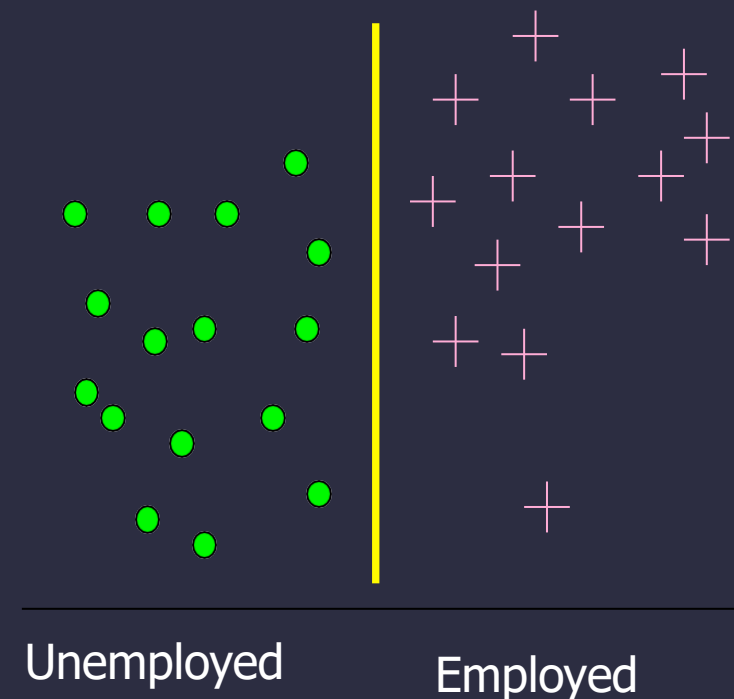
Information Gain

Which test is more informative?

**Split over whether
Balance exceeds 50K**



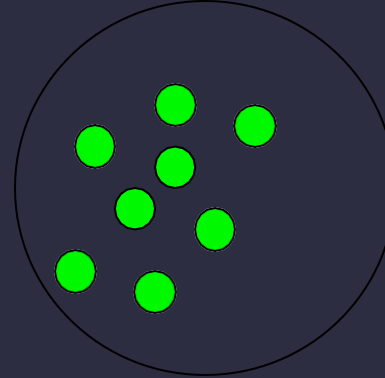
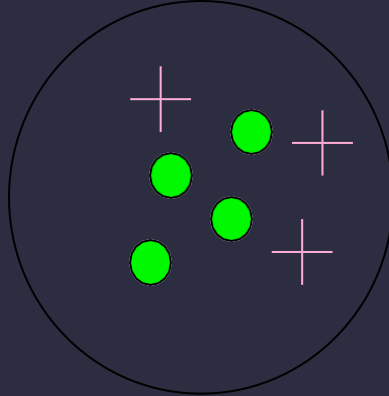
**Split over whether
applicant is employed**



Information Gain

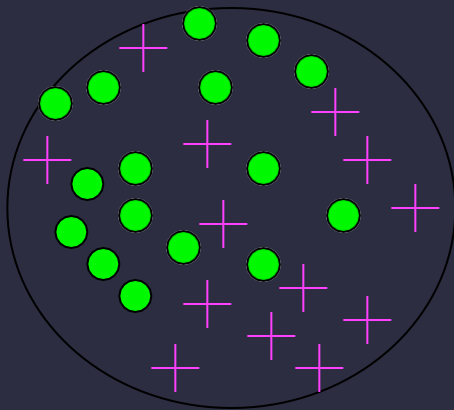
Impurity/Entropy (informal)

- Measures the level of **impurity** in a group of examples

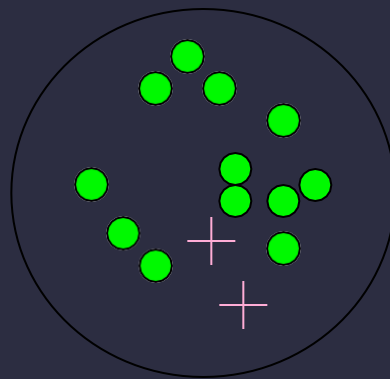


Impurity

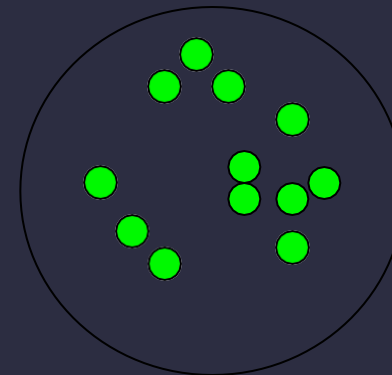
Very impure group



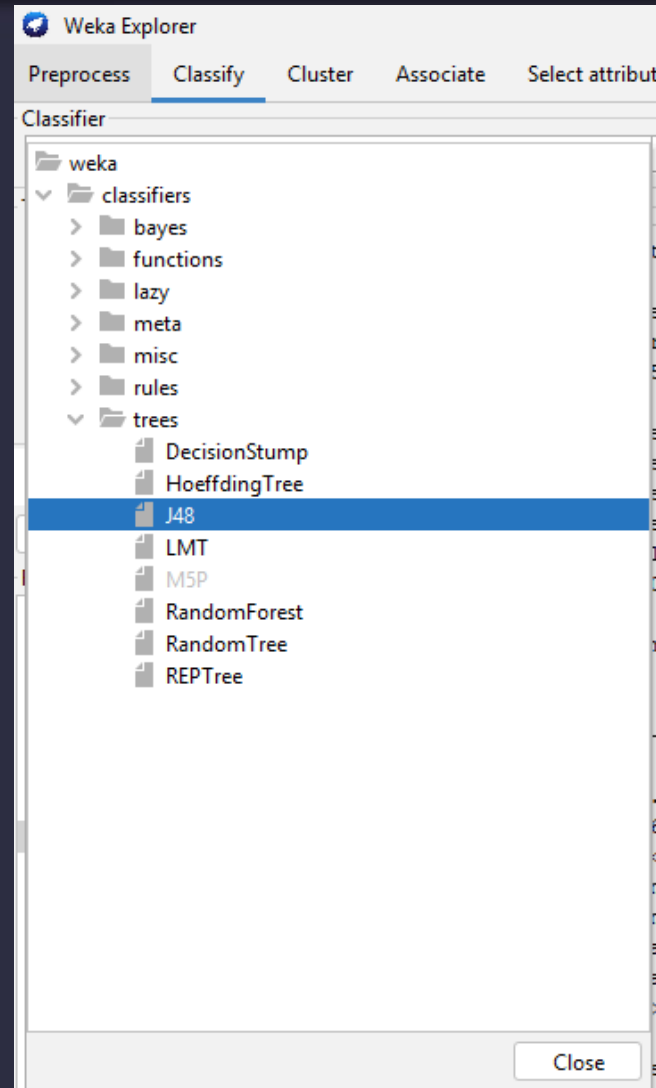
Less impure



Minimum impurity



Select Decision Tree Based Algorithms



Select Decision Tree Based Algorithms

Weka Explorer

Preprocess **Classify** Cluster Associate Select attributes Visualize

Classifier: Choose **J48 -C 0.25 -M 2**

Test options:

- ☐ Use training set
- ☐ Supplied test set (Set...)
- ☒ Cross-validation Folds: 10
- ☐ Percentage split %: 80
- More options...

(Nom) class: Start Stop

Result list (right-click for options):

- 17:24:16 - bayes.NaiveBayes
- 17:25:42 - bayes.NaiveBayes
- 17:25:52 - bayes.NaiveBayes
- 17:26:29 - bayes.NaiveBayesMultinomial
- 17:26:33 - bayes.NaiveBayes
- 17:26:34 - bayes.NaiveBayes
- 23:12:04 - trees.DecisionStump
- 23:12:28 - trees.J48**

Classifier output:

```

=== Run information ===

Scheme:      weka.classifiers.trees.J48 -C 0.25 -M 2
Relation:    iris
Instances:   150
Attributes:  5
              sepalwidth
              sepalwidth
              petalwidth
              petalwidth
              class
Test mode:   10-fold cross-validation

=== Classifier model (full training set) ===

J48 pruned tree
-----

petalwidth <= 0.6: Iris-setosa (50.0)
petalwidth > 0.6
| petalwidth <= 1.7
| | petalwidth <= 4.9: Iris-versicolor (48.0/1.0)
| | petalwidth > 4.9
| | | petalwidth <= 1.5: Iris-virginica (3.0)
| | | petalwidth > 1.5: Iris-versicolor (3.0/1.0)
| | petalwidth > 1.7: Iris-virginica (46.0/1.0)

Number of Leaves :    5

Size of the tree :    9

Time taken to build model: 0 seconds

=== Stratified cross-validation ===
=== Summary ===

Correctly Classified Instances      144          96 %
Kappa statistic                    0.94
Mean absolute error                  0.035
Root mean squared error              0.1586
Relative absolute error              7.8705 %
Root relative squared error          33.6353 %
Total Number of Instances          150

=== Detailed Accuracy By Class ===

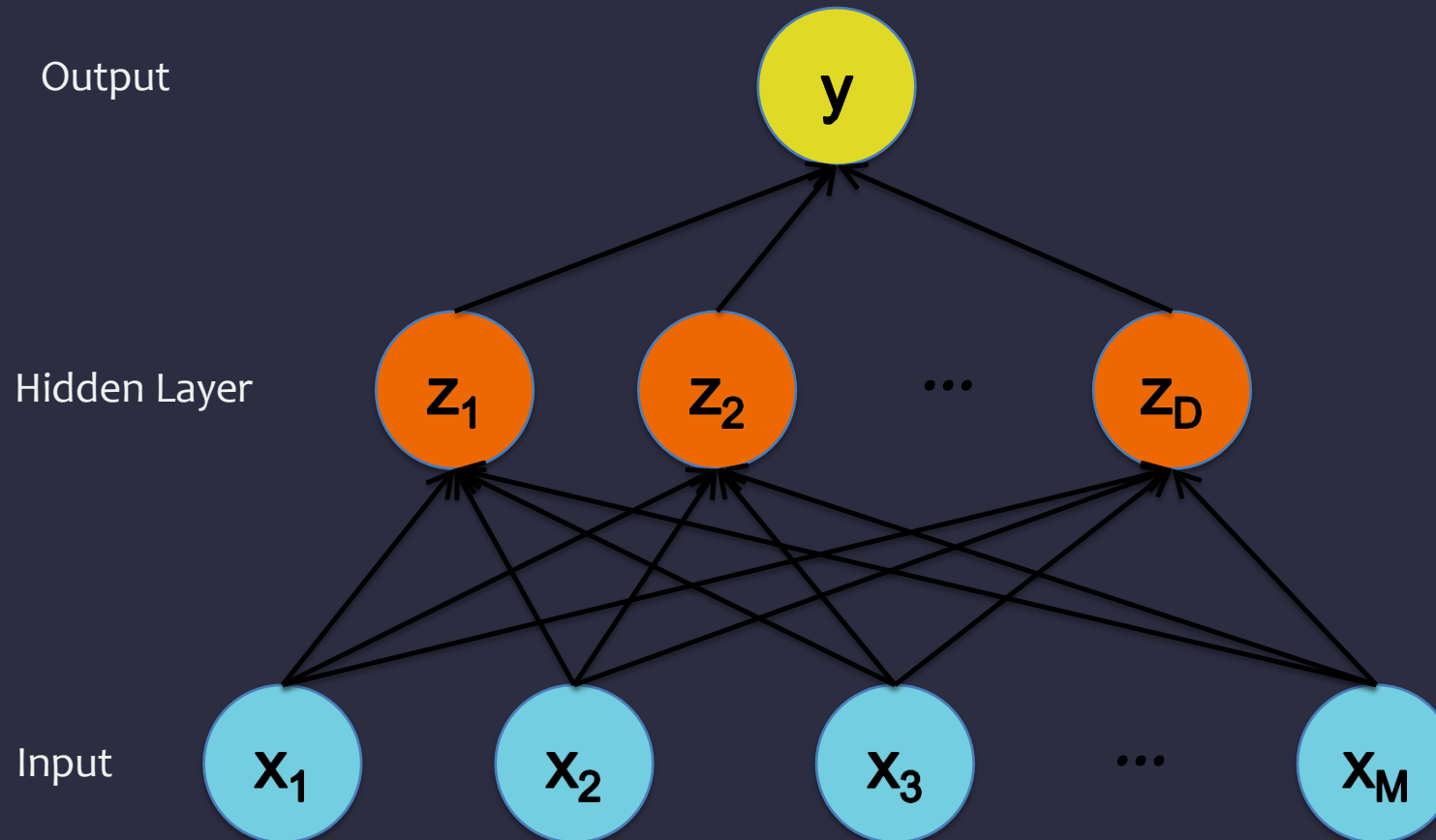
              TP Rate  FP Rate  Precision  Recall  F-Measure  MCC  ROC Area  PRC Area  Class
0.980    0.000    1.000    0.980    0.980    0.985    0.990    0.987    Iris-setosa
0.940    0.030    0.940    0.940    0.940    0.910    0.952    0.880    Iris-versicolor
  
```


Neural Networks

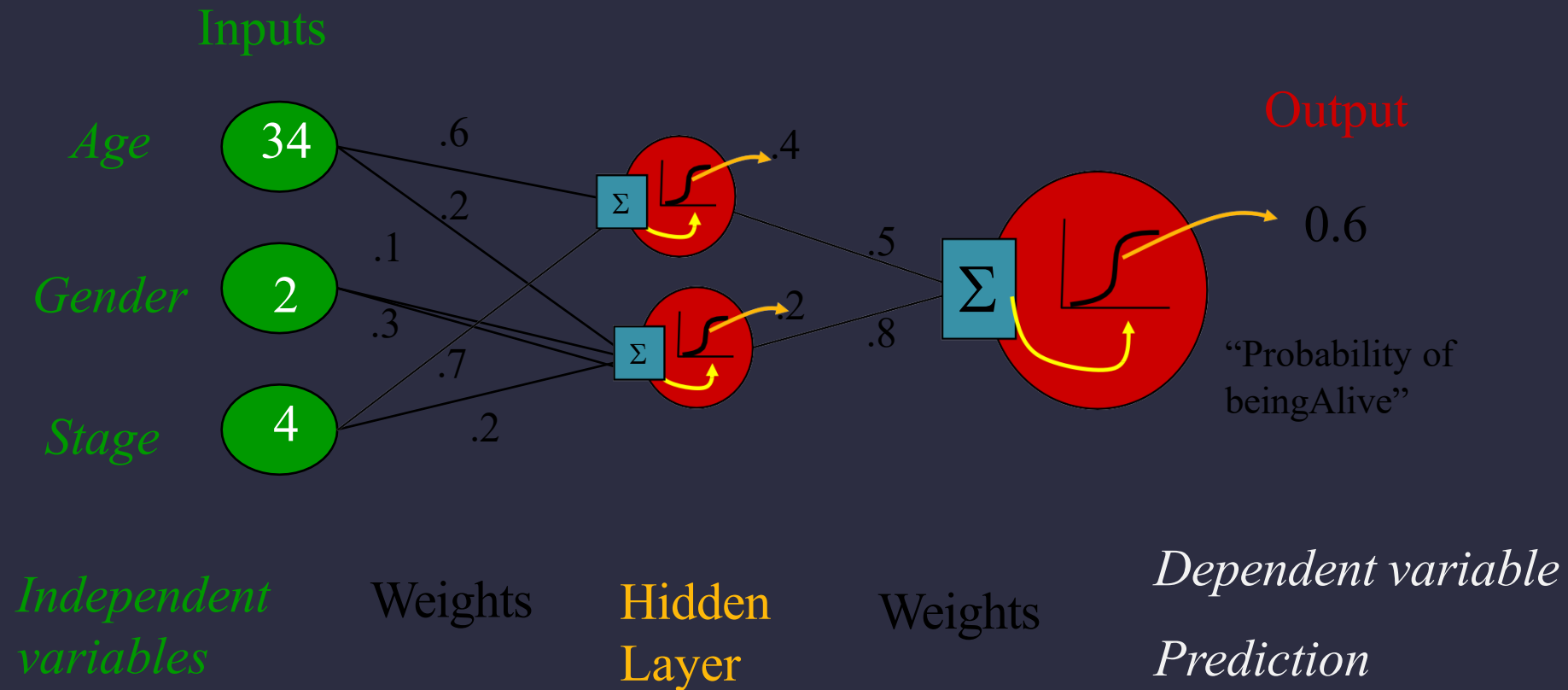
- Analogy to Biological Systems (Indeed a great example of a good learning system)
- Massive Parallelism allowing for computational efficiency
- The first learning algorithm came in 1959 (Rosenblatt) who suggested that if a target output value is provided for a single neuron with fixed inputs, one can incrementally change weights to learn to produce these outputs using the [perceptron learning rule](#)

Decision Functions

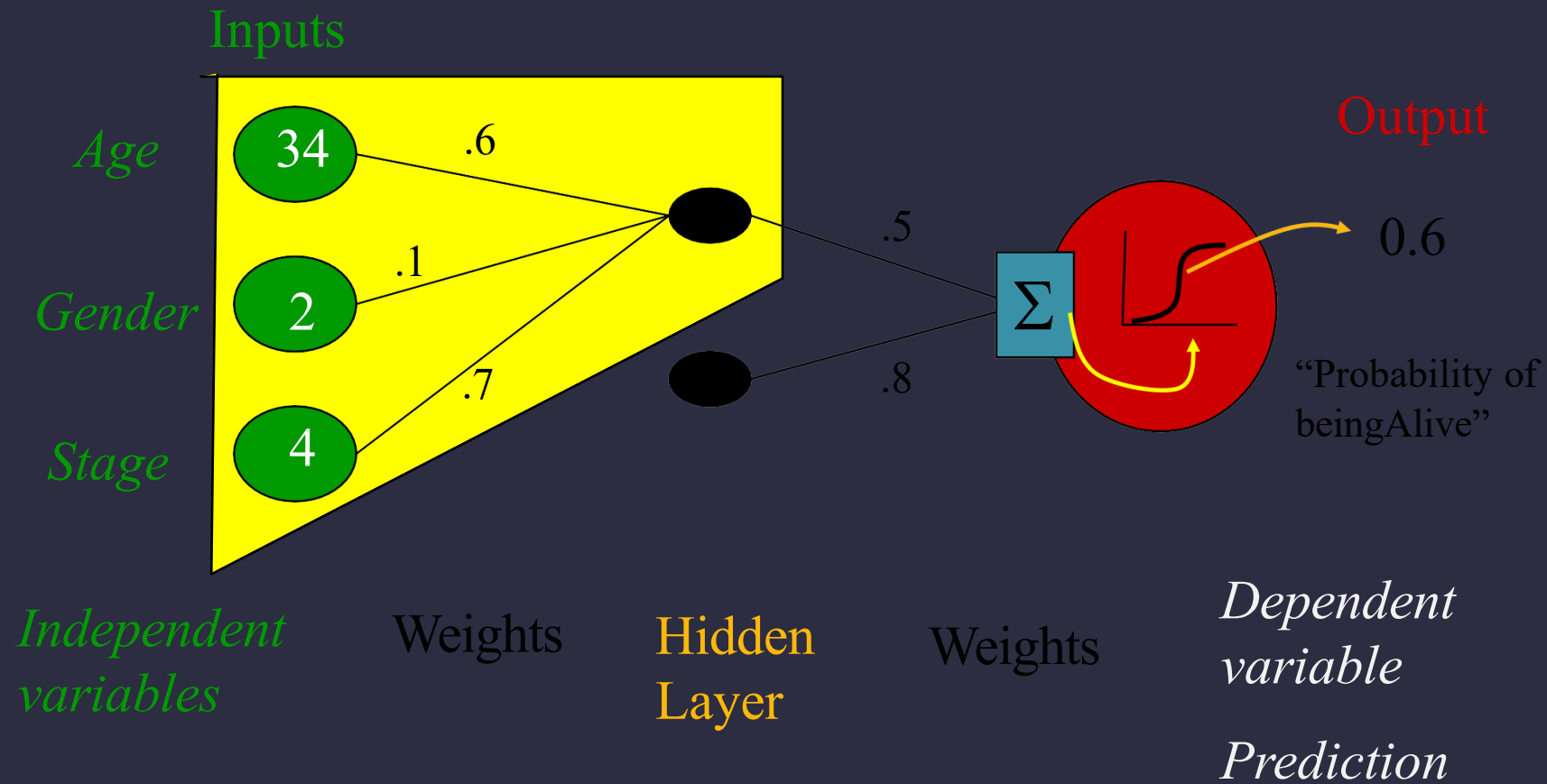
Neural Network

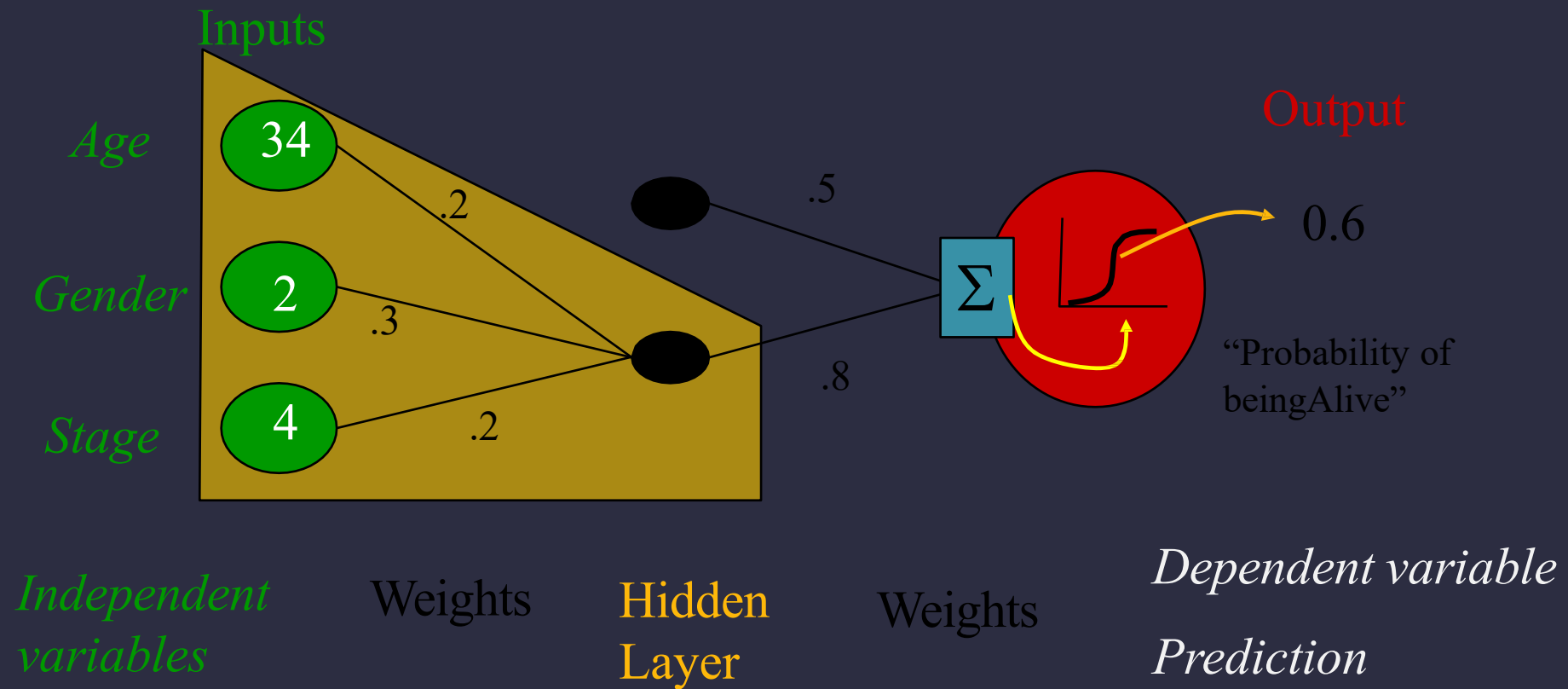


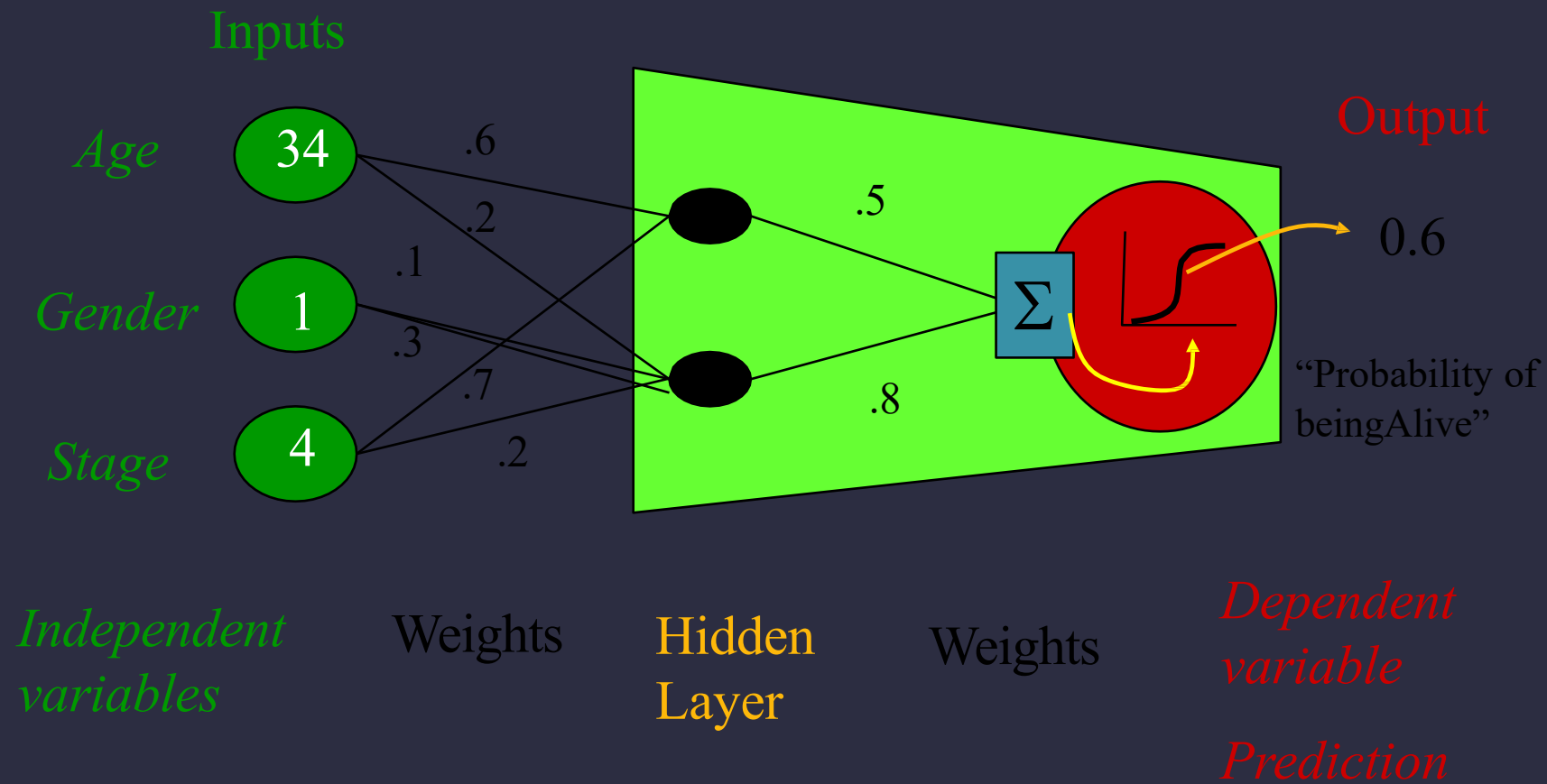
Neural Network Model

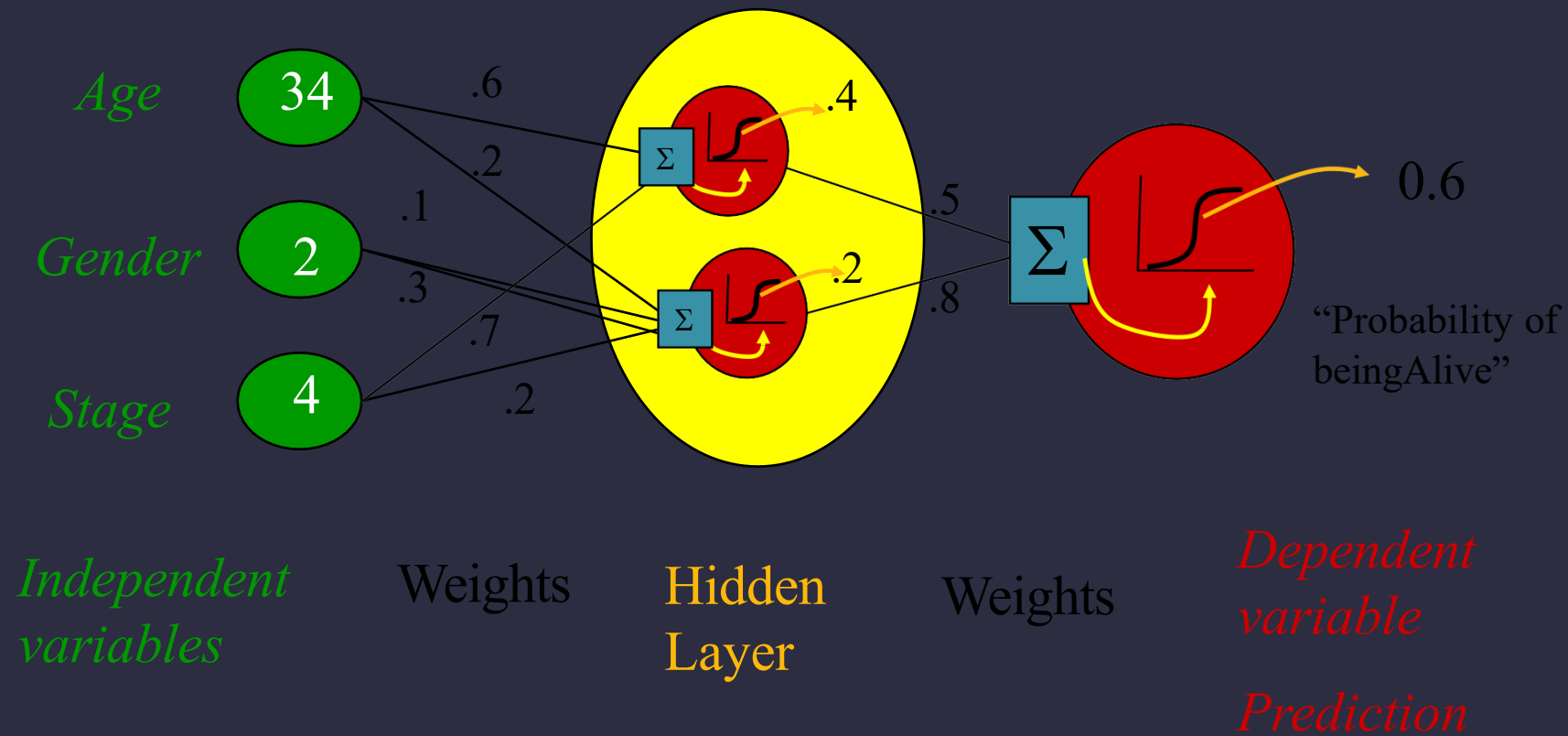


“Combined logistic models”





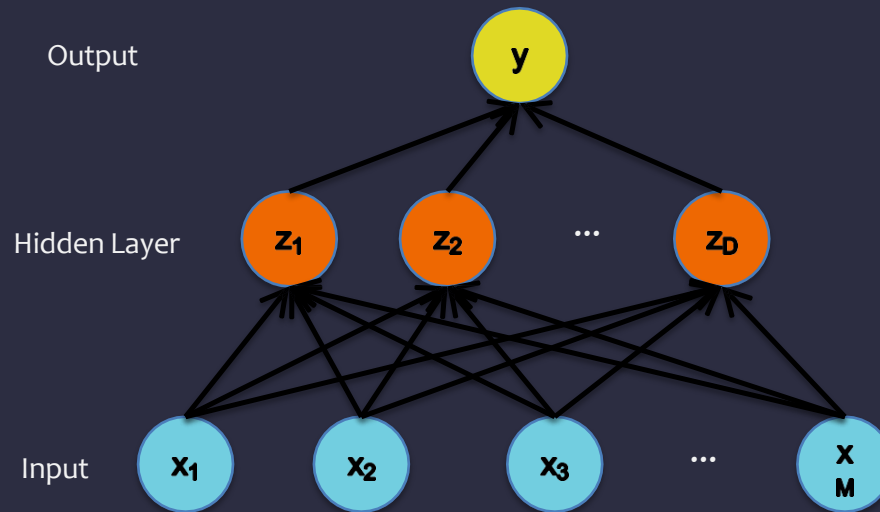




Neural Networks

- Example: Neural Network w/1 Hidden Layer
- Example: Neural Network w/2 Hidden Layers
- Example: Feed Forward Neural Network

Neural Network for Classification



(E) Output (sigmoid)

$$y = \frac{1}{1 + \exp(-b)}$$

(D) Output (linear)

$$b = \sum_{j=0}^D \beta_j z_j$$

(C) Hidden (sigmoid)

$$z_j = \frac{1}{1 + \exp(-a_j)}, \quad \forall j$$

(B) Hidden (linear)

$$a_j = \sum_{i=0}^M \alpha_{ji} x_i, \quad \forall j$$

(A) Input

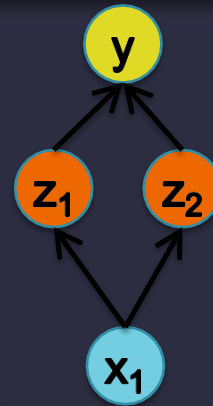
Given $x_i, \quad \forall i$

Neural Network Parameters

- Question:
- Suppose you are training a one-hidden layer neural network with sigmoid activations for binary classification.



True or False: There is a unique set of parameters that maximize the likelihood of the dataset above.



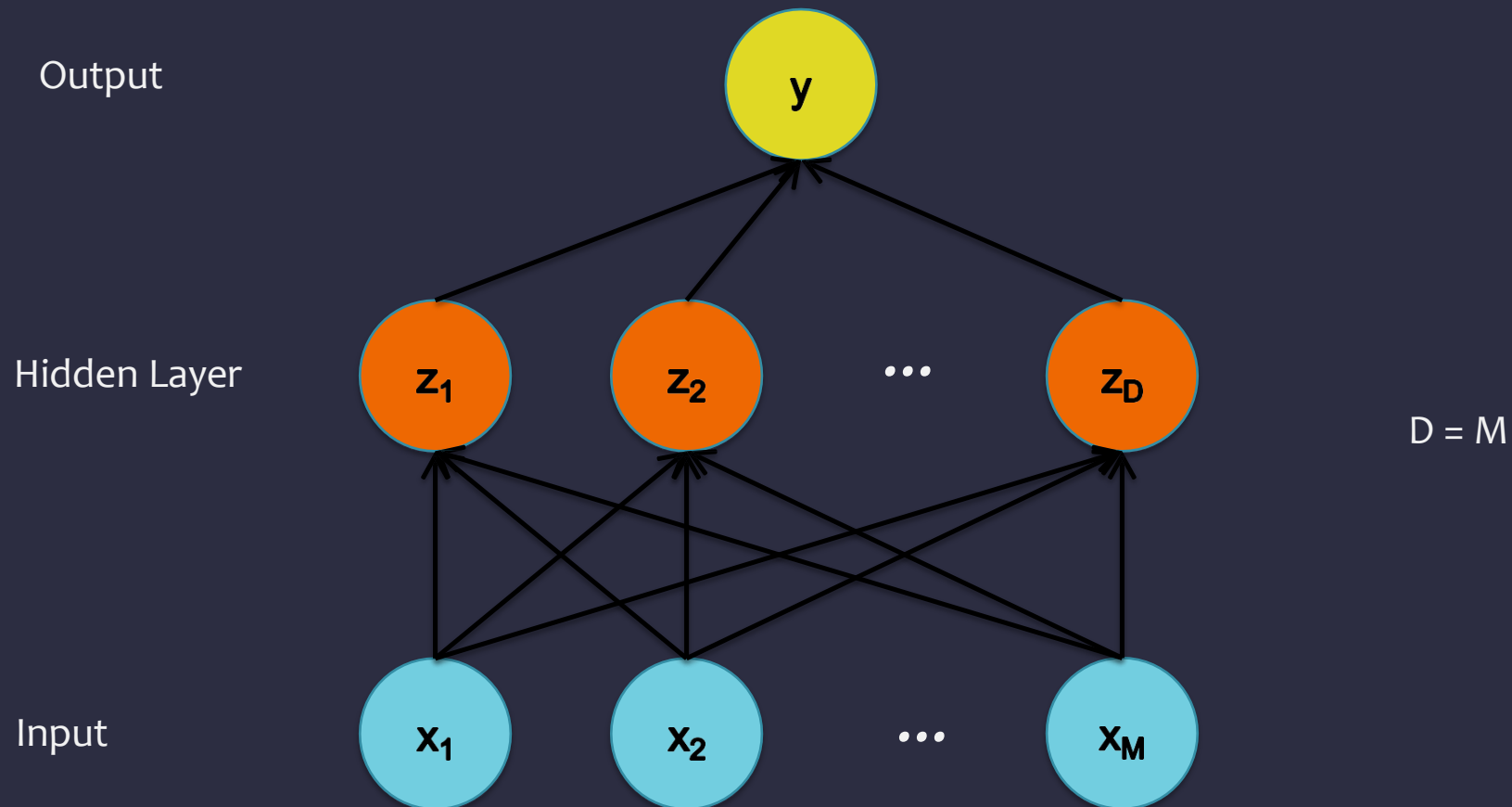
Neural Network Architectures

Even for a basic Neural Network, there are many design decisions to make:

1. # of hidden layers (depth)
2. # of units per hidden layer (width)
3. Type of activation function (nonlinearity)
4. Form of objective function

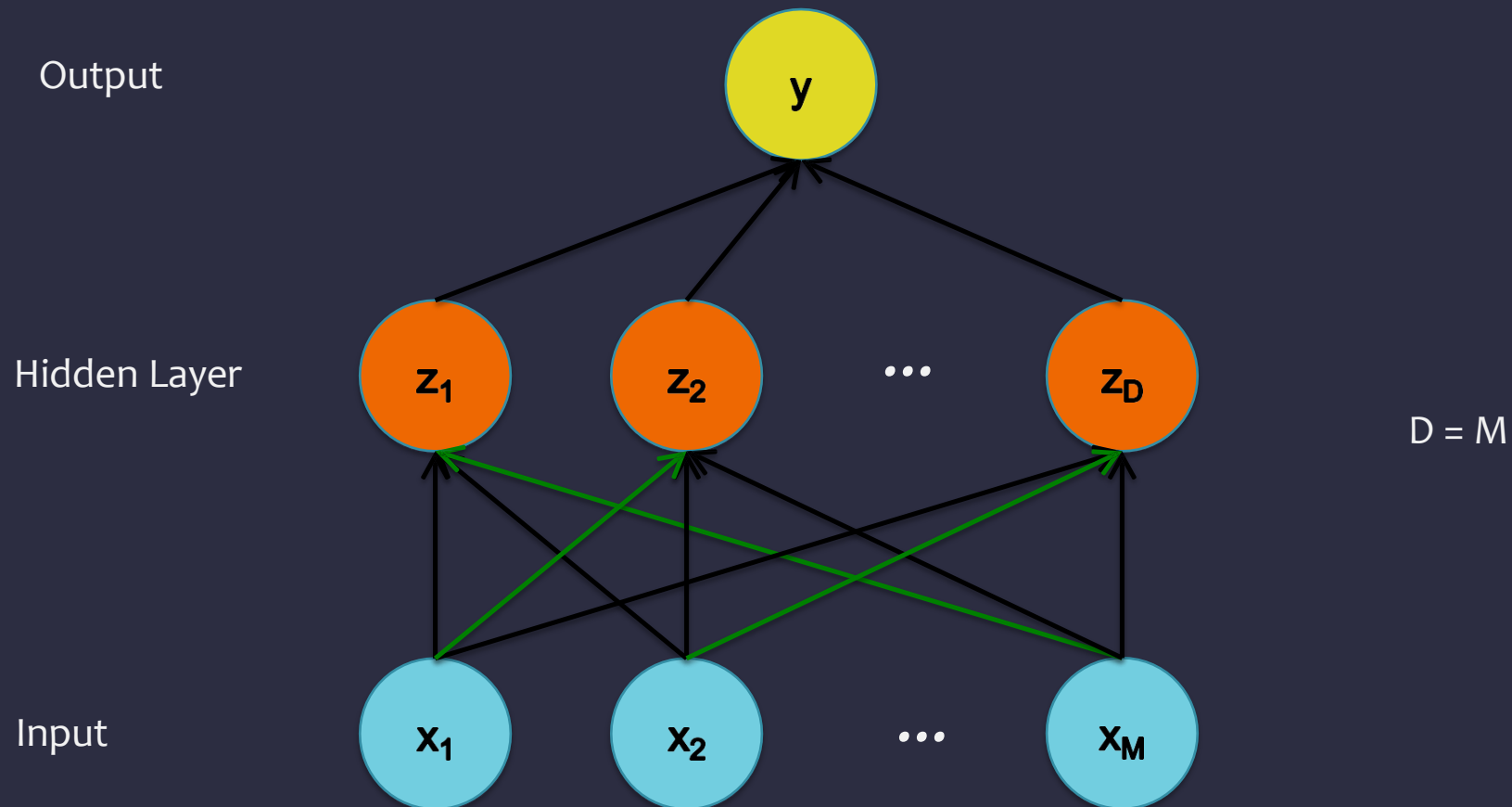
Building a Neural Net

Q: How many hidden units, D , should we use?



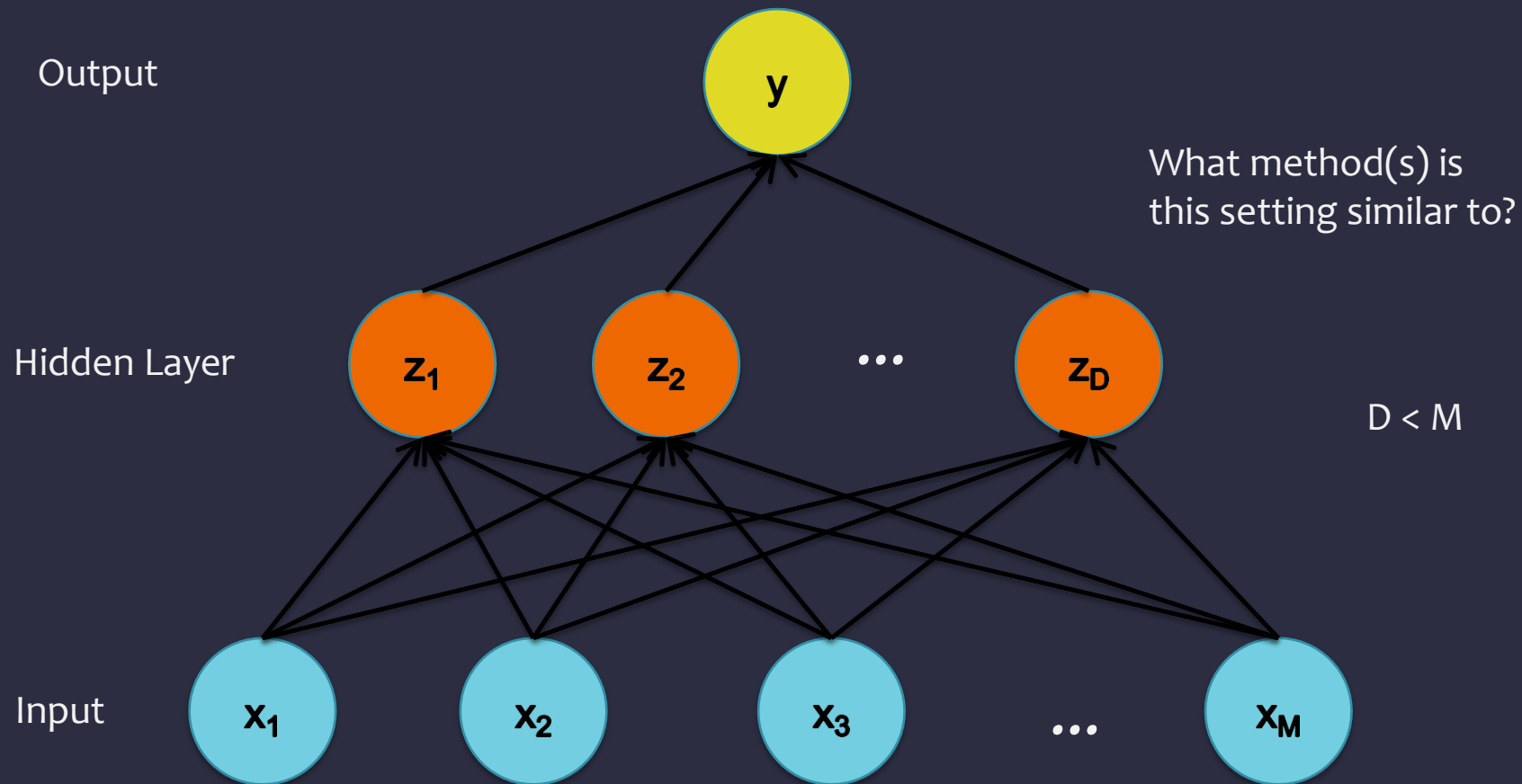
Building a Neural Net

Q: How many hidden units, D , should we use?



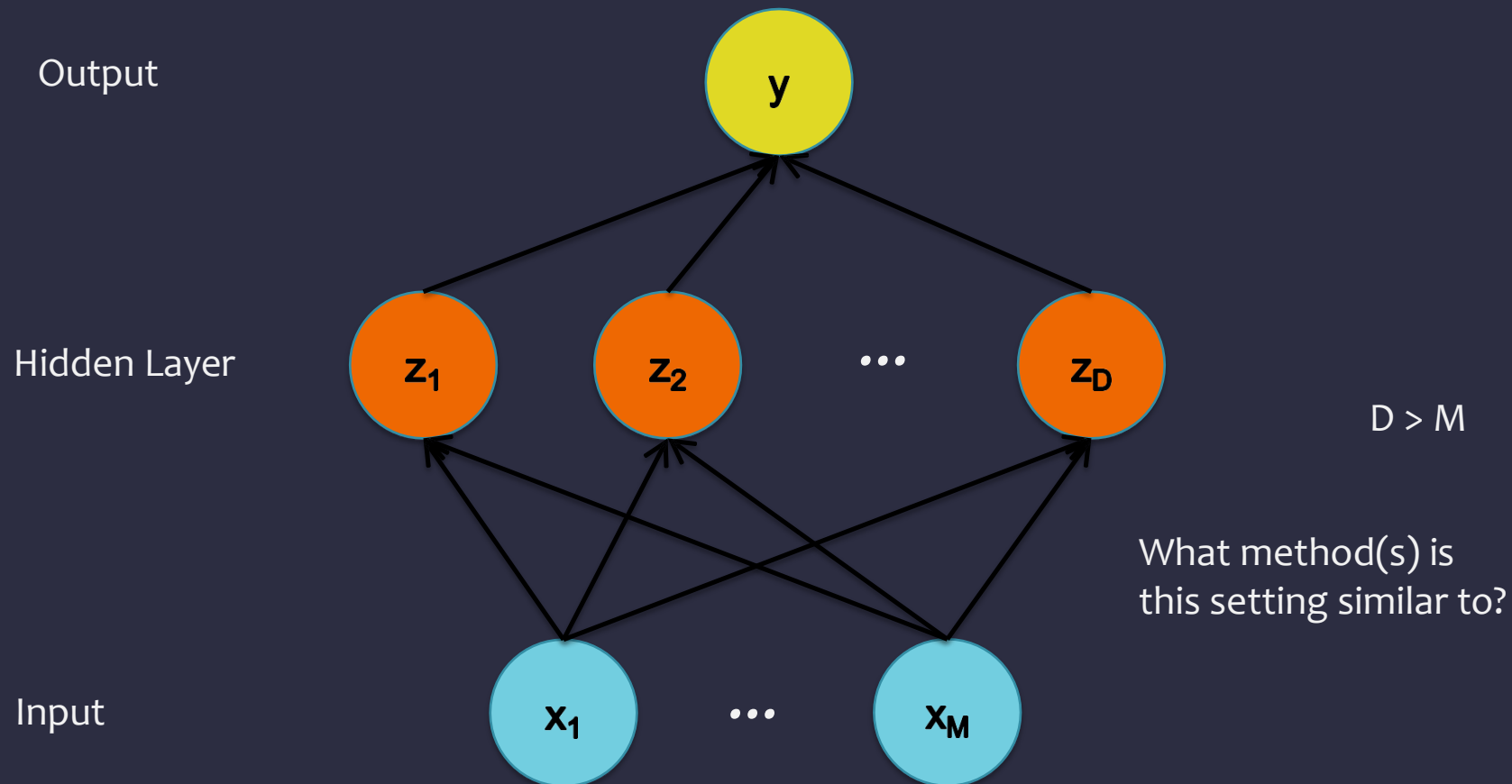
Building a Neural Net

Q: How many hidden units, D , should we use?



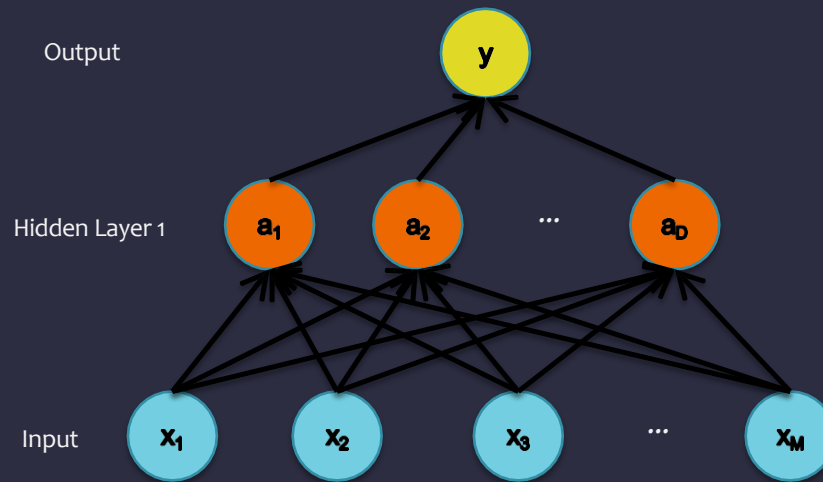
Building a Neural Net

Q: How many hidden units, D , should we use?



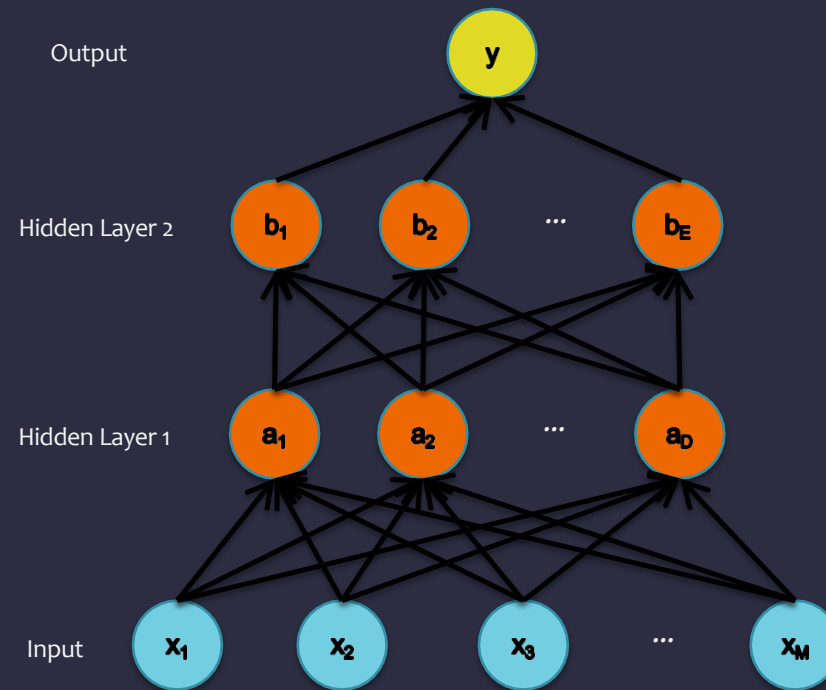
Deeper Networks

Q: How many layers should we use?



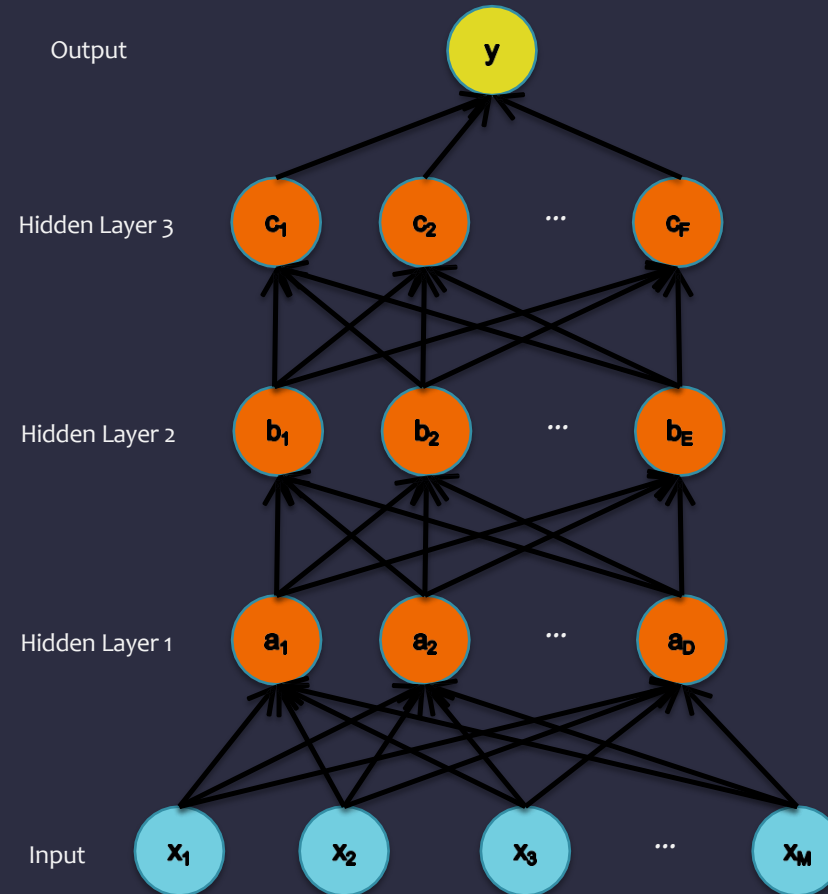
Deeper Networks

Q: How many layers should we use?



Deeper Networks

Q: How many layers should we use?



Deeper Networks

Q: How many layers should we use?

- **Theoretical answer:**

- A neural network with 1 hidden layer is a **universal function approximator**
- Cybenko (1989): For any continuous function $g(\mathbf{x})$, there exists a 1-hidden-layer neural net $h_{\theta}(\mathbf{x})$ s.t. $|h_{\theta}(\mathbf{x}) - g(\mathbf{x})| < \epsilon$ for all \mathbf{x} , assuming sigmoid activation functions

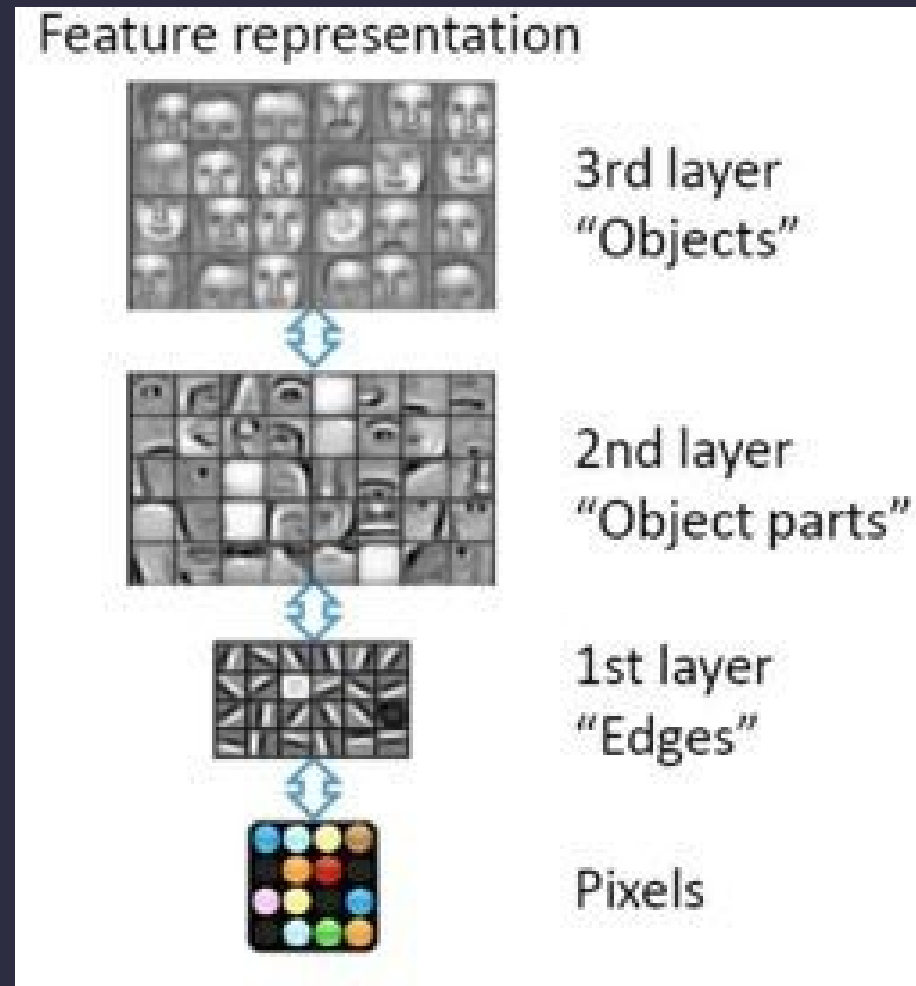
- **Empirical answer:**

- Before 2015 : “Deep networks (e.g. 3 or more hidden layers) are too hard to train”
- After 2015: “Deep networks are easier to train than shallow networks (e.g. 2 or fewer layers) for many problems”

Big caveat: You need to know and use the right tricks.

Different Levels of Abstraction

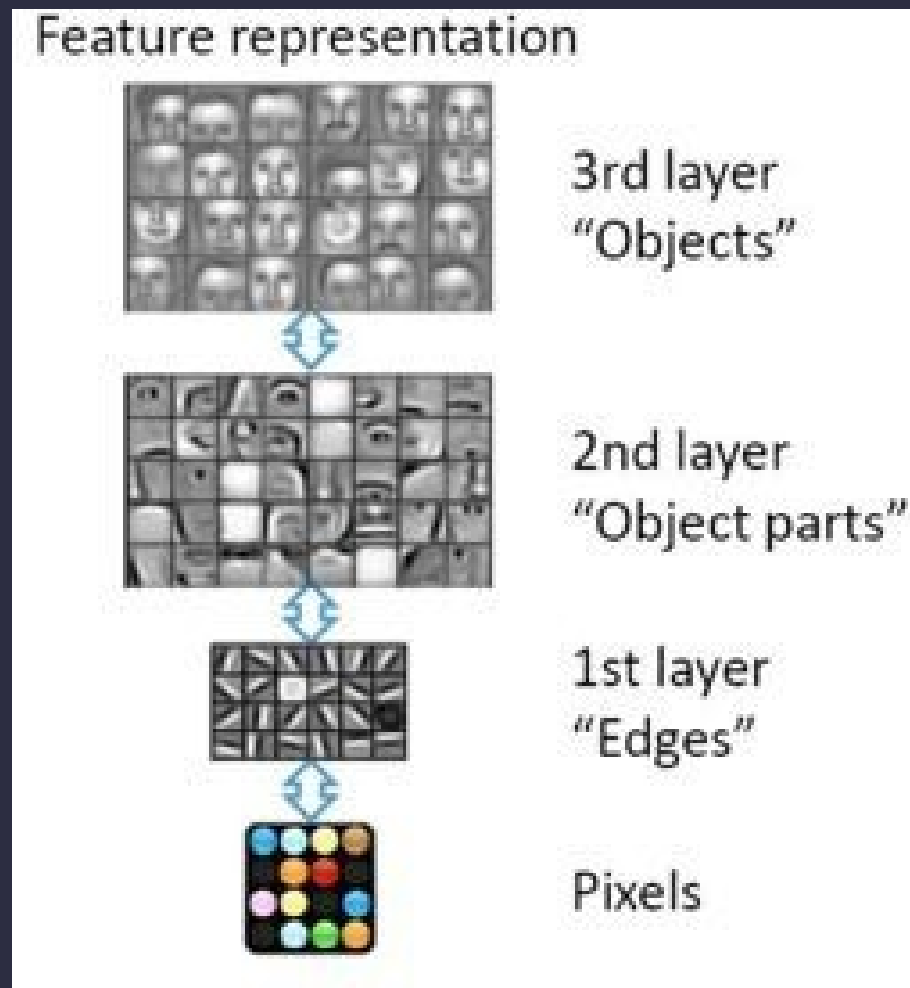
- We don't know the “right” levels of abstraction
- So let the model figure it out!



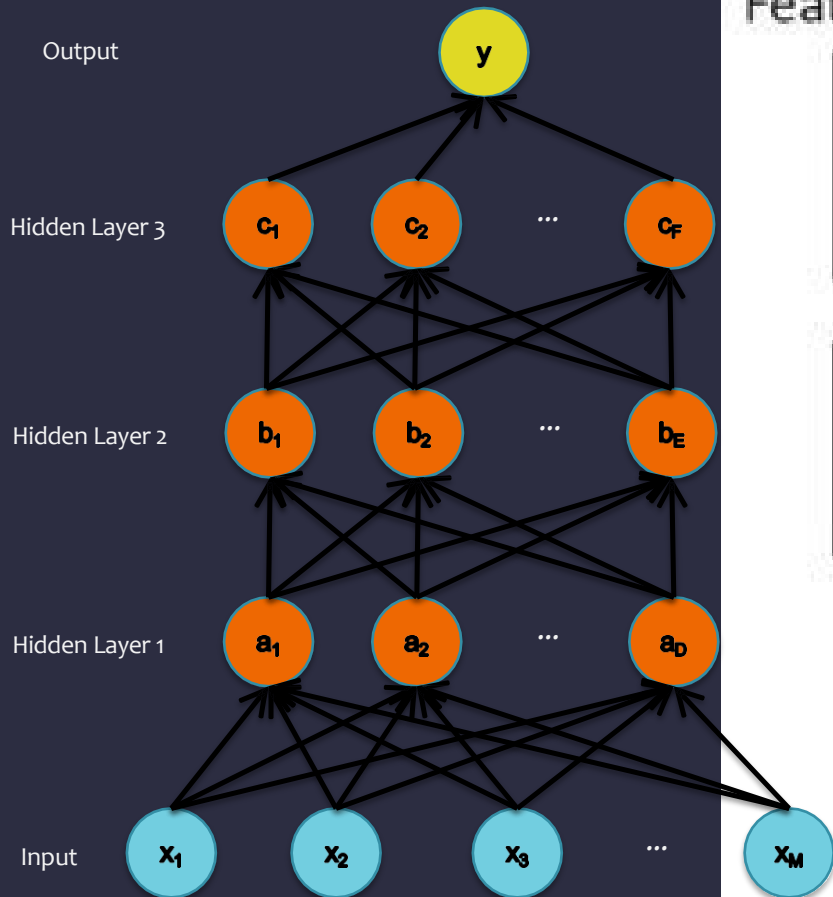
Different Levels of Abstraction

Face Recognition:

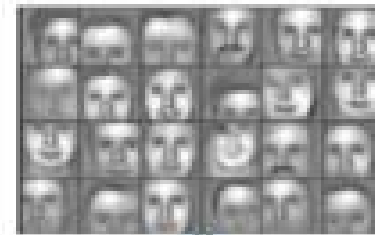
- Deep Network can build up increasingly higher levels of abstraction
- Lines, parts, regions



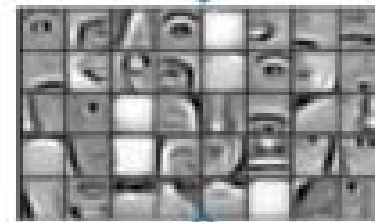
Different Levels of Abstraction



Feature representation



3rd layer
"Objects"



2nd layer
"Object parts"



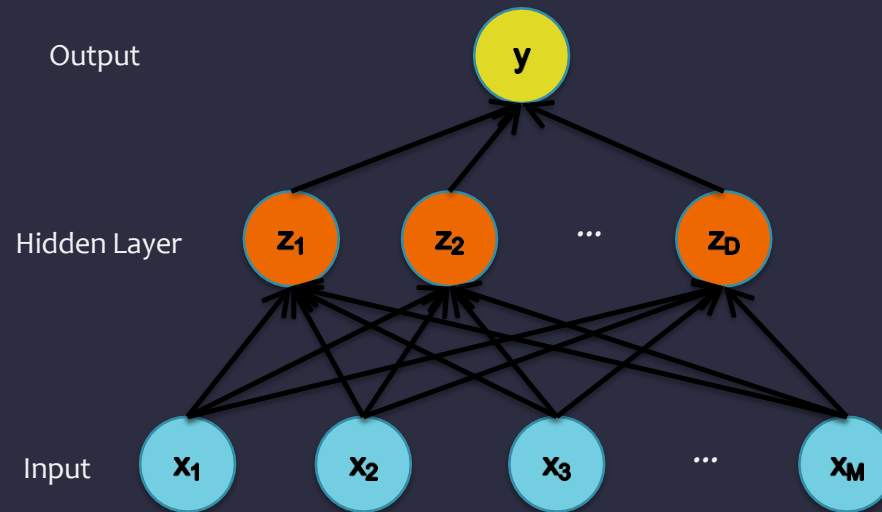
1st layer
"Edges"



Pixels

Activation Functions

Neural Network with sigmoid activation functions



(F) Loss

$$J = \frac{1}{2}(y - y^*)^2$$

(E) Output (sigmoid)

$$y = \frac{1}{1 + \exp(-b)}$$

(D) Output (linear)

$$b = \sum_{j=0}^D \beta_j z_j$$

(C) Hidden (sigmoid)

$$z_j = \frac{1}{1 + \exp(-a_j)}, \quad \forall j$$

(B) Hidden (linear)

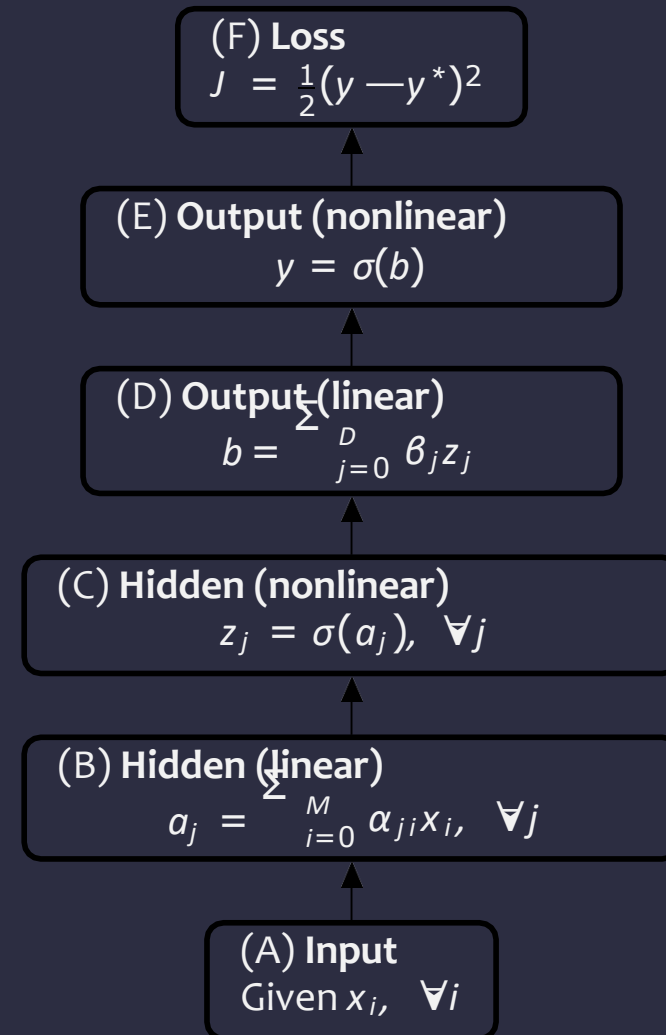
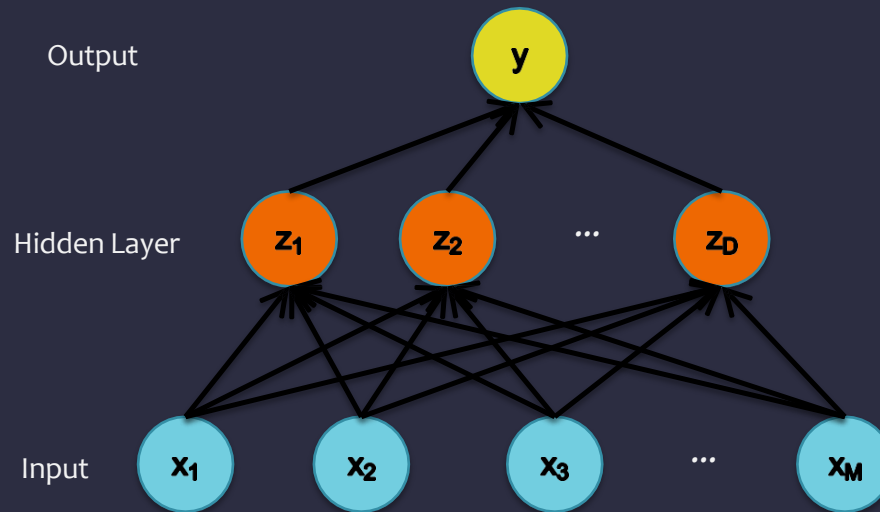
$$a_j = \sum_{i=0}^M \alpha_{ji} x_i, \quad \forall j$$

(A) Input

Given $x_i, \quad \forall i$

Activation Functions

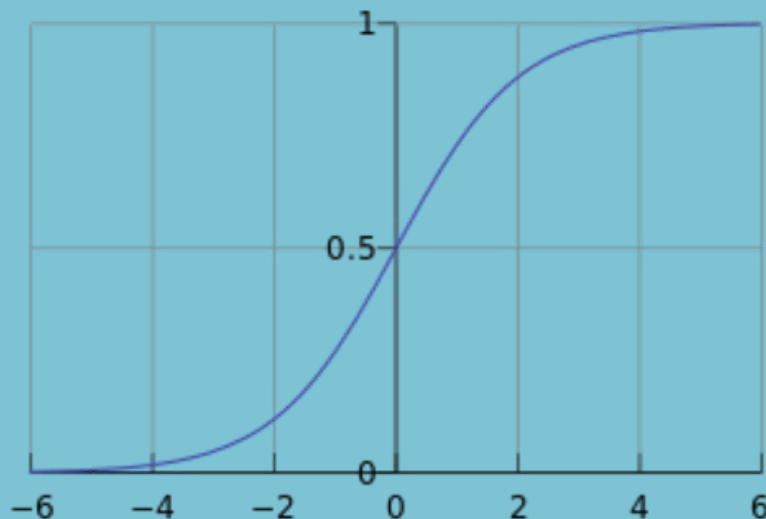
Neural Network with arbitrary nonlinear activation functions



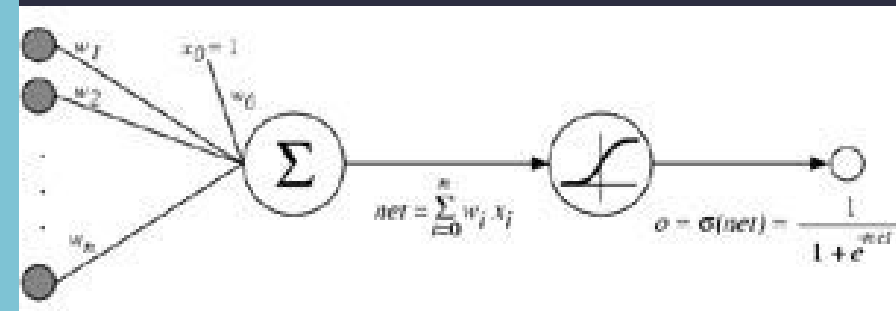
Activation Functions

Sigmoid / Logistic Function

$$\text{logistic}(u) \equiv \frac{1}{1 + e^{-u}}$$

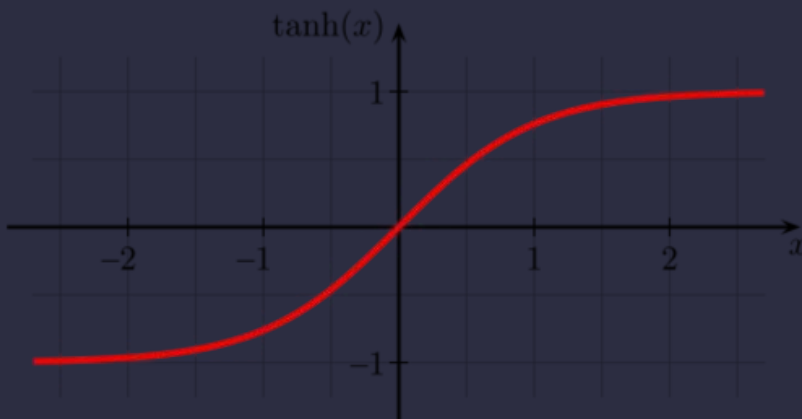


Activation function (nonlinearity) is sigmoid function...



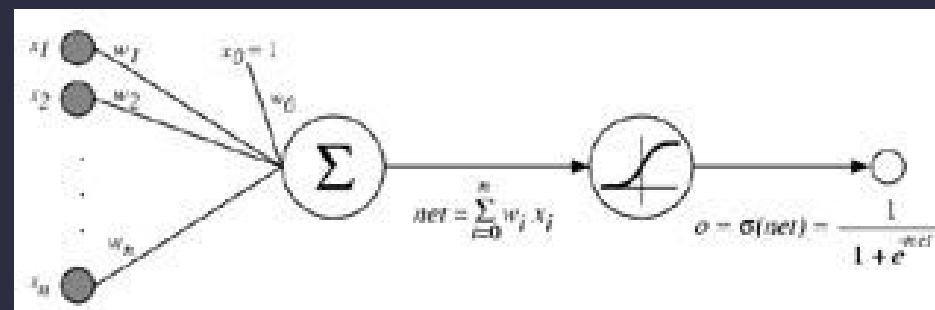
Activation Functions

- A new change: modifying the nonlinearity
 - The logistic is not widely used in modern ANNs



Alternate 1:
tanh

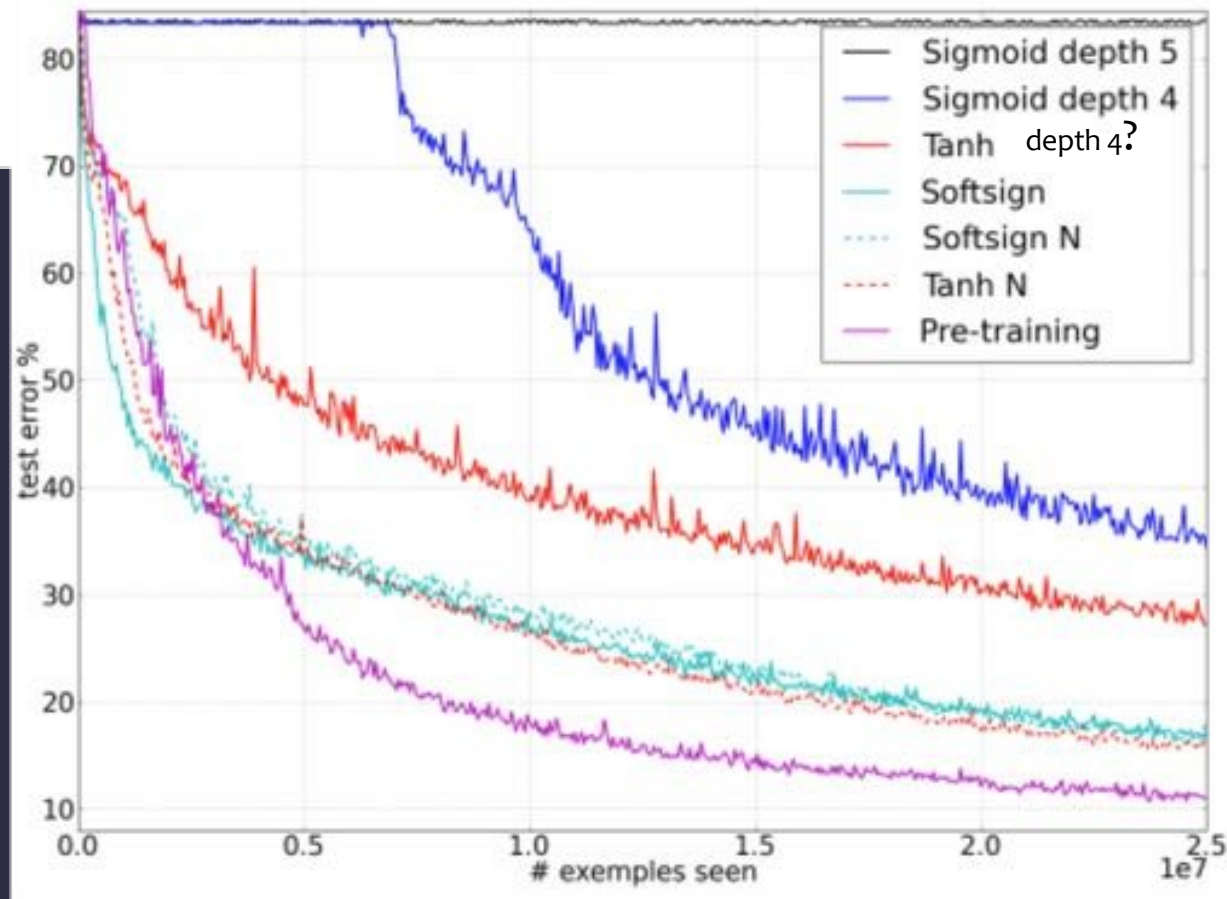
Like logistic function but
shifted to range $[-1, +1]$



Slide from William Cohen

Understanding the difficulty of training deep feedforward neural networks

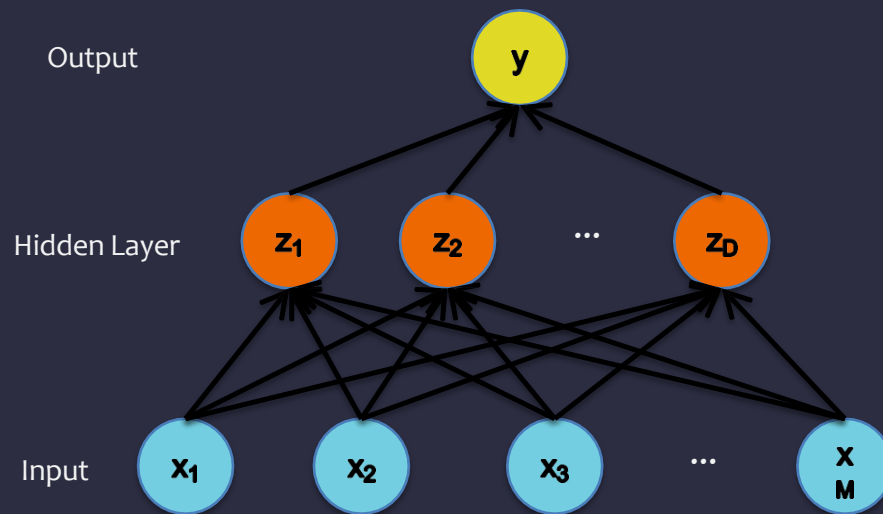
AI Stats 2010



sigmoid
vs.
tanh

Decision Functions

Neural Network for Classification



(E) Output (sigmoid)

$$y = \frac{1}{1 + \exp(-b)}$$

(D) Output (linear)

$$b = \sum_{j=0}^D \beta_j z_j$$

(C) Hidden (sigmoid)

$$z_j = \frac{1}{1 + \exp(-a_j)}, \quad \forall j$$

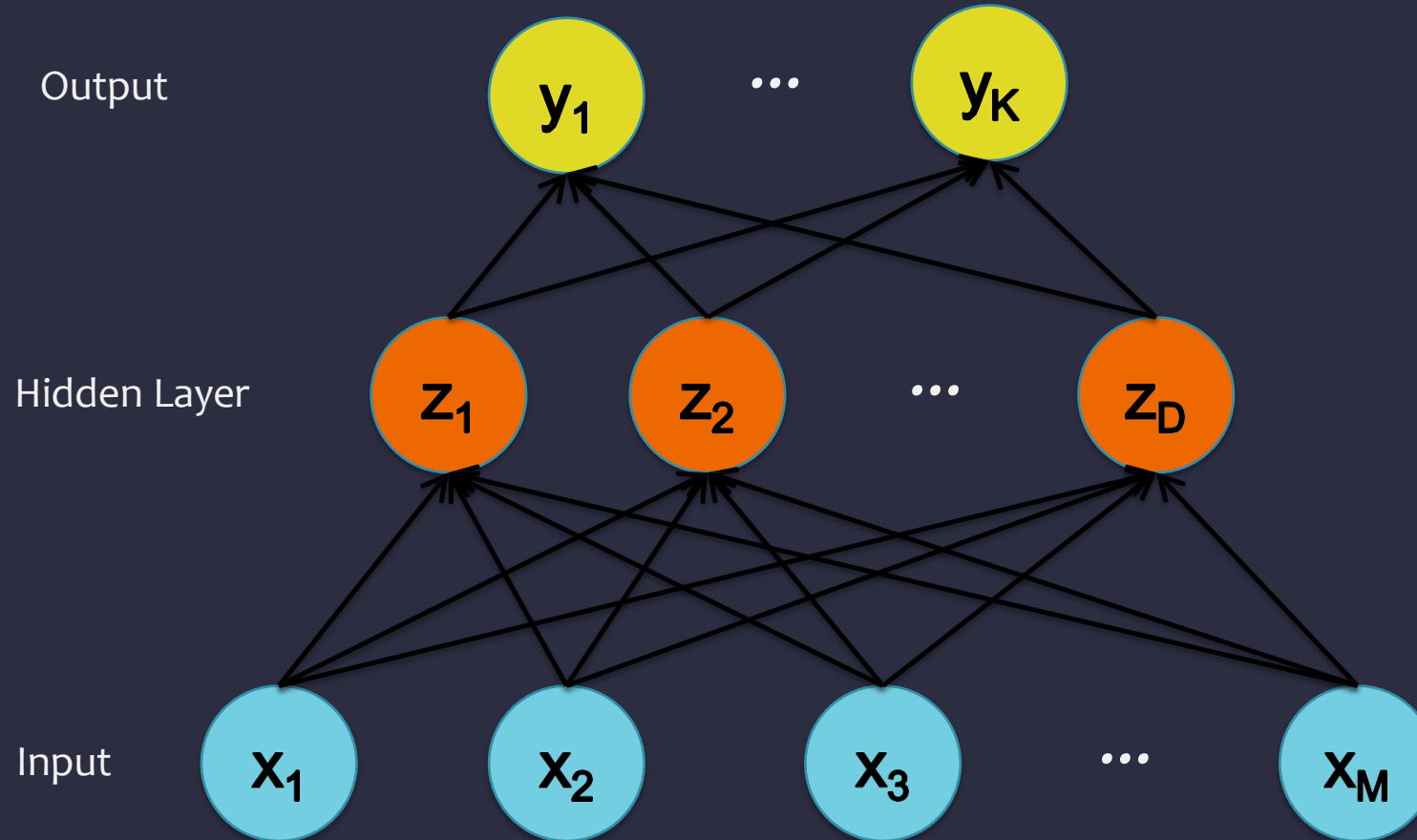
(B) Hidden (linear)

$$a_j = \sum_{i=0}^M \alpha_{ji} x_i, \quad \forall j$$

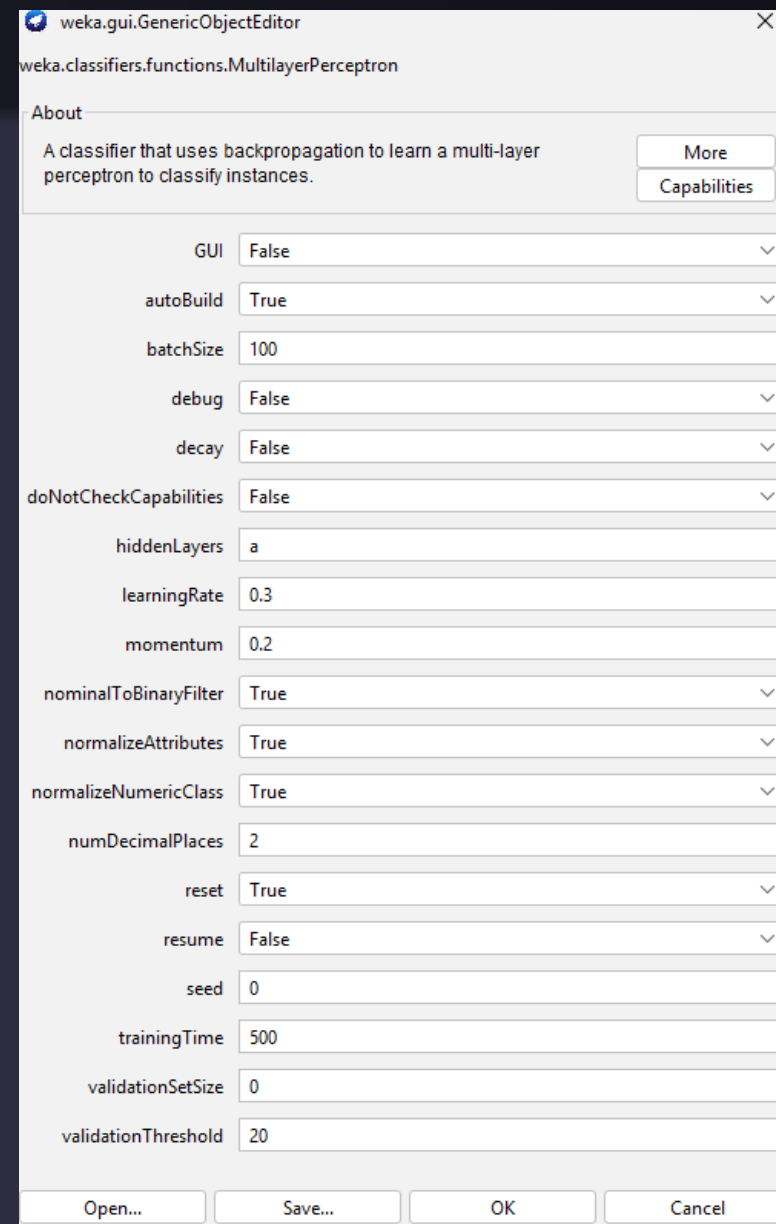
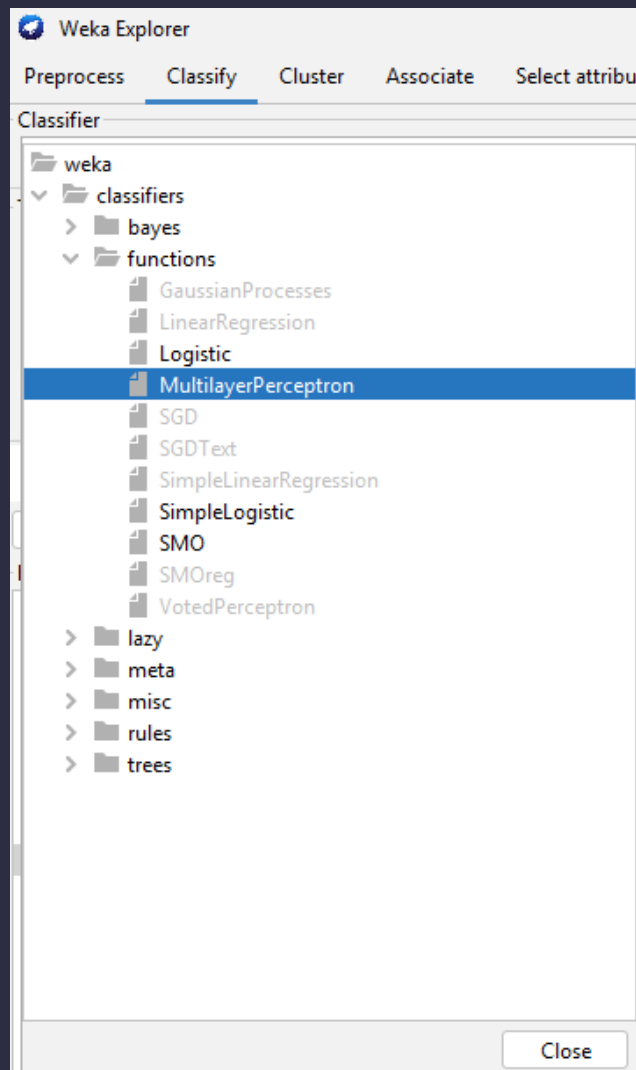
(A) Input

Given $x_i, \quad \forall i$

Multi-Class Output



NN on Weka



NN on Weka

Weka Explorer

Preprocess **Classify** Cluster Associate Select attributes Visualize

Classifier: Choose **MultilayerPerceptron -L 0.3 -M 0.2 -N 500 -V 0 -S 0 -E 20 -H a**

Test options

☐ Use training set

☐ Supplied test set

☒ Cross-validation Folds **10**

☐ Percentage split % **80**

(Nom) class

Result list (right-click for options)

- 17:24:16 - bayes.NaiveBayes
- 17:25:42 - bayes.NaiveBayes
- 17:25:52 - bayes.NaiveBayes
- 17:26:29 - bayes.NaiveBayesMultinomial
- 17:26:33 - bayes.NaiveBayes
- 17:26:34 - bayes.NaiveBayes
- 23:12:04 - trees.DecisionStump
- 23:12:28 - trees.J48
- 23:42:38 - lazy.IBk
- 23:58:23 - functions.MultilayerPerceptron**

Classifier output

Attrib sepalwidth 3.1250096866676538
 Attrib petallength -4.133137022912303
 Attrib petalwidth -4.079589727871457

Sigmoid Node 5

Inputs	Weights
Attrib sepalwidth	-1.2158878822058794
Attrib sepalwidth	-3.5332821317534946
Attrib petallength	8.401834252274107
Attrib petalwidth	9.460215580472836

Class Iris-setosa
 Input
 Node 0

Class Iris-versicolor
 Input
 Node 1

Class Iris-virginica
 Input
 Node 2

Time taken to build model: 0.04 seconds

=== Stratified cross-validation ===

=== Summary ===

Metric	Value	Percentage
Correctly Classified Instances	146	97.3333 %
Kappa statistic	0.96	
Mean absolute error	0.0327	
Root mean squared error	0.1291	
Relative absolute error	7.3555 %	
Root relative squared error	27.3796 %	
Total Number of Instances	150	

=== Detailed Accuracy By Class ===

	TP Rate	FP Rate	Precision	Recall	F-Measure	MCC	ROC Area	PRC Area	Class
	1,000	0,000	1,000	1,000	1,000	1,000	1,000	1,000	Iris-setosa
	0,960	0,020	0,960	0,960	0,960	0,940	0,996	0,993	Iris-versicolor
	0,960	0,020	0,960	0,960	0,960	0,940	0,996	0,993	Iris-virginica
Weighted Avg.	0,973	0,013	0,973	0,973	0,973	0,960	0,998	0,995	

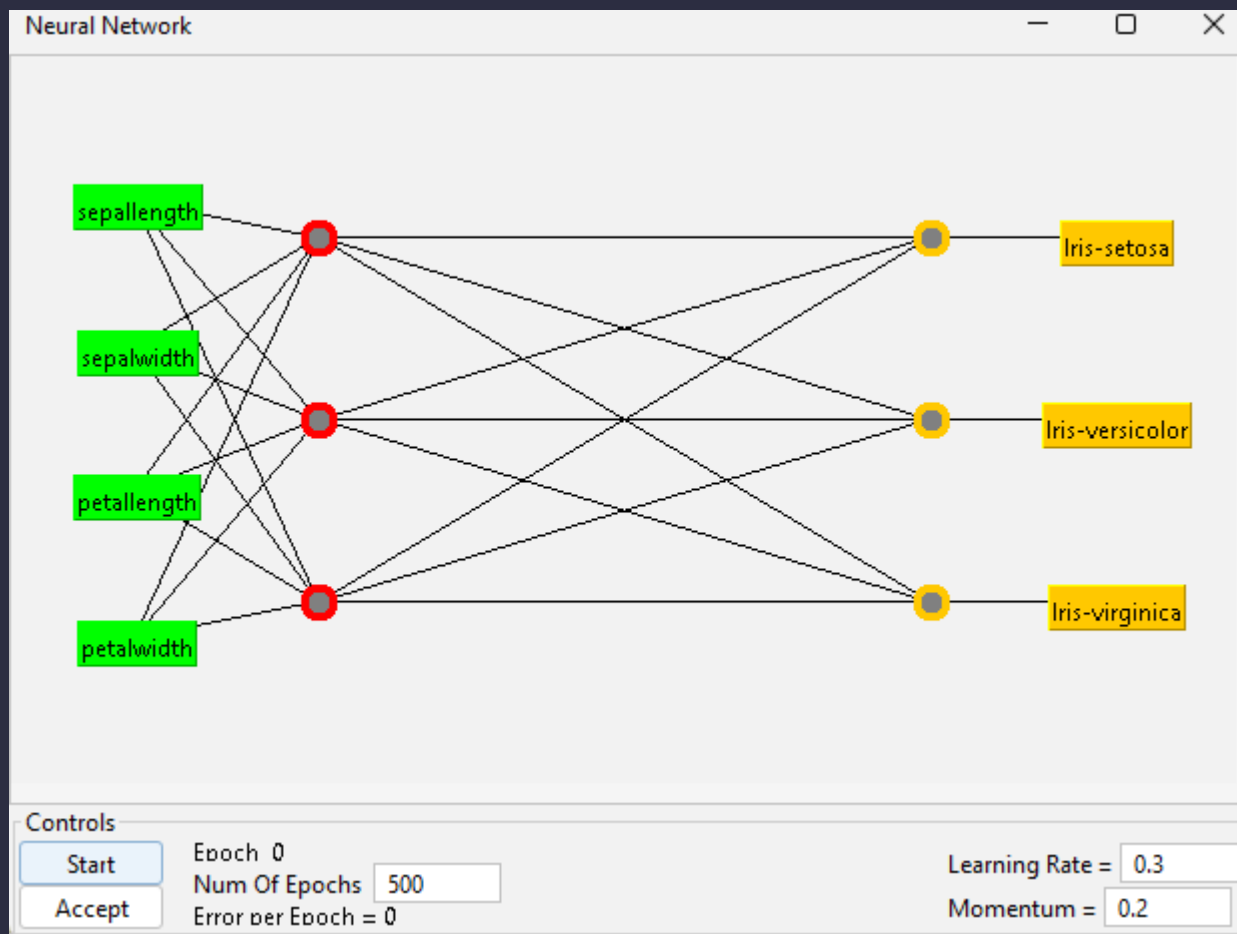
=== Confusion Matrix ===

```

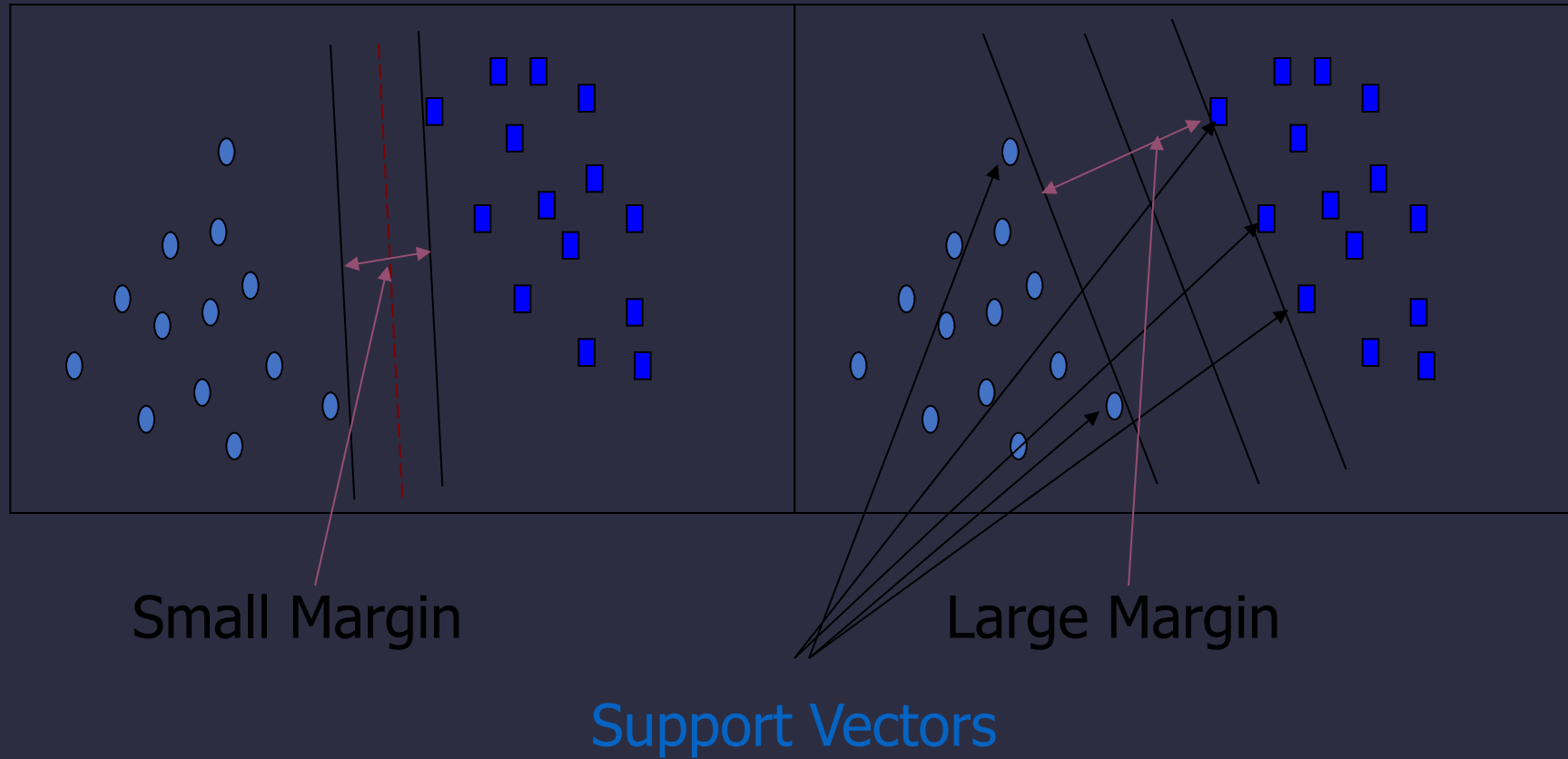
a b c <-- classified as
50 0 0 | a = Iris-setosa
0 48 2 | b = Iris-versicolor
0 2 48 | c = Iris-virginica

```

NN on Weka



SVM – Support Vector Machines

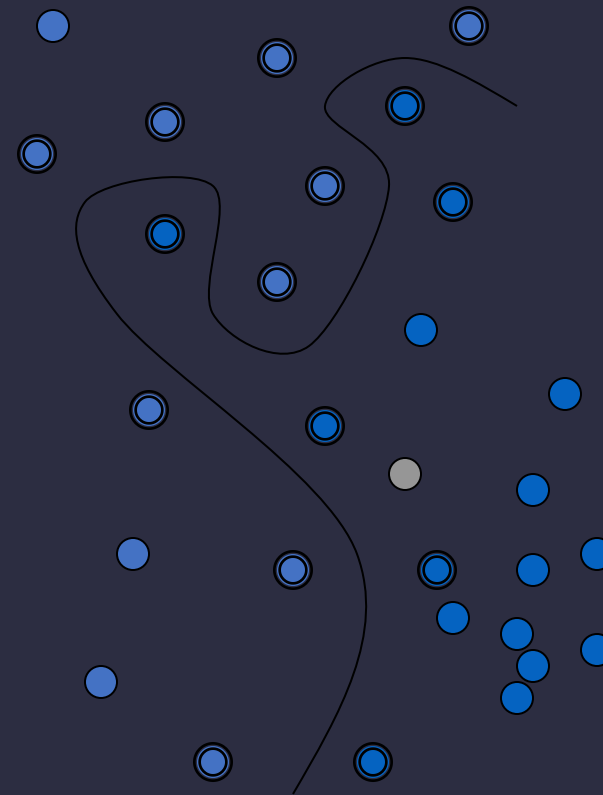


Support vector machine(SVM).

- Classification is essentially finding the best boundary between classes.
- Support vector machine finds the best boundary points called support vectors and build classifier on top of them.
- Linear and Non-linear support vector machine.

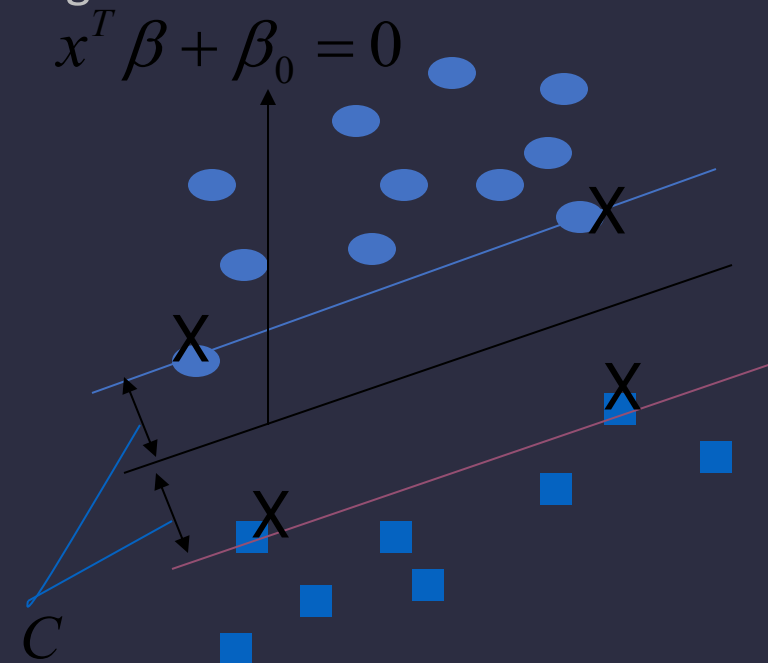
Example of general SVM

The dots with shadow around them are support vectors. Clearly they are the best data points to represent the boundary. The curve is the separating boundary.

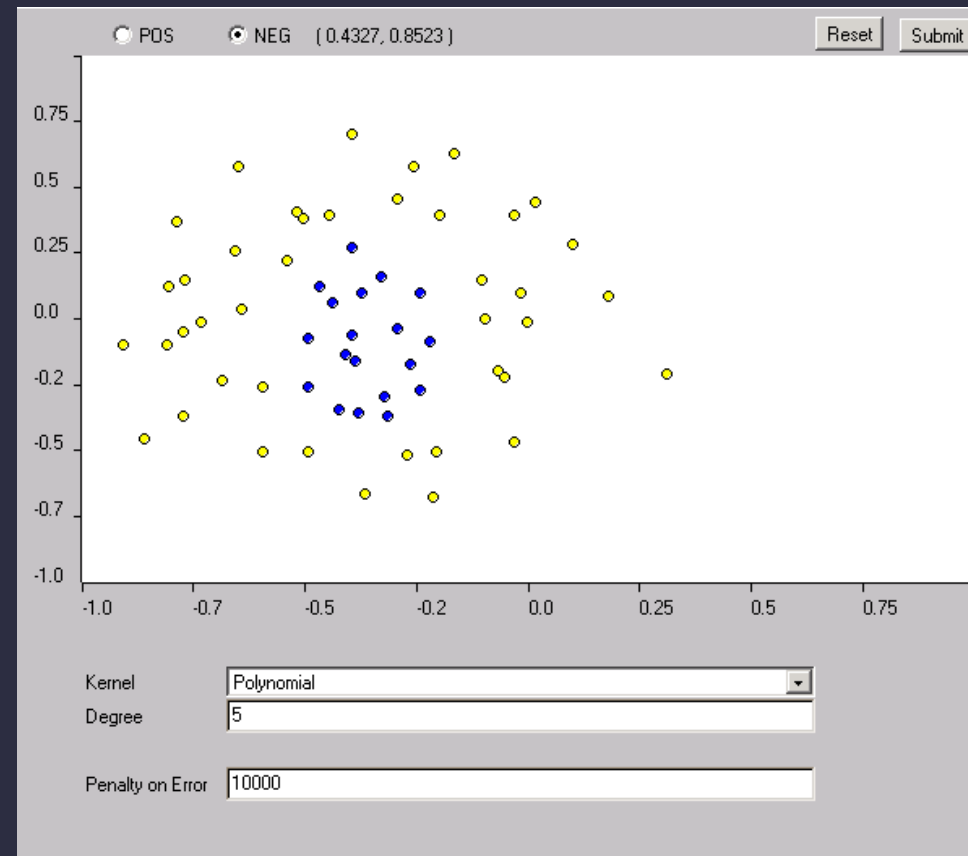


Optimal Hyper plane, separable case.

- In this case, class 1 and class 2 are separable.
- The representing points are selected such that the margin between two classes are maximized.
- Crossed points are support vectors.



Example of Non-linear SVM

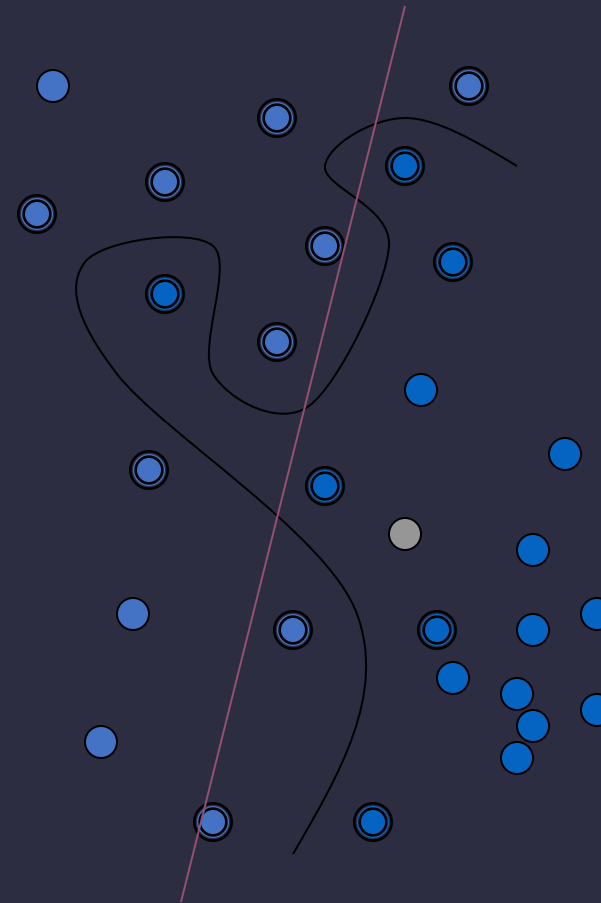


General SVM

This classification problem clearly do not have a good optimal linear classifier.

Can we do better?

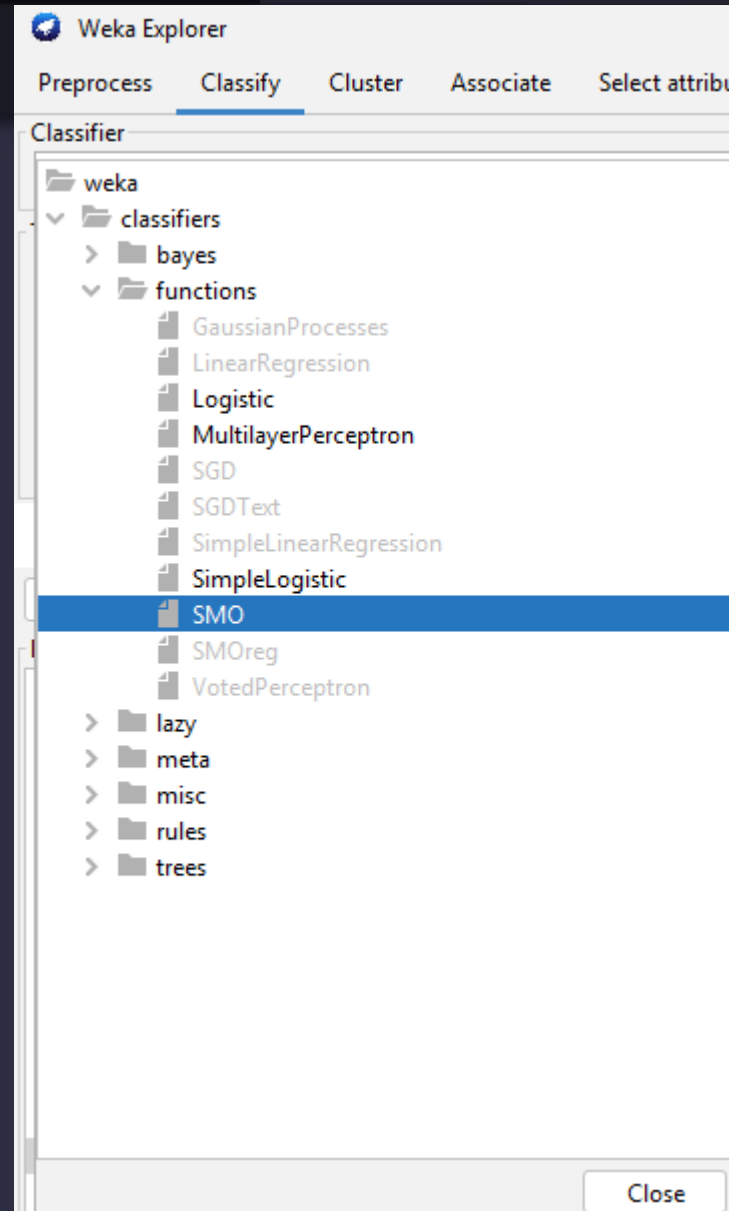
A non-linear boundary as shown will do fine.



General SVM Cont.

- The idea is to map the feature space into a much bigger space so that the boundary is linear in the new space.
- Generally linear boundaries in the enlarged space achieve better training-class separation, and it translates to non-linear boundaries in the original space.

SVM on Veka



SVM on Veka

weka.gui.GenericObjectEditor

weka.classifiers.functions.SMO

About

Implements John Platt's sequential minimal optimization algorithm for training a support vector classifier.

More

Capabilities

batchSize 100

buildCalibrationModels False

c 1.0

calibrator Choose **Logistic** -R 1.0E-8 -M -1 -num-decimal-places 4

checksTurnedOff False

debug False

doNotCheckCapabilities False

epsilon 1.0E-12

filterType Normalize training data

kernel Choose **PolyKernel** -E 1.0 -C 250007

numDecimalPlaces 2

numFolds -1

randomSeed 1

toleranceParameter 0.001

Open... Save... OK Cancel

SVM on Veka

Weka Explorer

Preprocess Classify Cluster Associate Select attributes Visualize

Classifier

Choose **SMO** -C 1.0 -L 0.001 -P 1.0E-12 -N 0 -V -1 -W 1 -K "weka.classifiers.functions.supportVector.PolyKernel -E 1.0 -C 250007" -calibrator "weka.classifiers.functions.Logistic -R 1.0E-8 -M -1 -"

Test options

☐ Use training set

☐ Supplied test set

☒ Cross-validation Folds **10**

☐ Percentage split % **80**

More options...

(Nom) class

Start Stop

Result list (right-click for options)

- 17:24:16 - bayes.NaiveBayes
- 17:25:42 - bayes.NaiveBayes
- 17:25:52 - bayes.NaiveBayes
- 17:26:29 - bayes.NaiveBayesMultinomial
- 17:26:33 - bayes.NaiveBayes
- 17:26:34 - bayes.NaiveBayes
- 23:12:04 - trees.DecisionStump
- 23:12:28 - trees.J48
- 23:42:38 - lazy.IBk
- 23:58:23 - functions.MultilayerPerceptron
- 23:58:55 - functions.MultilayerPerceptron
- 23:59:21 - functions.MultilayerPerceptron
- 23:59:24 - functions.MultilayerPerceptron
- 23:59:38 - functions.MultilayerPerceptron
- 00:09:40 - functions.SMO**

Classifier output

```
+ 1.4777 * (normalized) petalwidth
- 1.1668
```

Number of kernel evaluations: 284 (68.996% cached)

Classifier for classes: Iris-versicolor, Iris-virginica

BinarySMO

Machine linear: showing attribute weights, not support vectors.

```
0.3176 * (normalized) sepalength
+ -0.863 * (normalized) sepalwidth
+ 3.0543 * (normalized) petallength
+ 4.0815 * (normalized) petalwidth
- 4.5924
```

Number of kernel evaluations: 453 (61.381% cached)

Time taken to build model: 0.01 seconds

=== Stratified cross-validation ===

=== Summary ===

Correctly Classified Instances	144	96	%
Kappa statistic	0.94		
Mean absolute error	0.2311		
Root mean squared error	0.288		
Relative absolute error	52	%	
Root relative squared error	61.101	%	
Total Number of Instances	150		

=== Detailed Accuracy By Class ===

	TP Rate	FP Rate	Precision	Recall	F-Measure	MCC	ROC Area	PRC Area	Class
	1,000	0,000	1,000	1,000	1,000	1,000	1,000	1,000	Iris-setosa
	0,980	0,050	0,907	0,980	0,942	0,913	0,965	0,896	Iris-versicolor
	0,900	0,010	0,978	0,900	0,938	0,910	0,970	0,930	Iris-virginica
Weighted Avg.	0,960	0,020	0,962	0,960	0,960	0,941	0,978	0,942	

=== Confusion Matrix ===

```
a b c <-- classified as
50 0 0 | a = Iris-setosa
0 49 1 | b = Iris-versicolor
0 5 45 | c = Iris-virginica
```

The Problem of Feature Selection

- Large number of features; sometimes greater than 100.
- The number of combinations can be well over a billion!



- Is there a way to search for an optimal set of features in reasonable time and with reasonable computation power?

Different ways to search for this needle

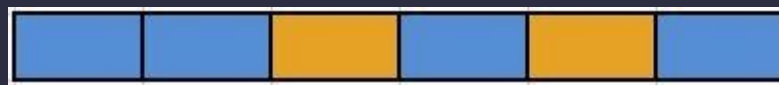
- Evaluate every possible combination to come up with the best combination – the brute force method!
- Step-up/step-down methods that add or remove a feature at a time and evaluate model performance.
- Use genetic algorithms (GA) for searching this huge solution space.

Genetic Algorithms (GA)

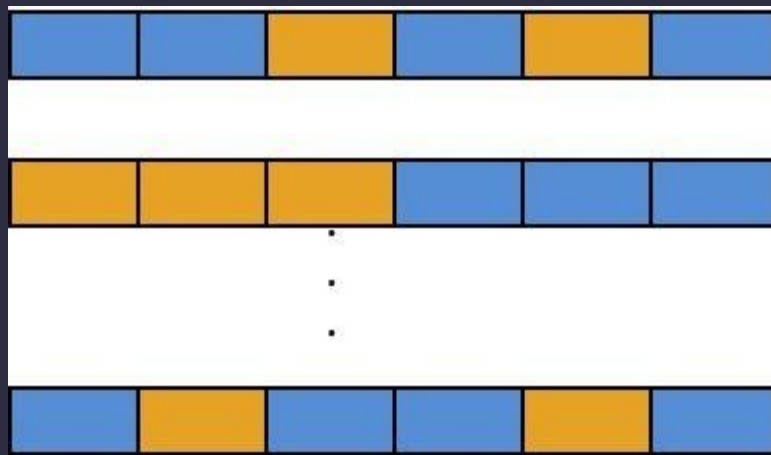
- This is a high level simulation of a biologically inspired adaptive system – evolution.
- Using a simple set of rules, this system can have emergent behaviour that makes it useful for various applications.
- GA have been used in applications such as
 - predicting the structure of proteins
 - training neural networks
- Here, I will talk about the use of GA for searching through the feature space to select an optimal set of features.

Terms associated with GA

- **Chromosome** – a potential solution to the problem. A common way to represent solutions is using binary numbers.

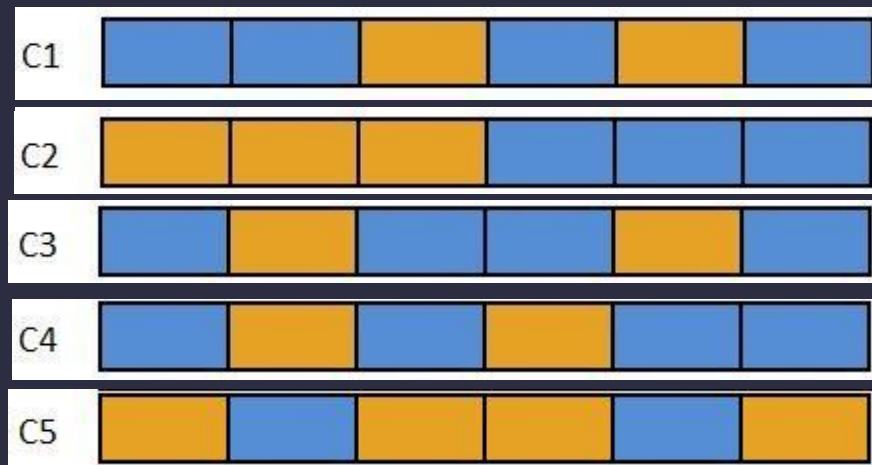


- **Population** – a set of chromosomes belonging to a generation.



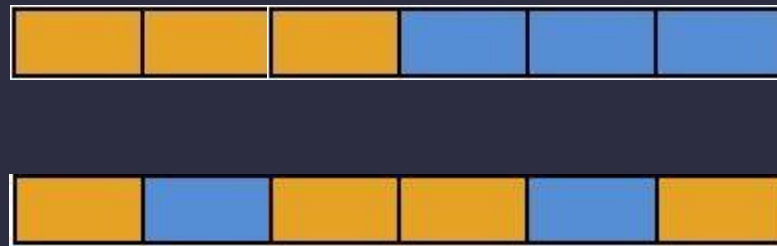
Terms associated with GA

- **Fitness** – a metric to evaluate how well a particular solution solves the problem.
- **Generation** – each iteration of the algorithm.
- **Selection** – a process by which some chromosomes of a population are chosen for generating new solutions.

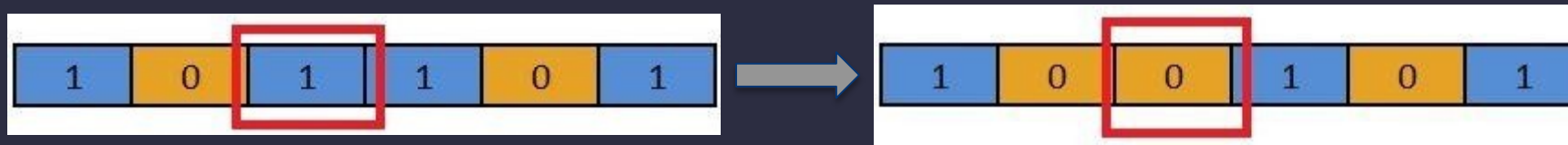


Terms associated with GA

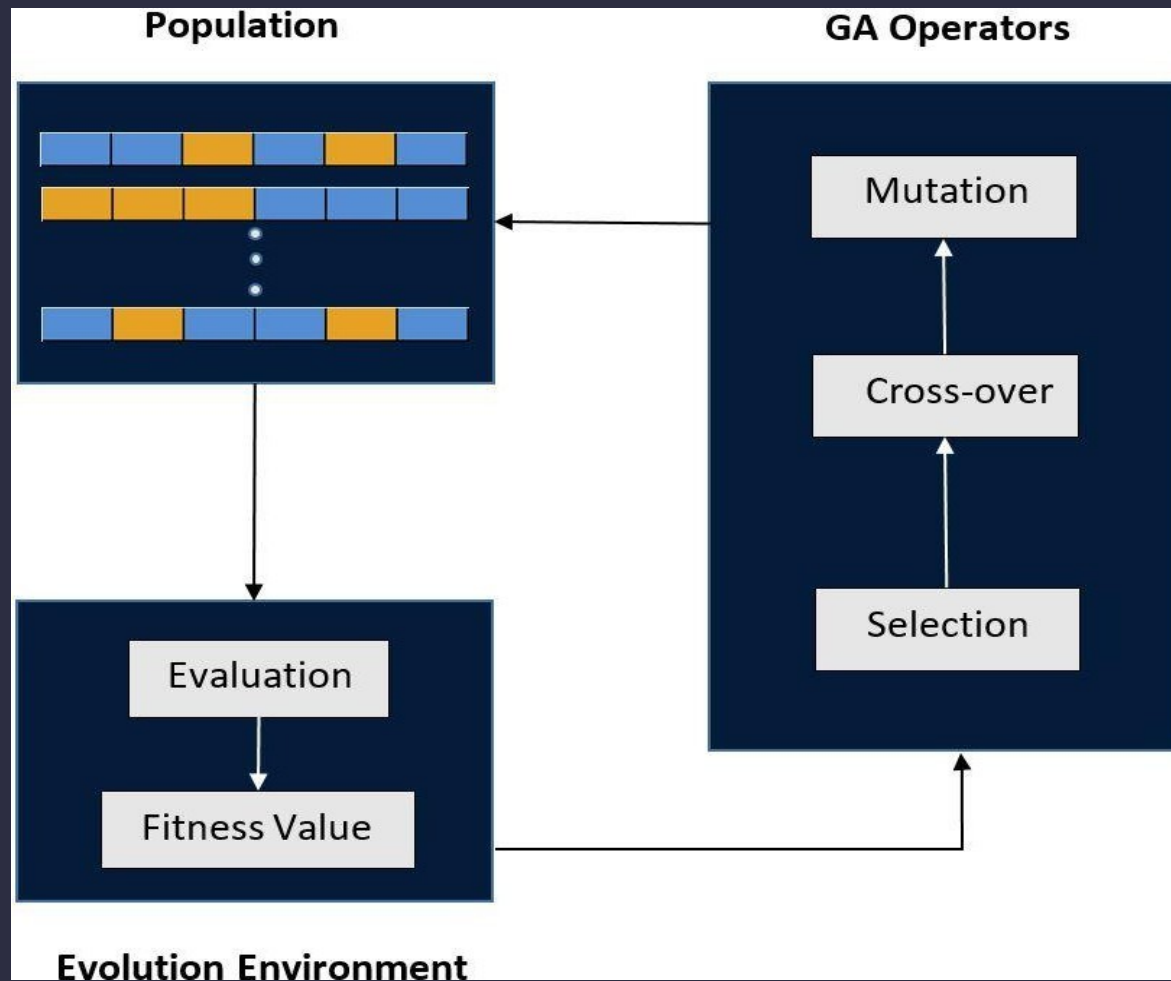
- **Cross-over** – is the process of exchange of information between selected chromosomes.



- **Mutation** – random changes in chromosomes.



Schematic of a GA



Performance

